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Electronic structure and lattice dynamics of 1T-VSe₂: Origin of the three-dimensional charge density wave

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To characterize in detail the charge density wave (CDW) transition of 1T-VSe₂, its electronic structure and lattice dynamics are comprehensively studied by means of x-ray diffraction, muon spectroscopy, angle resolved photoemission (ARPES), diffuse and inelastic x-ray scattering, and state-of-the-art first-principles density functional theory calculations. Resonant elastic x-ray scattering does not show any resonant enhancement at either V or Se, indicating that the CDW peak at the K edges describes a purely structural modulation of the electronic ordering. ARPES experiments identify (i) a pseudogap at $T > T_{\rm CDW}$, which leads to a depletion of the density of states in the ML-M'L' plane at $T < T_{\rm CDW}$, and (ii) anomalies in the electronic dispersion reflecting a sizable impact of phonons on it. A diffuse scattering precursor, characteristic of soft phonons, is observed at room temperature (RT) and leads to the full collapse of the low-energy phonon (ω_1) with propagation vector (0.25 0 -0.3) r.l.u. We show that the frequency and linewidth of this mode are anisotropic in momentum space, reflecting the momentum dependence of the electron-phonon interaction (EPI), hence demonstrating that the origin of the CDW is, to a much larger extent, due to the momentum dependent EPI with a small contribution from nesting. The pressure dependence of the ω_1 soft mode remains nearly constant up to 13 GPa at RT, with only a modest softening before the transition to the high-pressure monoclinic C2/m phase. The wide set of experimental data is well captured by our state-of-the art first-principles anharmonic calculations with the

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inclusion of van der Waals corrections in the exchange-correlation functional. The comprehensive description of the electronic and dynamical properties of VSe₂ reported here adds important pieces of information to the understanding of the electronic modulations in the family of transition-metal dichalcogenides.

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I. INTRODUCTION

The understanding of the origin of the charge density wave (CDW) and its coexistence/competition with other complex phenomena, like superconductivity (SC) [1–3] or magnetism [4,5], is one of the main challenges in condensed matter physics. Cuprates aside [6–12], layered two-dimensional transition metal dichalcogenides (2D-TMDs) have become the prototypical example for materials with a large variety of ground states that populate their phase diagrams, making them an ideal platform for advanced electronic applications [13]. An intriguing combination of correlated electronic states such as CDWs [14], SC [15], excitonic instabilities [16], and heavy fermions [17], as well as topological [18] and spin liquid [19] behaviors have been reported both in the bulk and monolayer limits, despite their relatively simple band structures.

At a microscopic level, the canonical Fermi surface nesting (FSN) scenario, originally devised to explain the Peierls transition in 1D, is questionable in higher dimensions and the critical role of the electron-phonon interaction (EPI) has gained more popularity in determining the CDW modulation vector, \mathbf{q}_{CDW} [20]. Moreover, the reduced electronic screening in one and two dimensions enhances electronic correlations and drives the CDW transition concomitant with other ordering phenomena. The vivid debate about the CDW origin and its relation with other electronic orders is exemplified in (i) 2H-NbSe₂, where charge instabilities and SC occur below 33 and 7 K, respectively, and different experimental and theoretical approaches are being discussed [3,21-24]; and in (ii), 1T-TiSe₂, where a long-lasting controversy surrounds the origin and stabilization of the electronic modulation [25–28] and its possible chiral charge and orbital order [29–34].

The quasi-2D 1T-VSe₂ is another TMD subject to strong debate and the main focus of this paper. The structure consists of van der Waals (vdW) stacked layers of V atoms covalently bonded to Se within an octahedral coordination, as shown in Fig. 1(a). A three-dimensional (3D) CDW with propagation vector $\mathbf{q}_{CDW} = (0.25 \ 0 \ -0.3)$ r.l.u. emerges below $T_{CDW} =$ 110 K [35]. Soft x-ray angle resolved photoemission (ARPES) data reported asymmetric dog-bone electron pockets centered at the M and L points and assigned the origin of the CDW to a pure electronic mechanism considering that a nesting vector matches q_{CDW} [36]. Nevertheless, its fermiology turns out to be more complicated with a multiband Fermi surface [37], an unexpected band inversion, and emergent Dirac nodal arc with spin-momentum locking [38]. On the other hand, Raman scattering [39] and more recent ARPES experiments pointed to a more sophisticated mechanism, involving the coupling of optical phonons to the electronic background, as revealed by kinks in the electronic band dispersion [40]. The role of the EPI was further corroborated by inelastic x-ray scattering (IXS) experiments that unveiled a low-energy damped phonon over a wide range of the Brillouin zone (BZ) [41], in contrast to the sharp dip expected at 2k_F in the FSN scenario. This latter work also showed that the temperature dependence of the soft mode is critically determined by both anharmonicity and the weak vdW interactions and the momentum dependence of the EPI, collapsing at $T_{\rm CDW}$ following a mean-field behavior with critical exponent $\beta \sim \frac{1}{2}$. Furthermore, detailed transport experiments under pressure reported an anomalous enhancement of the CDW ordering temperature up to practically room temperature (RT), in stark contrast to the usual pressure-induced suppression of the charge modulations observed in other TMDs [3], high T_c cuprates [42], and recently discovered kagome metals [43,44]. At pressures P > 13 GPa, a structural transition towards a C2/m symmetry phase has been reported, concomitant with the emergence of SC [45]. The complex picture reported in bulk VSe₂ extends to the monolayer limit, where distinct competing charge orders with a significant range of transition temperatures have been observed [46,47], a behavior that is explained by the subtle anharmonic condensation of different phonon modes [48]. Interestingly, the formation of the CDW in the VSe₂ monolayer also competes with ferromagnetism [49].

To shed more light on the origin and interactions determining the CDW in bulk VSe2, here we present a comprehensive experimental and theoretical survey of the properties of 1T-VSe₂. We combine resonant elastic x-ray scattering, muon spin rotation spectroscopy (μ SR), ARPES, diffuse and IXS, and state-of-the-art anharmonic calculations to fully characterize the temperature and pressure dependence of its electronic and lattice dynamical properties. We find that, unlike 1T-TiSe₂, the static charge modulations do not resonate at either the V or Se K-edge, and the main contributor to the CDW formation is a momentum-dependent anisotropic EPI. In addition to the collapse of the low-energy phonon mode at \mathbf{q}_{CDW} and \mathbf{T}_{CDW} , the longitudinal and transverse acoustic branches also undergo weak phonon anomalies, highlighting the 3D nature of the charge correlations. Furthermore, the critical phonon does not soften as one heads towards the RT high-pressure transition, indicating that the transition from $P\overline{3}$ m1 to the C2/m symmetry [50] is of first-order type. We explain how the phonon anomalies of VSe2 are well captured when anharmonic effects are included in the calculations with an appropriate inclusion of vdW forces. Taken as a whole, our paper demonstrates that the simplicity of the VSe2 structure, with a minimal number of atoms per unit cell, allows a direct comparison between experiments and theory, providing a clear understanding of the origin of the electronic modulations in TMDs. We believe our results can be of inspiration to the understanding of collective ground states in more complex materials, such as high T_c superconducting cuprates [6,7,51,52] and recently discovered correlated topological kagome metals [53–55].

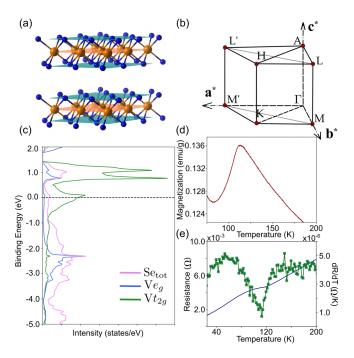


FIG. 1. (a) 2D structure of VSe_2 , where V and Se atoms are represented by orange and blue spheres, respectively. (b) BZ of the space group $P\overline{3}m1$ (164) and the main symmetry directions. (c) Density of states calculated using DFT showing the Se and V character close to the Fermi level. (d) Magnetization and (e) resistance of the VSe_2 single crystals, highlighting the CDW transition at 110 K.

The paper is organized as follows. In Sec. II, we describe the experimental and computational details as well as the fundamentals of the stochastic self-consistent harmonic approximation (SSCHA) method used to calculate the anharmonic phonons. In Sec. III, we present the experimental data and provide comparisons with first-principles calculations. Finally, our conclusions are summarized in Sec. IV.

II. EXPERIMENTAL AND COMPUTATIONAL METHODS

A. Experimental methods

High-quality single crystals of VSe₂ were synthesized by chemical vapor transport using iodine as a transport agent [41]. The chemical composition was confirmed with energy dispersive analysis. Resonant elastic x-ray scattering measurements were taken at the 4-ID-D station at the Argonne Photon Source (APS) and the P09 beamline at DESY. Temperaturedependent μ SR experiments were performed on the MUSR spectrometer of the ISIS pulsed muon facility in both powder and single-crystal VSe₂. Data were collected with zero field (ZF), and transverse field (TF), with the external magnetic field H applied perpendicular to S_{μ} . The data were analyzed using the software package WIMDA. The ARPES experiments, with energy and angular resolution of 20 meV and 0.2°, respectively, were performed at the LOREA beamline at the ALBA synchrotron. The lattice dynamics of VSe₂ were studied by high-resolution IXS and diffuse scattering (DS) at the HERIX spectrometer at the 30-ID beamline of the APS ($\Delta E = 1.5 \text{ meV}$), Argonne National Laboratory and the ID28 beamline at the European Synchrotron Research Facility (ESRF, $\Delta E = 3$ meV), with incoming energies of 23.7 and 17.8 keV for IXS and DS, respectively. Orientation matrix refinement and reciprocal space reconstructions images were performed using the CrysAlis software package. Final DS reconstructions were processed using in-house code. The components $(h \ k \ l)$ of the scattering vector are expressed in reciprocal lattice units (r.l.u.), $(h \ k \ l) = h\mathbf{a}^* +$ $k\mathbf{b}^* + l\mathbf{c}^*$, where \mathbf{a}^* , \mathbf{b}^* , and \mathbf{c}^* are the reciprocal lattice vectors. Low-energy modes of VSe2 were analyzed by fitting the phonon frequencies to damped harmonic oscillators convoluted with the instrumental resolution. High-pressure powder XRD measurements up to 20 GPa were carried out at RT at the BL04-MSPD beamline of ALBA synchrotron $(\lambda = 0.4246 \text{ Å, beam size } 20 \times 20 \text{ µm})$ [56] using a LeToullec membrane-type diamond-anvil cell (DAC), with a mixture of methanol-ethanol (4:1) as the pressure-transmitting medium. The pressure was determined using the equation of state (EOS) of copper (Cu) [57]. The data was analyzed with the GSAS suite [58]. High-pressure IXS experiments were performed at the ID28 beamline of the ESRF with an incident photon energy of 17.8 keV and a helium-pressurized membrane DAC.

B. Computational methods

1. Electronic property calculation details

Band-structure calculations were performed within density-functional theory (DFT) using the all-electron, full-potential WiEn2k code [59] based on the augmented plane-wave plus local orbital (APW+lo) basis set. The generalized gradient approximation (GGA) in the Perdew-Burke-Ernzerhof (PBE) [60] scheme was used for the exchange-correlation functional, with a fully converged k-mesh of $R_{\rm mt}K_{\rm max}=7.0$ and muffin-tin radii of 2.5 and 2.22 a.u. for V and Se, respectively. The theoretical ARPES spectra were calculated using the Chinook code [61], using an inner potential $V_0=14$ eV [4].

2. Anharmonic lattice dynamics: The SSCHA method

Vibrational properties of 1T-VSe $_2$ are described within the Born-Oppenheimer approximation, so the ionic vibrations are described by the Born-Oppenheimer energy surface (BOES) $V(\mathbf{R})$. \mathbf{R} specifies the positions of all ions in the crystal, i.e., R_a in component-free notation. Here, the single index $a=(\alpha,s,\mathbf{l})$ indicates Cartesian coordinates α , atom index inside the unit cell s, and crystal lattice vector l at the same time. Throughout this paper, bold letters generically denote vectors and tensors in component-free notation.

The SSCHA [62–66] is a quantum variational method on the free energy fully accounting for anharmonic effects and valid at any temperature. The variational minimization is carried out with respect to a trial density matrix $\rho_{\mathcal{H}}$ defined by a harmonic Hamiltonian \mathcal{H} , so it contains two groups of parameters: the auxiliary force-constants Φ and the average ionic positions \mathcal{R} , the so-called *centroid* positions. In the minimization procedure, the free energy and its gradient are evaluated through a stochastic technique by calculating forces and energies in supercells, without approximating the ionic potential $V(\mathbf{R})$. The centroid positions at the free-energy minimum \mathcal{R}_{eq} are the ionic equilibrium positions fully accounting

for quantum, thermal, and anharmonic effects. The dynamical matrix based on the final auxiliary force-constants,

$$D_{ab}^{(s)} = \frac{1}{\sqrt{M_a M_b}} \Phi_{ab}(\mathcal{R}_{eq}), \tag{1}$$

determines the amplitude of the vibrations around the \mathcal{R}_{eq} positions and is, thus, positive definite by construction. M_a and M_b are the masses of atom a and b.

According to Landau's theory [67], second-order structural phase transitions like many CDWs in 2D-TMDs can be identified through the analysis of the temperature evolution of the free-energy curvature with respect to the order parameter in a high-symmetry configuration. The appropriate order parameters in displacive second-order phase transitions are precisely the centroid positions. Within the SSCHA formalism, this free-energy Hessian can be calculated analytically as [63]

$$\frac{\partial^2 F}{\partial \mathbf{R} \partial \mathbf{R}} = \mathbf{\Phi} + \mathbf{\Phi} \mathbf{\Lambda}(0) [\mathbb{1} - \mathbf{\Phi} \mathbf{\Lambda}(0)]^{-1} \mathbf{\Phi}, \tag{2}$$

where Φ are the *n*th order anharmonic force constants, which are calculated as quantum averages taken with the SSCHA density matrix: $\Phi = \langle \frac{\partial^n V}{\partial \mathbf{R}^n} \rangle_{\rho_{\mathcal{H}}}$. The fourth-order tensor $\Lambda(0)$ is the static limit of $\Lambda(z)$, which in component notation is given by

$$\Lambda^{abcd}(z) = -\frac{1}{2} \sum_{\mu\nu} F(z, \omega_{\mu}, \omega_{\nu}) \sqrt{\frac{\hbar}{2M_{a}\omega_{\mu}}} \varepsilon_{\mu}^{a} \times \sqrt{\frac{\hbar}{2M_{b}\omega_{\nu}}} \varepsilon_{\nu}^{b} \sqrt{\frac{\hbar}{2M_{c}\omega_{\mu}}} \varepsilon_{\mu}^{c} \sqrt{\frac{\hbar}{2M_{d}\omega_{\nu}}} \varepsilon_{\nu}^{d}, \quad (3)$$

where ω_{μ}^2 and ε_{μ}^a are the eigenvalues and corresponding eigenvectors of the auxiliary SSCHA dynamical matrix $D_{ab}^{(s)}$ in Eq. (1), and

$$F(z, \omega_{\mu}, \omega_{\nu}) = \frac{2}{\hbar} \left[\frac{(\omega_{\mu} + \omega_{\nu})[1 + n_{B}(\omega_{\mu}) + n_{B}(\omega_{\nu})]}{(\omega_{\mu} + \omega_{\nu})^{2} - z^{2}} - \frac{(\omega_{\mu} - \omega_{\nu})[n_{B}(\omega_{\mu}) - n_{B}(\omega_{\nu})]}{(\omega_{\mu} - \omega_{\nu})^{2} - z^{2}} \right], \quad (4)$$

with $n_B(\omega)$ the bosonic occupation factor. Therefore, negative eigenvalues of the free-energy Hessian-based dynamical matrix,

$$D_{ab}^{(F)} = \frac{1}{\sqrt{M_a M_b}} \frac{\partial^2 F}{\partial \mathcal{R}_a \partial \mathcal{R}_b} \bigg|_{\mathcal{R}_{ca}}, \tag{5}$$

indicate a structural distortion that decreases the free energy. This information can be used to determine CDW transition temperatures, since the CDW will appear when $\mathbf{D}^{(F)}$ develops a negative eigenvalue in the high-symmetry phase upon lowering the temperature. This technique has been successful in the characterization of displacive structural phase transitions in a large variety of strongly anharmonic systems, such as superconducting hydrides [64,68], thermoelectric compounds [69,70], and similar CDW materials [24,71–73].

The physical phonons measured experimentally with, for instance, inelastic scattering experiments, are not the eigen-

values of $\mathbf{D}^{(F)}$ nor $\mathbf{D}^{(s)}$, but the spectral functions associated to the displacement-displacement correlation functions. Within the SSCHA [63,74,75], for a given point \mathbf{q} of the BZ, it is given by [64]

$$\sigma(\mathbf{q},\omega) = -\frac{\omega}{\pi} \text{Im}(\text{Tr}[\omega^2 \mathbb{1} - \mathbf{D}^{(s)}(\mathbf{q}) - \mathbf{\Pi}(\mathbf{q},\omega + i\delta^+)]^{-1}),$$
(6)

where $\Pi(\mathbf{q}, z)$ is the SSCHA self-energy, defined as

$$\mathbf{\Pi}(z) = \mathbf{M}^{-\frac{1}{2}} \stackrel{(3)}{\mathbf{\Phi}} \mathbf{\Lambda}(z) [\mathbb{1} - \stackrel{(4)}{\mathbf{\Phi}} \mathbf{\Lambda}(z)]^{-1} \stackrel{(3)}{\mathbf{\Phi}} \mathbf{M}^{-\frac{1}{2}}, \tag{7}$$

and δ^+ is a small positive number. Note that in the static $\omega = 0$ limit, the peaks of the $\sigma(\mathbf{q}, \omega)$ spectral function coincide with the eigenvalues of $\mathbf{D}^{(F)}$.

As a first approximation in the calculation of the spectral function, the mixing between phonon modes can be neglected by assuming that $\Pi(z)$ is diagonal in the basis of the modes. In this way, each mode (\mathbf{q},μ) has a particular contribution to the spectral function

$$\sigma(\mathbf{q}, \omega) = \sum_{\mu} \frac{1}{2} \left[\frac{-\text{Im} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)}{[\omega - \text{Re} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)]^{2} + [\text{Im} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)]^{2}} + \frac{1}{\pi} \frac{\text{Im} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)}{[\omega + \text{Re} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)]^{2} + [\text{Im} \mathcal{Z}_{\mu}(\mathbf{q}, \omega)]^{2}} \right],$$
(8)

with

$$\mathcal{Z}_{\mu}(\mathbf{q},\omega) = \sqrt{\omega_{\mu}^{2}(\mathbf{q}) + \Pi_{\mu\mu}(\mathbf{q},\omega + i0^{+})},$$
 (9)

where $\Pi_{\mu\mu}(\mathbf{q},z)$ is the diagonal part of the self-energy in the mode basis.

The form of the spectral function in Eq. (8) resembles a superposition of Lorentzian functions but with frequency-dependent centers and widths, meaning that its actual form may differ from real Lorentzians. One can take a Lorentzian approximation by fixing the frequency in the $\mathcal{Z}_{\mu}(\mathbf{q},\omega)$ function. In the so-called one-shot approximation, the Lorentzian shape is recovered by calculating the position of the peak as

$$\Theta_{\mu}^{(os)}(\mathbf{q}) = \text{Re}\mathcal{Z}_{\mu}(\mathbf{q}, \omega_{\mu}(\mathbf{q}))$$
 (10)

and the half-width at half-maximum linewidth as

$$\Gamma_{\mu}^{(os)}(\mathbf{q}) = -\text{Im}\mathcal{Z}_{\mu}(\mathbf{q}, \omega_{\mu}(\mathbf{q})). \tag{11}$$

When the SSCHA self-energy is a small perturbation of the SSCHA free propagator $(\Pi_{\mu\mu} \ll \omega_{\mu}^2)$, a further approximation can be taken by truncating the Taylor expansion of Eq. (9) at first order:

$$\Theta_{\mu}^{\text{(pert)}}(\mathbf{q}) = \frac{1}{2\omega_{\mu}(\mathbf{q})} \text{Re}\Pi_{\mu\mu}(\mathbf{q}, \omega_{\mu}(\mathbf{q})), \tag{12a}$$

$$\Gamma_{\mu}^{(\text{pert})}(\mathbf{q}) = -\frac{1}{2\omega_{\mu}(\mathbf{q})} \text{Im} \Pi_{\mu\mu}(\mathbf{q}, \omega_{\mu}(\mathbf{q})). \tag{12b}$$

We have applied the SSCHA theory to the normal state phase of 1T-VSe₂ [Fig. 1(a)], with the experimental lattice parameters at RT: a = b = 3.35 Å and c = 6.09 Å. The Born-Oppenheimer energies and forces required for the SSCHA variational minimization were calculated on $4 \times 4 \times 3$ sized

supercells (almost commensurate with \mathbf{q}_{CDW}) using plane-wave-based DFT within the PBE approximation [60] of the exchange-correlation functional, making use of the QUANTUM ESPRESSO package [76,77]. We also performed calculations by including vdW interactions using Grimme's semiempirical approach [78] and within the nonlocal functional developed by Dion *et al.* [79]. We used an ultrasoft pseudopotential that includes $4s^2$ $3d^3$ valence electrons for V and a norm-conserving one with $4s^2$ $4p^4$ electrons in the valence for Se. We used a plane-wave energy cutoff of 40 Ry for the wave functions and 450 Ry for the charge density. The BZ integrals were performed in a $3 \times 3 \times 3$ k-point grid in the supercell with a Methfessel-Paxton smearing [80] of 0.01 Ry.

formed in the so-called bubble approximation [63], setting $\Phi = 0$ in Eqs. (2) and (7). The dynamical spectral function was calculated considering a broadening of $\delta^+ = 0.5$ cm⁻¹ and a $48 \times 48 \times 32$ grid to determine the SSCHA self-energy. The phonon frequencies and third-order force constants at these points were obtained by Fourier interpolation. The spectral function was calculated within the no mode-mixing approximation, i.e., directly from Eq. (6), as well as in the one-shot approximation [Eqs. (10) and (11)], and in the perturbative case [Eq. (12)].

Both static and dynamical SSCHA calculations were per-

3. Harmonic phonons and the EPI

Harmonic phonon frequencies and electron-phonon matrix elements were calculated within density functional perturbation theory (DFPT) [81] as implemented in QUANTUM ESPRESSO [76,77]. DFPT calculations were performed with the same parameters as in the SSCHA but with a $24 \times 24 \times 16$ grid in the unit cell for the BZ integrals and a smearing of 0.005 Ry. The electron-phonon linewidth is given by

$$\gamma_{\mu}(\mathbf{q}) = \frac{2\pi \omega_{\mu}(\mathbf{q})}{N} \sum_{nn'} \sum_{\mathbf{k}}^{\mathrm{IBZ}} \left| g_{n'\mathbf{k}+\mathbf{q},n\mathbf{k}}^{\mu} \right|^{2} \delta(\epsilon_{n'\mathbf{k}+\mathbf{q}}) \delta(\epsilon_{n\mathbf{k}}), \quad (13)$$

where $\epsilon_{n\mathbf{k}}$ is the energy of band n with wave number \mathbf{k} measured from the Fermi level, N the number of \mathbf{k} points in the sum over the first BZ, and $g^{\mu}_{n'\mathbf{k}+\mathbf{q},n\mathbf{k}}$ the electron-phonon matrix elements. In Eq. (13), we use a $48\times48\times32$ **k**-point grid and a Gaussian broadening of 0.003 Ry for the Dirac deltas.

III. RESULTS

A. Characterization of the CDW: Transport, resonant elastic x-ray scattering, and μ SR

Figures 1(a) and 1(b) show the crystalline structure of 1T-VSe $_2$ and the high-symmetry directions of the BZ. The unit cell of the 1T polymorph consists of a 2D stacking of VSe $_2$ monolayers bonded together by vdW interactions [82]. The V ion is octahedrally coordinated by Se atoms within the $P\overline{3}m1$ space group with lattice parameters a=b=3.35 Å and c=6.09 Å. Transport experiments reveal a CDW transition at 110 K, as shown in Figs. 1(d) and 1(e), in very good agreement with previous reports [45,83]. The small amplitude of the hump in the resistivity and magnetic susceptibility curves illustrates the high quality of our crystal and demon-

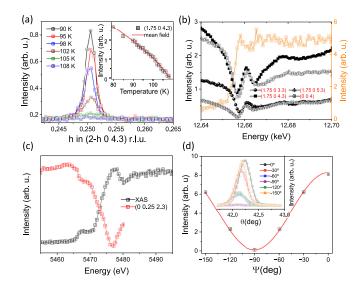


FIG. 2. (a) Temperature dependence of the CDW peak at the Se K-edge (12.66 keV). Inset, fitting of the temperature dependence of the intensity to a power law with $\alpha = 0.43 \pm 0.05$. (b) Energy dependence of several CDW reflections and the (0 0 4) Bragg peak at 60 K. The orange spectrum follows the x-ray absorption at $\mathbf{q} \neq \mathbf{q}_{\text{CDW}}$. (c) Energy scan at the CDW peak (0 0.25 2.3) r.l.u. (red) and absorption spectrum (black) at the V K-edge. (d) Polarization dependence of the (0 0.25 2.3) r.l.u peak. Inset: Raw spectra.

strates that only a small fraction of carriers are lost at the CDW transition. DFT calculations show that the charge carriers at the Fermi level [Fig. 1(c)] come mostly from the V bands, with a predominant contribution from the trigonally-split V t_{2g} orbitals. The Se p bands dominate the spectra from 1 eV below the Fermi level (strongly mixed with the V e_g bands).

We initiate our experimental survey studying the charge reflections by means of resonant hard x-ray diffraction at the V and Se K-edges. Figure 2(a) displays the momentumtemperature dependence of the raw scans (Se K-edge, 12.66 keV) at the (1.75 0 4.3) r.l.u. CDW peak. The integrated intensity follows a mean field power law with $\alpha =$ 0.43 ± 0.05 , characteristic of a second-order phase transition. On the other hand, the energy dependence of the CDW reflections does not show any resonant enhancement of the CDW signal. The charge reflections are dominated by Thompson scattering, as demonstrated by a wiggled energy dependence that follows the (0 0 4) Bragg peak [Fig. 2(b)]. Hence, the resonant scattering is described by a full occupation of the Se p states associated with a purely structural distortion at the CDW transition. Focusing on the V K-edge [Fig. 2(c)], the energy scan displays the main absorption edge at 5.475 keV, which corresponds to the dipole allowed transition from the 1s to the empty 4p states of V. A pre-edge absorption is visible 10 eV below the main edge, ascribed to the dipole forbidden $1s \rightarrow 3d$ transition, which becomes allowed due to a distorted octahedral symmetry that switches on the mixing between 3d orbitals of V and 4p orbitals of Se [84]. Similar to the Se K-edge, the energy scan across the CDW does not show any resonant enhancement at any azimuthal angle, pointing to a pure charge scattering process. Fitting the polarization dependence of the scattered radiation [Fig. 2(d) and inset] to

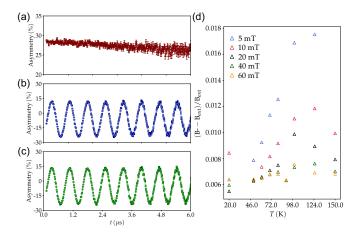


FIG. 3. (a) Zero-field longitudinal μ SR spectrum taken at 20 K. (b) TF- μ SR spectra at 20 K and 10 mT and (c) 150 K. Symbols are the experimental data and the solid line, its fitting to a Gaussian decay. (d) Temperature dependence of the muon Knight shift.

the equation [85]

$$I \propto S + P_1 \cos(2\Psi) + P_2 \sin(2\Psi) \tag{14}$$

returns the values of the Poincaré-Stokes parameters, P_1 and P_2 of 0.992 and -0.013, respectively (a value of $P_1 \sim 1$ indicates no change in the rotation of the polarized scattered light). This reaffirms the purely structural origin of the CDW reflections. Furthermore, an exhaustive search for signatures of orbital ordering and symmetry-forbidden reflections gave a negative result at both edges. Hence, the CDW of 1T-VSe₂ seems to be more conventional in comparison to the chiral/orbital order reported in the 1T-TiSe₂ [32,34]. This conclusion is further corroborated by the absence of time reversal symmetry breaking in the CDW state by μ SR. Zerofield μ SR measured in the longitudinal (relaxation) geometry, in Fig. 3(a), does not detect any precession or relaxation which could be attributed to magnetic order. Figures 3(b) and 3(c) show the time evolution of the asymmetry spectra taken in TF geometry with 10 mT external field at 20 K and 150 K. No significant changes can be found in the two asymmetry spectra as a function of temperature. The time-domain TF asymmetry spectra are fitted to the function,

$$A_0 P(t) = A_i \cos(2\pi \nu_i t + \phi) \exp(-\lambda_i t)^2, \tag{15}$$

where A_0 and A_i are asymmetries $[A(t) = [N_F(t) - \alpha N_B(t)]/[N_F(t) + \alpha N_B(t)]$, $N_F(t)$, and $N_B(t)$ are the respective signals in the forward and backward detectors and α a balancing factor], P(t) the muon polarization, λ_i relaxation rates, and ϕ and ν_i are the offset phase and the frequency that correspond to local magnetic fields, i.e., $2\pi \nu_i = \gamma_\mu B_i$, where $\gamma_\mu = 2\pi \times 135.5$ MHz/T is the gyromagnetic ratio of the muon [86]. In Fig. 3(d), we plot the muon Knight shift, defined as $K_{\rm exp} = \frac{B_u - B_{\rm ext}}{B_{\rm ext}}$, against temperature, showing that the muon Knight shift follows the local magnetic susceptibility of itinerant electrons that are modified by the CDW, as shown in Fig. 1(d). Taken together, the resonant scattering and the μ SR data, the CDW state of VSe₂ does not break the time-reversal symmetry, discarding any magnetic and orbital/flux order scenario.

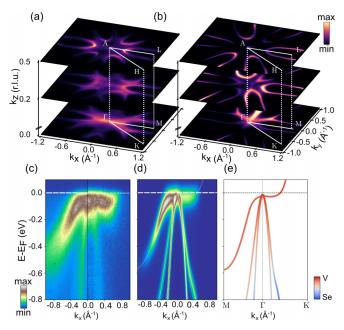


FIG. 4. (a) Experimental Fermi surface at the $k_z=0$, 0.2 and 0.5 r.l.u. planes ($h\nu=57$, 62, 72 eV, respectively, $V_0=14$ eV) in the low temperature phase. (b) ARPES simulated spectra of the Fermi surface at the same planes. (c) Experimental energy-momentum dispersion along the direction $M-\Gamma-K$ ($h\nu=57$ eV). (d) Simulated energy-momentum dispersion through the direction $M-\Gamma-K$. (e) Atomic orbital contribution of vanadium and selenium to the bands in the $M-\Gamma-K$ direction.

B. Electronic structure: ARPES

Now, we detail our study of the electronic structure by means of ARPES. Figures 4(a) and 4(b) display an overall nice agreement between the experimental and calculated Fermi surfaces in the $k_z = 0$, 0.2 and 0.5 r.l.u. planes. At 10 K, the Fermi surface consists of an intense feature at Γ and large ellipsoids centered at each M point that extend over the whole BZ. In Figs. 4(c) and 4(d), we plot the measured and calculated band dispersion along the high-symmetry line $M - \Gamma - K$. Figure 4(c) shows two nearly degenerate holelike bands that merge at the Fermi level at the Γ point and separate at higher binding energy. The inner of these bands is a largely covalent mixture of Se p states together with V e_{ρ} bands (forming a σ bond), while the outer degenerate band comes mostly from the V a_{1g} orbital. This is the only (mostly) occupied t_{2g} orbital in VSe₂, with lobes pointing along the trigonal axis of the Se octahedra (off the vdW hexagonal plane of the structure). This band disperses upwards along the high-symmetry line Γ – K. The dominant V d character just below the Fermi level can be seen in Fig. 4(e). At the A point, the band character comes mostly from V $e_{g^{\pi}}$ states, the doublet formed by t_{2g} states in a trigonal environment, which is dispersionless along the Γ -A direction. Overall, the measured electronic band structure is fully reproduced by the DFT calculations and is consistent with the previous reports in the literature [36,87].

On the other hand, the experimental Fermi surface centered at $\overline{\rm M}$ for $k_z=0.2$ and 0.5 r.l.u. shows a suppression of spectral weight at the Fermi level around $|k_x|\sim 0.55~{\rm \AA}^{-1}~(h\sim 0.25$

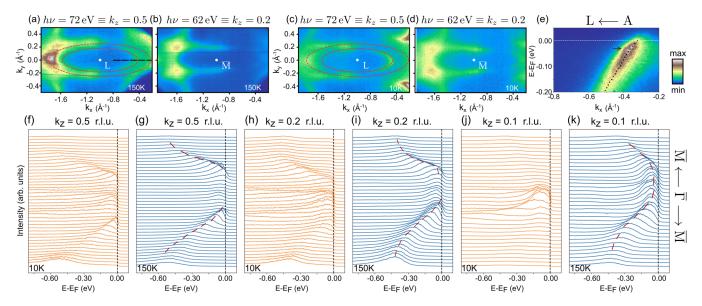


FIG. 5. (a), (b) Fermi Surface ± 50 meV centered on an ellipsoid measured with hv = 72, 62 eV at T = 150 K. (c), (d) Fermi Surface ± 50 meV centered on an ellipsoid measured with hv = 72, 62 eV at T = 10 K. The red dashed lines with ellipses are a guide to the eye. The black dashed line in (a) represents the momentum-dependent energy dispersion. (e) Band dispersion in the direction L - A at T = 150 K. The maxima of intensity of the band for each binding energy is marked by the black points and the kink feature is highlighted with an arrow. (f), (h), (j) Orange energy distribution curves (EDCs) at 72, 62, 52.5 eV at T = 10 K. (g), (i), (k) Blue EDCs at 72, 62, 52.5 eV at T = 150 K. Note that in (f)–(k), the intensities of each EDCs panel is normalized with respect to its maximum value. The dashed red lines are guides to the eye.

r.l.u.), both at low (10 K) and high (150 K) temperatures [Figs. 5(a)-5(d). To better visualize this loss of DOS, in Figs. 5(f)-5(k) we compare the energy distribution curves (EDCs) that characterize the ellipsoidal Fermi surface along the $\overline{M} - \overline{\Gamma}$ direction at different k₂'s. At 150 K, the dispersive band along the $\overline{M} - \overline{\Gamma}$ direction [dashed line in Figs. 5(g), 5(i) and 5(k)] present much larger spectral weight than the holelike band. However, at low temperature, both bands develop a similar spectral weight in the ARPES spectra, Figs. 5(f), 5(h), and 5(j). This loss of intensity happens for all values of k_z , in agreement with the presence of a pseudogap phase above the CDW transition [88] and the absence of a clear full gap [37,89]. Further, our ARPES data at low and high temperatures resolve two ellipsoidal bands around the M point [Figs. 5(a) and 5(c)], more clearly visible in the second BZ, which are not captured by the DFT calculations but are in agreement with recent reports [87]. Our results also reveal a nonlinear band dispersion close to E_F and a small kink in the L \rightarrow A direction [Fig. 5(e)], corroborating the presence of strong EPI, as recently reported by Raman and high-resolution ARPES [40].

Further, we can evaluate the presence of FSN vectors by approximating the imaginary part of zero-energy Lindhard charge susceptibility, $\operatorname{Im}(\chi_q) = \sum_k \delta(\epsilon_k - \epsilon_F) \delta(\epsilon_{k+q} - \epsilon_F)$, to the autocorrelation function of the Fermi surface measured in the MLL'M' plane [see the BZ in Fig. 1(b)] [36]. We define the autocorrelation function as $R(q) = \int_{\Omega} I_F(k) I_F(k+q) d^2k$, where $I_F(k)$ is the photoemission intensity of the Fermi surface at each k. This autocorrelation function has been used extensively to search for a divergent behavior in χ_q [90] and is a quantitative test of FS nesting [91]. Although our measurements were carried out below $h\nu = 100\,\mathrm{eV}$ and the intrinsic k_z broadening is not small enough to treat the final

states as free-electron-like, we can still gain some valuable information using this approach. In Figs. 6(c) and 6(d), we plot R(q) at low and high temperatures, respectively. At 150 K, the autocorrelation map develops a broad streak of intensity with its maximum at $q_{\parallel} = 0.216 \pm 0.005$ r.l.u. and $q_{\perp} = 0.28 \pm 0.03$ r.l.u. At low temperature, this maximum appears slightly shifted, ($q_{\perp} = 0.32 \pm 0.03$ r.l.u.), but is still very close to the \mathbf{q}_{CDW} observed experimentally in the diffraction experiments, hence, demonstrating the enhanced charge correlations at \mathbf{q}_{CDW} . Indeed, the charge correlations appear throughout the whole \mathbf{k}_z direction, not exclusively at \mathbf{q}_{CDW} . It should be stressed that this does not support the FSN scenario,

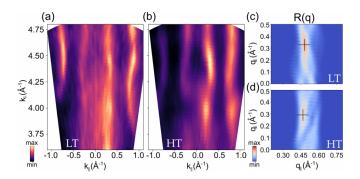


FIG. 6. (a), (b) Fermi surface in the plane $(k_{\parallel}, k_{\perp})$ at $T \simeq 10$, 150 K, respectively. The energy scans are plotted at the Fermi level integrated in a range of $\pm 100\,\mathrm{meV}$. (c), (d) Autocorrelation $R(q_{\parallel}, q_{\perp})$ for the k_z dispersion at low and high temperatures, respectively. The autocorrelation is maximum at $q_{\parallel} = 0.48 \pm 0.01\,\mathrm{\mathring{A}}^{-1}$ and $q_{\perp} = 0.33 \pm 0.03\,\mathrm{\mathring{A}}^{-1}$ for low temperature and $q_{\parallel} = 0.47 \pm 0.01\,\mathrm{\mathring{A}}^{-1}$ and $q_{\perp} = 0.29 \pm 0.03\,\mathrm{\mathring{A}}^{-1}$ for high temperature. These maxima are indicated with the crosses.

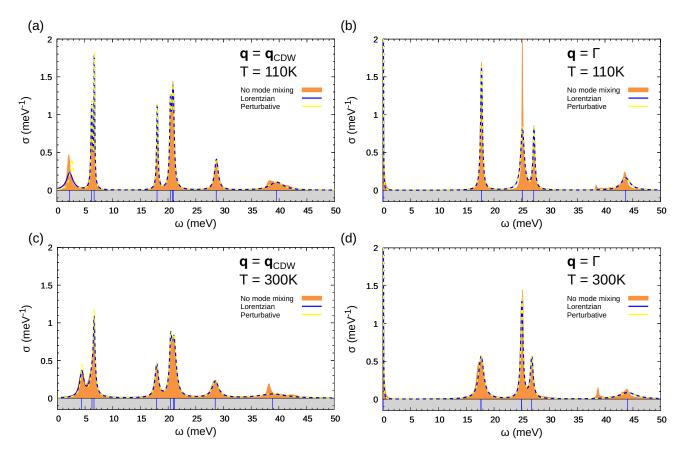


FIG. 7. Anharmonic phonon spectral functions at 110 K at (a) $\mathbf{q}_{CDW} = (0\ 1/4\ 1/3)\ r.l.u.$ and (b) Γ points, and at RT at (c) \mathbf{q}_{CDW} and (d) Γ points. The orange-filled area indicates the result obtained with the no mode-mixing approximation in Eq. (8). The blue solid line is the spectrum calculated in the one-shot Lorentzian approximation in Eqs. (10) and (11). The center of these Lorentzians, specified with vertical blue lines in the grey shaded area below, indicate the anharmonic phonon frequencies in the quasiparticle picture. The yellow line is the spectrum in the perturbative limit [see Eqs. (12)].

but correlates with the softening of the low-energy phonon branches, as we will detail later.

C. Lattice dynamical properties of the high-symmetry phase

Having studied the structural and electronic properties, we now move to the lattice dynamical properties of 1T-VSe₂.

1. Anharmonic DFT spectral functions

Before moving to experimental results, in this section we present the theoretical analysis of the anharmonic spectral functions $\sigma(\mathbf{q}, \omega)$ at ambient pressure at two relevant temperatures including Grimme's semiempirical vdW interactions: the experimental critical temperature (110 K) and RT. First, we check the adequacy of the approximations introduced in Sec. II B 2 by calculating the anharmonic phonon spectral function at the critical wave vector $\sigma(\mathbf{q}_{CDW}, \omega)$ and 110 K. As shown in Fig. 7(a), not all modes have a Lorentzian profile. For instance, the highest energy mode has a clear satellite peak, indicating that anharmonicity makes the quasiparticle picture questionable for this mode and, consequently, the Lorentzian approximations do not work well. This result emphasizes that anharmonicity is not only crucial to stabilize the lowest energy mode at \mathbf{q}_{CDW} [41], it also impacts high-energy optical modes considerably in their spectral properties. Nevertheless, the spectrum obtained within the Lorentzian one-shot approximation, plotted with blue solid lines, yields a reasonable result for most modes. In particular, for the lowest energy branch, the one driving the CDW transition, the result is not identical to the non-Lorentzian no-mode mixing approximation, but in both cases the positions coincide. The spectrum obtained in the perturbative limit, plotted with dashed yellow lines, is generally in agreement with the one-shot calculation. However, the frequency attributed to the phonon that drives the CDW transition is blue shifted in the latter case. This means the SSCHA self-energy cannot be considered small for the softened mode, and the perturbative approach fails. As shown in Fig. 7(c), temperature flattens and broadens all phonon peaks due to enhanced scattering between phonons, hindering their experimental detection. Interestingly, the soft mode is strongly blueshifted with temperature up to 5 meV at 300 K as expected from the previous static calculations [41], while the other two acoustic modes become quasidegenerate.

In Figs. 7(b) and 7(d), the anharmonic phonon spectral function is presented at the Γ point for both 110 K and 300 K. For low-energy excitations, the phonon quasiparticle picture is rather well-defined. However, the huge phonon satellite ascribed to the highest-energy optical mode confirms this mode is strongly anharmonic throughout the whole BZ

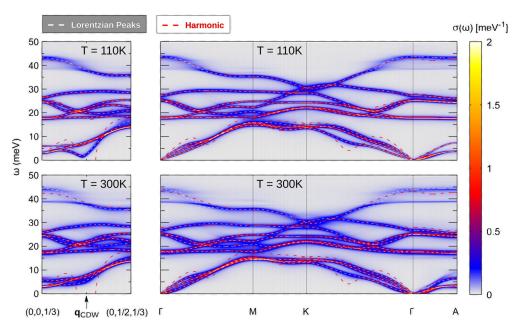


FIG. 8. Anharmonic phonon spectral functions at 110 K and 300 K along (0 k 1/3) r.l.u. and $\Gamma - M - K - \Gamma - A$ paths. The dashed white lines are the anharmonic phonon frequencies extracted from the center of the Lorentzians in the one-shot approximation, while red dashed lines are the harmonic phonons.

despite its high energy and that anharmonicity removes its quasiparticle nature. In fact, the splitting of this peak in two can lead to confusion during experiments. The highest energy mode is infrared (IR) and not Raman active, so it might be difficult to observe the peak splitting with either of these techniques due to the large reflectivity of metals in the IR.

In Fig. 8, the full anharmonic phonon spectrum is plotted both at 110 K and 300 K and is compared to calculations using the harmonic approximation. The figure clearly illustrates that the main anharmonic renormalization of the phonon frequency concentrates around \mathbf{q}_{CDW} . The frequency of the CDW driving ω_1 mode, unstable in the harmonic approximation, is strongly temperature dependent as reflected by the spectral function. It is interesting to remark that also halfway between Γ -M and Γ -K, an important anharmonic renormalization of the lowest energy acoustic mode is also observed, despite its temperature dependence being weak. The full spectral function reveals that the highest energy optical mode shows a clear double peak structure in most of the BZ at low and high temperatures and the highest energy longitudinal acoustic mode exhibits a satellite peak close to A at 300 K.

In the rest of the calculations presented here, we assume the one-shot Lorentzian approximation, which allows an estimation of the phonon linewidth that can be compared directly to the experimentally determined one.

2. Diffuse scattering

Before discussing the experimental phonon data of VSe₂, we describe the DS measurements (Fig. 9). Strong diffuse signals coming from the condensation of a mixture of longitudinal and transverse phonons are already present at temperatures above 250 K in the $(h\ 0\ l)$ plane. The DS develops its maximum intensity at the reciprocal lattice vector

 G_{201} and follows the C_3 symmetry of the P3m1 space group. This CDW precursor increases its intensity on cooling and condenses into a 3D-CDW at $T_{\text{CDW}} \approx 110$ K, in agreement with the transport and x-ray data of Figs. 1 and 2.

3. Low-energy lattice dynamics: IXS

In Fig. 10, we plot the DFT anharmonic spectral function along the Γ -A direction at 110 K in the high-temperature phase, together with the experimental measurements at 50 K performed along the (0 0 4+l) direction in the CDW phase. As the Γ -A direction lies along the C_3 rotation axis, the only visible acoustic branch ω_3 (higher energy) corresponds to a pure longitudinal mode polarized along the c axis of the crystal. The remaining modes ω_1 and ω_2 (which are degenerate in frequency) are transversal and, thus, invisible. The ω_3

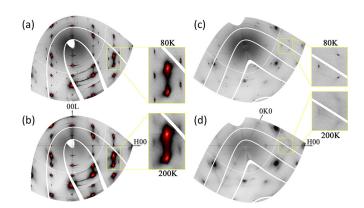


FIG. 9. (a), (b) Diffuse scattering (DS) maps of VSe₂ for the $(h \ 0 \ l)$ plane, showing the CDW reflections at 80 K and diffuse signal at 200 K, respectively. (c), (d) DS maps for the $(h \ k \ 0)$ plane, showing the CDW reflections at 80 K and diffuse signal at 200 K, respectively.

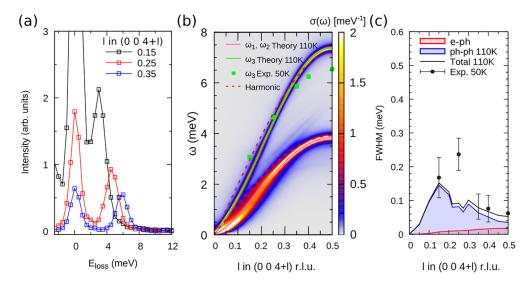


FIG. 10. (a) Representative momentum dependence of the IXS spectra at 50 K, (b) anharmonic spectral function compared to the experimental peaks and (c) linewidth of the longitudinal $(0\ 0\ 4+l)$ r.l.u. phonon at 50 K in experiments and 110 K in anharmonic theoretical calculations.

phonon follows a sinusoidal dispersion, consistent with DFT calculations. At 110 K, it has a frequency of 7 meV at the BZ border, lower than the acoustic mode at M, presumably due to the confinement of the acoustic mode in the low-dimensional VSe₂ layer. This longitudinal c-axis polarized mode is barely temperature dependent and the experimental dispersion measured at 50 K, even though it is within the CDW phase, also follows the dispersion obtained from the harmonic calculations. However, as can be seen in Fig. 10(c), the largest contribution to the linewidth of ω_3 comes from anharmonic effects rather than from EPI. Furthermore, as shown in Fig. 8, we also see that the anharmonic contribution to the total linewidth clearly increases with temperature. Together, this indicates that anharmonicity has a larger impact on linewidths than frequencies for the phonon modes along the C_3 rotation axis.

We now turn our attention to the phonon branches propagating in the VSe₂ plane. Figures 11(a) and 11(b) summarize the experimental data taken along the (2+h 0 0) r.l.u. direction for $0.15 < h < 0.9 (\Gamma - M - \Gamma)$ at 300 K. The intensity dispersion of the VSe₂ lattice dynamics matches the DFT anharmonic calculation, where two branches are clearly visible below 30 meV. The highest mode corresponds to an optical branch and disperses along the Γ – M direction, with frequencies from 20 to 25 meV. Focusing on the purely acoustic phonon, between 0.15 < h < 0.5, we observe one single lattice mode, which changes character along the Γ – M direction. Between 0.22 < h < 0.3, ω_1 , with transversal character, it develops more intensity [see Fig. 11 (c), where we plot the (2.25 0 0) r.l.u. scan], while the branch with longitudinal character (ω_3) dominates between 0 < h < 0.22 and 0.3 < h <0.5. Furthermore, the analysis of the linewidth of the acoustic branch along the $(2+h\ 0\ 0)$ r.l.u. direction $(0 < h < 0.5\ r.l.u.)$ reveals an anomalous broadening around h = 0.3, which is well captured by our anharmonic calculations. We point out here that the remaining transversal ω_2 mode is silent in IXS. On the other hand, along the 0.5 < h < 1 direction, both the ω_1 and ω_3 modes can be discerned [see the spectrum at (2.75)]

0 0) r.l.u. in 11 (c)] and their dispersions are superimposed to the dynamical phonon spectra calculated with the SSCHA in Fig. 11(b). The ω_1 and ω_3 modes overlap between 0.6 < h <0.7 [Fig. 11(c)] and, thus, were fitted to a single Lorentzian convoluted with the experimental resolution. Moreover, as directly visualized in the raw spectra, the temperature dependence of the frequency of ω_3 undergoes a partial softening (~ 1.3 meV), which is accompanied by a small broadening of the total linewidth ($\omega_1 + \omega_3$) at T_{CDW} [Figs. 11(f) and 11(g)], reflecting the response of the acoustic branch to the CDW transition. In Fig. 11(h), we plot a representative set of the single phonon dispersion along the (h 0 4) r.l.u. direction (0 < h < 0.5), which probes only the transversal component of the acoustic mode. It disperses linearly up to 15 meV and shows again a small softening and broadening at h = 0.25and 110 K [Fig. 11(j)] followed by a phonon hardening and narrowing down to 50 K. The temperature dependence of the transversal, longitudinal, and soft branches are summarized in Fig. 12(a). We can clearly observe that, while the phonon at $(2.25\ 0\ 0.7)$ r.l.u. fully collapses at T_{CDW} [41], the transversal and longitudinal branches soften by only 12% and 3%, respectively. This is in agreement with the ARPES data presented in Figs. 6(a) and 6(b), which shows a depletion of the DOS at an in-plane propagation vector consistent with the partial phonon softening as well as along the whole k_{τ} direction.

Figure 12(b) compares the experimental data with the SSCHA calculations using different exchange-correlation functionals for the vdW interactions. We performed SSCHA minimizations *ab initio* with and without considering vdW corrections at all temperatures at which the IXS experiments were carried out. We center our analysis on the characterization of the CDW transition through the study of the temperature dependence of the softest acoustic mode at **q**_{CDW}. As explained in Sec. II B 2, from a thermodynamic point of view, the structural instability under study can be correctly characterized through the phonons obtained by diagonalizing the free-energy Hessian. As already discussed in Ref. [41], anharmonicity stabilizes the 1T structure of VSe₂ at high

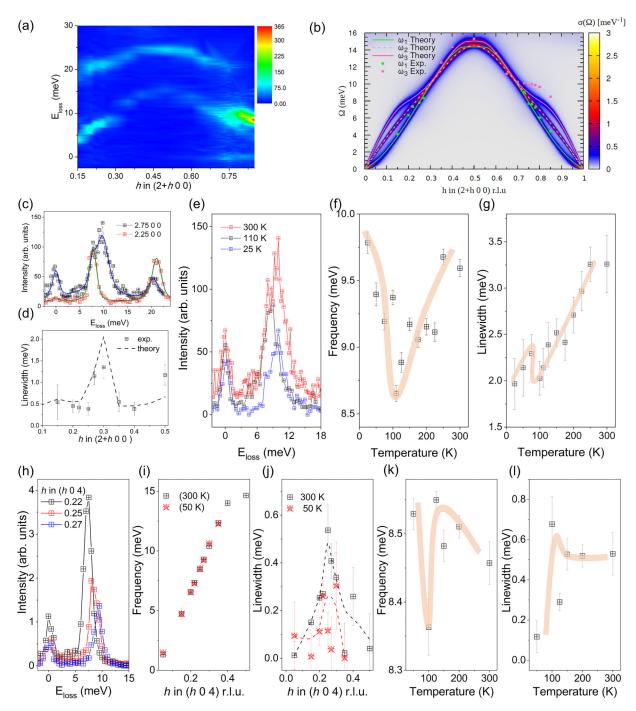


FIG. 11. (a) IXS dispersion of the low-energy phonons at 300 K along the $(2+h\ 0\ 0)$ direction, for 0.15 < h < 0.85 r.l.u. at 300 K. (b) SS-CHA spectral function calculated in the Lorentzian one-shot approximation at 300 K together with the experimental data. (c) Representative IXS spectra for h=0.25 and 0.75 r.l.u., highlighting the overlapping of the two longitudinal modes at high q. (d) Momentum dependence of the $(2+h\ 0\ 0)$ linewidth of phonon [full width at half maximum (FWHM)] for 0.15 < h < 0.5 r.l.u. at 300 K both from IXS and anharmonic SSCHA calculations including both phonon-phonon and EPI. (e)–(g) Temperature dependence of the longitudinal mode at $q=(2.25\ 0\ 0)$ r.l.u.: raw data (e), frequency (f), and linewidth (FWHM) (g). (h) Raw IXS spectra of the transverse character of the acoustic branch and (i) the corresponding dispersion obtained from the analysis at 300 and 50 K. (j) Momentum dependence of the linewidth of the transversal mode at 300 and 50 K. Broken lines are a guide to eye. (k) Temperature dependence of the frequency and (l) linewidth (FWHM) of the transversal branch $q=(0.25\ 0\ 4)$ r.l.u. Note that the softening in (f) is one order of magnitude larger than in (k).

temperatures only if vdW forces are taken into account in the calculation of the energies and forces needed to carry out the SSCHA variational minimization. vdW corrections must be included to properly characterize the transition that is related to the out-of-plane nature of the CDW, in which the interlayer distance is modulated. Definitely, anharmonicity and weak vdW interactions are responsible for the melting of the CDW.

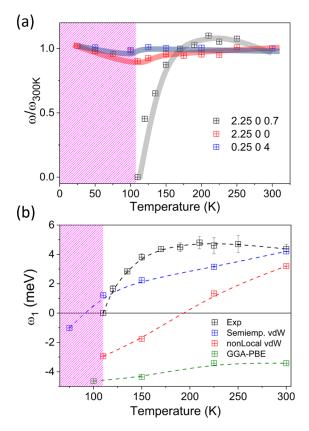


FIG. 12. (a) Experimental temperature dependence of the ω_1 mode normalized frequency at (2.25 0 0.7) r.l.u., the CDW wave vector, (2.25 0 0) r.l.u., and (2.25 0 4) r.l.u. (b) Experimental temperature of the ω_1 mode energy at (2.25 0 0.7) r.l.u. together with the anharmonic theoretical energies obtained with and without vdW corrections. The shaded area defines the CDW region in both panels.

The calculated CDW critical temperature strongly depends on how vdW interactions are included. The best agreement with the experimental result is obtained with the DFT-D2 method of Grimme [78], plotted with blue squares in Fig. 12, which simply adds a semiempirical dispersion correction on top of a converged Kohn-Sham energy. This theoretical result predicts that the soft mode frequency vanishes between 75 and 110 K, in good agreement with the experimental value of $T_{CDW} = 110 \text{ K}$ [41]. The, a priori, more sophisticated vdW-DF functional proposed by Dion et al. [79], which is truly nonlocal, is plotted with red squares and succeeds in melting the CDW, but overestimates the critical temperature by approximately 80 K. The lower critical temperatures obtained with Grimme's semiempirical vdW interactions might be due to the fact that it provides larger forces than the nonlocal vdW functional. It is interesting to remark, however, that the nonlocal vdW functional reproduces the CDW physics much better than the semiempirical approach in the VSe₂ monolayer [48], which is unable to predict the existence of the CDW transitions. The reason may be that Grimme's semiempirical approach is rather elemental and is probably introducing some arguably spurious intralayer contributions in supercell forces and energies that is slightly overestimating the contribution of vdW corrections.

D. Anisotropic EPI

The origin and stabilization mechanism of the CDW transition is still under debate, especially in systems with dimensions higher than 1D or quasi-1D, where Peierls' initial analysis of the FSN scenario probably does not hold. In fact, IXS and theoretical calculations already highlighted the importance of a highly momentum-dependent EPI in the formation of the CDW in similar compounds of the TMD family, such as 2H-NbSe₂ [23,92] and 1*T*-TiSe₂ [2,25]. Regarding 1*T*-VSe₂, the critical role of the momentum dependence of the EPI was already pointed out in Ref. [93] by means of quantitative models. More recently, IXS experiments and DFT-based SSCHA calculations have agreed in endorsing the electron-phonon coupling as the driving mechanism of the CDW transition in 1*T*-VSe₂, in spite of the presence of nesting [41].

Despite reaching clear conclusions, these calculations were only done for the constant height path in the reciprocal space that passes through \mathbf{q}_{CDW} . Considering that experiments trying to elucidate the CDW origin base their conclusions on the width of the BZ range in which the phonon branch is damped, we consider it useful to provide a deeper analysis by extending both the experimental and theoretical analysis to the perpendicular directions $(h \ k \ l)$ r.l.u. around \mathbf{q}_{CDW} .

In Fig. 13, we compare the frequencies of the soft phonon branch together with their total linewidth, which includes both the electron-phonon and anharmonic contributions, at 150 K, sweeping the CDW critical wave vector along h, k, and l. Figures 13(a)-13(c) display the momentum dependence of the phonon softening along the three directions with the (an)harmonic calculations. The theoretical calculations nicely match the experimental data when considering anharmonicity within SSCHA. Similarly, the experimental linewidth, which shows an anomalous broadening at the critical wave vector, follows the total linewidth obtained theoretically. Considering this effect in finer detail, we find that the region of momenta that undergoes a phonon renormalization (we define this region as the full width at half maximum (FWHM) of the momentum dependent softening) is anisotropic in momentum, space, both experimentally and theoretically. The phonon softening (broadening) extends to 0.05 r.l.u. (0.1 Å^{-1}) along h, 0.1 r.l.u. (0.2 Å^{-1}) along k, and 0.35 r.l.u. (0.35 Å^{-1}) along l. This momentum dependence is already present at the harmonic level, which reflects the anisotropy of the electron-phonon matrix-elements in momentum space, and nesting in a lower extent. Considering the FSN scenario as the driving force of the CDW formation, naively one would expect an isotropic softening (broadening) as a consequence of the localization of the phonon fluctuations in momentum space. This is in clear contrast with the data reported in Fig. 13. The anisotropic behavior we report evidences the fragility of proposing the nesting scenario as the origin of the CDW based only on the width of the BZ range in which the phonon branch is damped. Precisely, this kind of argument may be conditioned by the direction in which the scan is performed, at least in the case of 1T-VSe₂. Still, the fact that the anisotropy is accentuated in the out-of-plane l direction suggests that it may be related to the quasi-2D nature of the compound and, thus, it is reasonable to think that the EPI and anharmonic effects are also anisotropic in other compounds of the TMD family

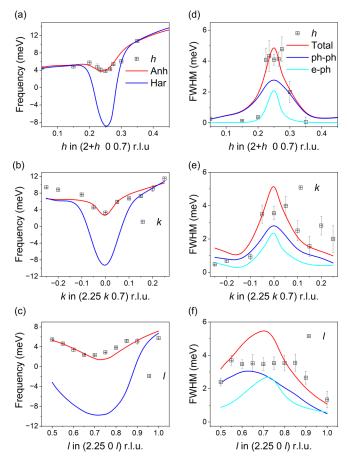


FIG. 13. (a)–(c) Experimental (points) and calculated (solid lines) dispersion of the soft mode at 150K around \mathbf{q}_{CDW} , but probing perpendicular directions (h k l) r.l.u. (d)–(f) Experimental (points) and theoretical (solid lines) linewidth as a function of momentum. The calculated linewidth (red line) includes the contribution of the EPI (light blue line) and anharmonicity (dark blue line).

and in other strongly correlated electron systems. Regardless of any potential generality, our results allow us to indicate that a pure nesting scenario for 1T-VSe $_2$ cannot solely act as the driving force, and clearly support previous claims that point to the electron-phonon coupling as the trigger for the CDW formation.

E. Pressure dependence of the soft mode at RT

Having comprehensively described the electronic structure and the temperature dependence of the low-energy lattice dynamics of VSe_2 , we finish our experimental survey by studying the evolution of the soft mode with pressure at RT. Systematic studies of the pressure dependence of the CDW in 2D and correlated materials reported a dramatic weakening of the charge modulations under low-to-moderate pressure [3,42–44,55]. In particular, the suppression of the CDW in 2H-NbSe₂ is directly related to the strong anharmonic character of the lattice potential, which stabilizes the high-temperature phase under pressure [3]. Recent transport experiments reported an intriguing enhancement of the CDW order in VSe_2 up to almost RT at \sim 13 GPa, in clear contrast to the typical behavior observed in CDW systems. At this

pressure, 1*T*-VSe₂ undergoes a first-order phase transition to a new C2/m phase, which destroys the charge order and allows SC to emerge [45]. Furthermore, high-pressure Raman [94], x-ray diffraction, and spectroscopic experiments [50] confirmed the transition to the C2/m phase proceeds at RT, similar to the 1*T*'-structures of ditellurides (Nb,Ta)Te₂ [95].

Figure 14 summarizes the pressure experiments carried out at RT. Up to 13 GPa, Fig. 14(a), the x-ray diffraction data shows a gradual displacement of the Bragg peaks towards larger detector angles, signaling the decrease of the lattice parameters under pressure. New Bragg peaks corresponding to a different phase, labeled with asterisks, appear above 13 GPa. The diffraction patterns below 13 GPa (P3m1 space group) were fitted with the GSAS software and returned the evolution of the lattice parameters displayed in Fig. 14(b). Fitting the pressure dependence of the volume to the second-order Birch-Murnaghan equation of state (EoS),

$$P(V) = \frac{3B_0}{2} \left[\left(\frac{V_0}{V} \right)^{7/3} - \left(\frac{V_0}{V} \right)^{5/3} \right] \times \left\{ 1 + \frac{3}{4} (B_0' - 4) \left[\left(\frac{V_0}{V} \right)^{2/3} - 1 \right] \right\}, \tag{16}$$

where P is the pressure, V_0 is the volume at zero pressure, B_0 is the Bulk modulus, and B_0' is the derivative of the bulk modulus with respect to pressure, returns a bulk modulus of $B_0 = 46.5$ GPa, slightly larger than the value reported in the literature [96].

Due to a favored scattering geometry, high-pressure IXS spectra of VSe2 were recorded in the BZ adjacent to the G_{031} reciprocal lattice vector (0 2.75 0.7) r.l.u., Fig. 14(c), equivalent to the G_{201} (see the DS in Fig. 9), scanning in reciprocal space along k as the pressure was increased. The results of these fits are given in Fig. 14(d). Focusing on the ω_2 branch, its frequency increases linearly under pressure ($\sim 0.3 \text{ meV/GPa}$) up to 13 GPa, as expected as the lattice becomes stiffer under pressure. Further, the linewidth decreases up to 10 GPa, after which the mode broadens on approaching the high-pressure phase transition (not shown). In contrast, the frequency of the soft ω_1 mode remains pressure independent up to 10 GPa, without collapsing on approaching the high pressure phase, but softens $\sim 10\%$ between 10 and 13 GPa. The phonon linewidth of this mode smoothly increases with pressure. The distinct behavior of the ω_1 phonon with temperature and pressure demonstrates the different nature of the phase transitions. While the CDW transition at 110 K agrees with a mean-field behavior with 0.5 critical exponent, the RT-high pressure transition is better described by a first-order phase transition.

SSCHA anharmonic calculations have been performed at RT for pressure values in the experimental range, making use of the experimental lattice parameters in Fig. 14(b). The application of pressure leads to a reduction of the interlayer distance c, which in turn lowers out-of-plane vdW interactions. Consequently, the choice of exchange-correlation functional has to be performed carefully. The theoretical phonon frequencies calculated with different exchange-correlation functionals are presented in Fig. 14(d). GGA-PBE wrongly predicts that, at 300 K, the system stays in the CDW phase for

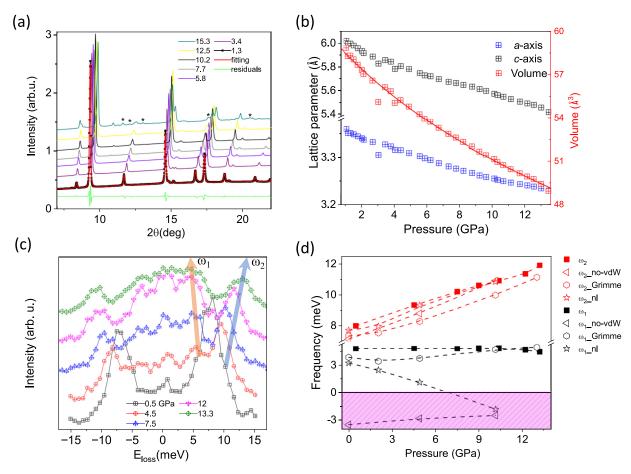


FIG. 14. (a) Representative x-ray diffraction scans as a function of pressure at 300 K. Peaks marked with an asterisk denote the new phase. The LeBail fitting to the experimental data is shown for 1.3 GPa. (b) Pressure dependence of the lattice parameters a and c. (c) Experimental pressure dependence of ω_1 and ω_2 at \mathbf{q}_{CDW} and (d) its comparison with SSCHA results from the free-energy Hessian including different vdW functionals.

all pressures. The nonlocal vdW exchange-correlation functional captures the CDW transition under pressure as the ω_1 phonon at q_{CDW} softens with increasing pressure, indicating that this functional correctly describes the increase of the CDW critical temperature with pressure. However, it underestimates the transition pressure to the new phase, in agreement with the fact that it overestimates at 0 GPa the CDW critical temperature. The semiempirical approach yields a phonon frequency ω_1 that increases with pressure, the opposite of the expected behavior and the experimentally observed trend, even if the absolute values obtained with this approach yield the closest frequencies to the experimental ones. All functionals yield accurate frequencies for the ω_2 phonon branch. The behavior of the frequencies with respect to the choice of functionals resembles the situation in the monolayer limit [48], in which the inclusion of the nonlocal vdW interactions in the exchange-correlation functional was mandatory to obtain a good description of the transition to the CDW phase.

IV. DISCUSSION AND CONCLUSIONS

Before summarizing the conclusions of our paper, we will briefly restate the major results. The resonant x-ray diffraction

does not find any possible indication of either chiral or orbital order, as reported for the 1T-TiSe₂ system [29–34], which is further corroborated by means of μSR . We see that a CDW with propagation vector (0.25 0 -0.3) r.l.u. in 1T-VSe₂ opens a pseudogap at $T > T_C$, with further depletion of DOS below T_C . Autocorrelation analysis of the Fermi surface maps finds indications of an enhanced charge susceptibility with propagation vector similar to the experimentally observed \mathbf{q}_{CDW} , but spread across all k_z values. It turns out that the maximum enhanced charge susceptibility coincides with the phonon collapse at T_{CDW}. However, from a nesting scenario point of view [91], one would expect (1) a singularity in the charge correlation map, which isotropically localizes the phonon fluctuations in momentum space, (2) a collapse of the low-energy phonon in a very narrow region of momenta [97], and (3) an isotropic EPI, contrary to the experimental observations. Furthermore, the acoustic longitudinal and transversal modes with l = 0 and 0.5 also undergo phonon renormalizations without collapsing, hence correlating the phonon anomalies with the charge susceptibility. In fact, the anisotropic linewidth shown in Fig. 13 is derived from highly anisotropic electron-phonon coupling matrix elements, which are related to the symmetry of the phonon polarization and the

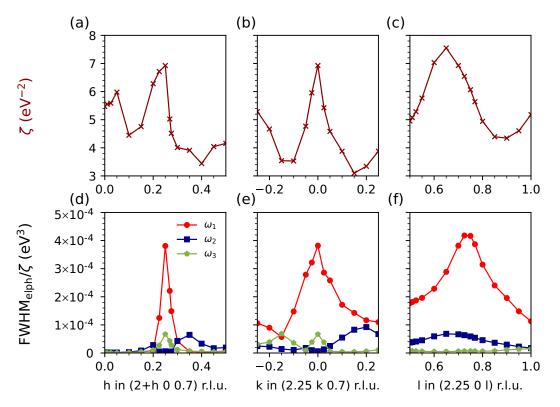


FIG. 15. (a)–(c) Nesting function around \mathbf{q}_{CDW} , probing perpendicular directions ($h \ k \ l$) r.l.u. (d)–(f) Ratio between the full width at half maximum given by the electron-phonon interaction and the nesting function at the same wave vectors.

anisotropic electronic band structure or the multiband Fermi surface recently pointed out [37].

To gain a deeper understanding of the correlation between the electronic structure and lattice dynamics of VSe_2 , we compute the nesting function $\zeta(\mathbf{q})$:

$$\zeta(\mathbf{q}) = \frac{1}{N} \sum_{nn'} \sum_{\mathbf{k}}^{1BZ} \delta(\epsilon_{n'\mathbf{k}+\mathbf{q}}) \delta(\epsilon_{n\mathbf{k}}). \tag{17}$$

The nesting function probes the Fermi surface by peaking at nesting \mathbf{q} wave vectors, revealing if the CDW emerges from a purely electronic instability. In Figs. 15(a)–15(c), we plot the nesting function around the perpendicular directions (h k l) r.l.u. of \mathbf{q}_{CDW} . The nesting function peaks just at the CDW vector for h and k in-plane scans, and nearby for the out-of-plane l scan, so \mathbf{q}_{CDW} coincides with a nested region of the Fermi surface.

To compare nesting and EPI scenarios, we plot the ratio between the electron-phonon linewidth and the nesting function in Figs. 15(d)–15(f), which allows us to directly assess the momentum and mode dependence of the electron-phonon coupling matrix elements following Eq. (13). The ratio shows that the EPI matrix elements still depend more strongly on momentum than the nesting function and, in fact, they have a very similar shape to the electron-phonon linewidth plotted in grey in Fig. 13. Remarkably, the scan alongside the out-of-plane direction shows that while the nesting function favors a commensurate $4\times4\times3$ CDW reconstruction, it is the EPI mechanism that leads to the incommensurate CDW reconstruction reported in our experiments with $l\simeq0.7$ r.l.u. Therefore, despite the presence of FSN, these calculations

also suggest that it is the EPI that is mostly responsible for the formation of the CDW in VSe₂.

In conclusion, the thorough experimental and theoretical analysis further supports the argument that the EPI is the main driving force of the CDW transition in 1T-VSe $_2$. This is in agreement with the general consensus that is being built in TMDs based on inelastic scattering experiments [23,25,41], detailed DFT calculations [20,91,93], and recent ARPES data [98] where the weak FS nesting is rather a factor enhancing the electron-phonon matrix elements than a driver of the CDW formation in these compounds.

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