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First-principles study of Co- and Cu-doped Ni$_2$MnGa along the tetragonal deformation path

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The influence of Co and Cu doping on Ni-Mn-Ga Heusler alloy is investigated using the first-principles exact muffin-tin orbital method in combination with the coherent-potential approximation. Single-element doping and simultaneous doping by both elements are investigated in Ni$_{50-x}$Co$_x$Mn$_{25-y}$Ga$_{25+y}$Cu$_4$ alloys, with dopant concentrations $x$, $y$, and $z$ up to 7.5 at. %. Doping with Co in the Ni sublattice decreases the $(c/a)_\text{NM}$ ratio of the nonmodulated (NM) martensite, but it simultaneously increases the cubic phase stability with respect to the NM phase. Doping with Cu in the Mn or in Ga sublattices does not change the $(c/a)_\text{NM}$ ratio significantly and it decreases the cubic phase stability. For simultaneous doping by Co in the Ni sublattice and Cu in the Mn or Ga sublattices, the effects of the individual dopants are independent and about the same as for the single-element doping. Thus, the $(c/a)_\text{NM}$ ratio can be adjusted by Co doping while the phase stability can be balanced by Cu doping, resulting in stable martensite with a reduced $(c/a)_\text{NM}$. The local stability of the cubic phase with respect to the tetragonal deformation can be understood on the basis of a density-of-states analysis.

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I. INTRODUCTION

Much attention has been paid to the Ni-Mn-Ga magnetic shape memory (MSM) alloys in the scientific and engineering communities for their application potential in actuators, sensors, harvesters, and magnetic refrigeration systems [1–3]. An interesting phenomenon exhibited by the MSM alloys is a giant magnetic-field-induced strain (MFIS) of up to 12% [4], which is known also as the MSM effect or magnetically induced reorientation (MIR) [1–3]. The effect occurs by the motion of twin boundaries in twinned martensite microstructure or, in other words, by the rearrangement of twins, in an applied external magnetic field.

The prerequisite for the MFIS is the existence of a twinned martensite microstructure. This is generated by a temperature-induced martensitic phase transformation of a high-temperature cubic phase, austenite, to a low-temperature phase of lower symmetry, martensite [5,6]. For stoichiometric Ni$_2$MnGa, the martensitic transformation occurs at the temperature $T_M = 202$ K, whereas the Curie temperature $T_C$ is about 376 K [7]. Several kinds of martensites have been observed in the Ni-Mn-Ga system [8,9]. The modulated five-layered (10M) phase exhibits about 6% MFIS [10,11], whereas nearly 10% MFIS can be obtained in the modulated seven-layered (14M) phase [12]. These values correspond to the maximum theoretical strains for MFIS allowed by the lattice distortion [1]. Both phases have $c/a$ ratios smaller than 1.

GIANT MFIS has never been reported for the third martensitic Ni$_x$Mn-Ga phase (see Ref. [4] and references therein) which has a purely tetragonal lattice without modulation [nonmodulated (NM) martensite] and a $(c/a)_\text{NM} \approx 1.17–1.23$ [13]. However, a MFIS of 12% has recently been reported in the NM phase for a structure with reduced $(c/a)_\text{NM} = 1.147$, achieved by simultaneous doping by 4 at. % of Cu and Co [4] resulting in the alloy composition Ni$_{46}$Co$_{3}$Mn$_{25}$Ga$_{22}$Cu$_{4}$. The large MFIS was made possible by the lowered twinning stress, which seems to be related to the reduced value of $(c/a)_\text{NM}$. Doping also had an effect on $T_M$ and $T_C$: both temperatures were above room temperature, $T_M = 330$ K and $T_C = 393$ K, which improves the practical applicability of the material.

The effect of compositional changes in Ni-Mn-Ga alloys and doping by different elements have been studied intensively in the recent decade by experimental and theoretical techniques and have been summarized in several reviews [14–17]. One of the important reasons for the alloy doping and composition adjustments is the increase of the operating temperature of the MSM material by shifting $T_M$ and $T_C$ to high temperatures. For example, when the concentration of Ni is increased in the Ni-Mn-Ga alloy, the $T_M$ also increases [18,19]. For the Co- and Cu-doped alloys deficient in Mn or Ga, $T_M$ increases [20,21], but it decreases if Co or Cu replaces Ni atoms [14,23]. On the other hand, the addition of Co instead of Ni increases the $T_C$. Here, we focus on simultaneous Cu and Co doping as this case has been shown recently to be crucial for keeping both $T_M$ and $T_C$ high and for the existence of MSM effect in the NM phase [4].

On the basis of the ab initio band-structure calculations, the Jahn-Teller effect has been proposed as responsible for structural instability of the austenite phase [22,24–26]. This effect is closely related to the Fermi surface nesting and phonon mode softening, which were revealed for the cubic phase [27–29]. Also, the exchange interaction between the Mn atoms is likely of high importance for structural properties of Ni-Mn-Ga alloys [17]. Unfortunately, the general mechanism of these effects has not been yet completely clarified.

Many theoretical works based on ab initio calculations have been dedicated to off-stoichiometric or doped Ni-Mn-Ga alloys, with special attention to site preference and elastic constants. For most of the off-stoichiometric Ni$_2$MnGa, the

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normal site preference is predicted, i.e., the excess atoms of the rich component prefer to occupy the sublattice of the deficient element [29]. The site preference problem of doping elements has been successfully clarified also for Cu and Co doping: Co exhibits a strong tendency to occupy the Ni sublattice in all types of alloys and Cu atoms always occupy the sublattice of the host elements in deficiency [26].

The works dedicated to the calculation of elastic constants have focused mainly on the high-temperature cubic phase and their correlations with $T_M$ since $T_M$ usually decreases with increasing $C'$ [30]. An empirical rule also follows from experiments: a larger number of valence electrons per atom ($e/a$) corresponds to a higher $T_M$ [18, 31–33]. The energy difference between the austenite and the nonmodulated martensite phase $\Delta E_{ANM}$ is another quantity closely related to $T_M$ that can be easily obtained from ab initio calculations. Its comparison with experimentally determined $T_M$ shows that a larger difference in total energies corresponds to a higher $T_M$ [34]. A comparative study for the total energy differences between austenite and the NM phase is still missing for (Cu- and Co-) doped Ni-Mn-Ga alloys, despite the importance of this quantity for understanding the phase stability in these systems.

The purpose of this paper is to reveal how the Co and Cu doping influences the stability of austenite with respect to NM martensite and also its effect on the equilibrium ($c/a_{NM}$) ratio of NM martensite. We present a detailed and comprehensive first-principles investigation of the effects of Co and Cu doping, studying first doping by single element and then simultaneous doping by both elements. Special attention is paid to the latter case, i.e., to Ni-Mn-Ga-Co-Cu alloys, since these exhibit new and interesting properties [4] but have not previously been studied theoretically and published experimental results are rare. We find that previously known empirical rules to an extent can be accounted for by a density-of-states (DOS) analysis. This study presents an attempt to understand the Ni-Mn-Ga-Co-Cu alloys theoretically and as such it can not provide complete answers to all questions on these new alloys, e.g., properties of modulated structures or nature of low twinning stress. Nonetheless, we believe that the presented results are of high relevance for the design of new compositions and provide a firm base for further more detailed theoretical work.

II. COMPUTATIONAL METHODS

All calculations of this work were carried out by the use of the first-principles method formulated with the exact muffin-tin orbital (EMTO) method [35–37]. In combination with the full charge density (FCD) technique for total energy calculations [35], the EMTO method is also suitable to accurately describe the total energy with respect to anisotropic lattice distortions such as tetragonal deformation. The chemical disorder caused by doping elements was included by using of the coherent-potential approximation (CPA) [38, 39]. This approximation does not take into account short-range interactions around the doping atoms, however, in full Heusler alloys, such short-range interactions only have a small influence on the electronic structure [40]. The exchange correlation was described using the Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation [41], and the scalar-relativistic and soft-core approximations were employed. The $s$, $p$, $d$, and $f$ orbitals were included in the EMTO basis sets. The Ni 3d$^8$4s$^2$, Mn 3d$^5$4s$^2$, Ga 3d$^{10}$4s$^2$4p$^1$, Co 3d$^7$4s$^2$, and Cu 3d$^{10}$4s$^1$ were treated as valence states. The Green’s function was calculated for 32 complex energy points distributed exponentially on a semicircular contour. In order to obtain the best agreement with experiments for a ($c/a_{NM}$), we introduced an additional optimization of the muffin-tin potential on the Ni sublattice according to Refs. [16, 42] by choosing the atomic radius $R_{Ni}^{s}$ = 1.10$R_{ws}$ and overlapping potential spheres $R_{Ni}^{p} = 0.95R_{ws}$, where $R_{ws}$ is the average Wigner-Seitz radius. For the other sublattices, the usual setup $R_{mg} = R_{ws}$ was used. In the one-center expansion of the full charge density, the number of components was truncated at 8. The Brillouin zone was sampled by a $13 \times 13 \times 13$ uniform $k$-point mesh without any smearing technique.

For stoichiometric Ni$_2$MnGa, the described settings resulted in the lattice constant of austenite ($L_2$) structure equal to 5.813 Å and local magnetic moments 0.33 $\mu_B$ and 3.52 $\mu_B$ of Ni and Mn atoms, respectively. For the NM phase, we obtained the lattice constant $a_{NM} = 5.382$ Å, ($c/a$)$_{NM} = 1.256$, and local magnetic moments 0.38 $\mu_B$ for Ni and 3.42 $\mu_B$ for Mn. These results are in good agreement with previous calculations (see Table 6.1 in Ref. [43] and references therein). The agreement for the lattice parameter of austenite is also very good compared to the experimental value $a_A = 5.825$ Å [8, 24]. The experimental lattice parameter of martensite $a_{NM} = 5.520$ Å is slightly larger [8, 24] than our calculated value. The calculated equilibrium ($c/a_{NM}$) ratio is overestimated compared to experimental value ($c/a_{NM}$) = 1.17 [8], which is, however, usual for all first-principles calculations [15, 17, 43–45].

After careful analysis of previous theoretical studies and available experimental results, three types of doping were considered: Co in Ni sublattice and Cu in Mn or Ga sublattices with dopant concentrations $x$, $y$, and $z$ between 0% and 7.5% in Ni$_{50−x}$Co$_x$Mn$_{25−y}$Ga$_y$S$_{5−z}$−Cu$_{y+z}$ alloys. For all such combinations, we calculated a series of total energies as a function of $c/a$ in the range between $c/a = 0.9$ and 1.4 at constant volume, which describes the tetragonal deformation of austenite phase with $L_2$ structure ($c/a = 1$). All calculated total energies along the deformation path are related to the energy of cubic structure for alloy with given composition. This provides a clear picture about the effect of doping elements on equilibrium ($c/a$)$_{NM}$ and relative energy difference $\Delta E_{ANM}$ between austenite and the NM phase.

III. RESULTS

A. Equilibrium volume and magnetic moments

We started the investigation by estimating the equilibrium atomic volumes of austenite $V_{0A}$ and tetragonal NM martensite $V_{0NM}$. This is important for correct calculations of total energies since they depend on the equilibrium atomic volume. Our results for austenite with single-element doping show a linear decrease of atomic volume with increasing dopant concentration, which is in agreement with previous published data [26]. For combined two-element doping, the...
TABLE I. The local magnetic moments (in $\mu_B$) of Ni, Mn, and Co in austenite and martensite phases for nondoped Ni$_{50}$Mn$_{25}$Ga$_{25}$ and for alloys with dopant concentrations $x$, $y$, or $z$ equal to 5% or 7.5%. The columns with equilibrium $(c/a)_{NM}$ and relative change of equilibrium volume with respect to volume of austenite $\Delta V_{el}$ (in %) are also included for the martensite phase.

<table>
<thead>
<tr>
<th>Composition</th>
<th>Austenite</th>
<th>Nonmodulated martensite</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ni$<em>{50}$Mn$</em>{25}$Ga$_{25}$</td>
<td>0.33</td>
<td>0.38</td>
</tr>
<tr>
<td>Ni$<em>{42}$Co$</em>{13}$Mn$<em>{25}$Ga$</em>{25}$</td>
<td>0.35</td>
<td>0.39</td>
</tr>
<tr>
<td>Ni$<em>{50}$Mn$</em>{22}$Ga$<em>{17}$Cu$</em>{15}$</td>
<td>0.39</td>
<td>0.38</td>
</tr>
<tr>
<td>Ni$<em>{50}$Mn$</em>{17}$Ga$<em>{32}$Cu$</em>{15}$</td>
<td>0.26</td>
<td>0.30</td>
</tr>
<tr>
<td>Ni$<em>{42}$Co$</em>{5}$Mn$<em>{25}$Ga$</em>{25}$Cu$_{15}$</td>
<td>0.42</td>
<td>0.39</td>
</tr>
<tr>
<td>Ni$<em>{42}$Co$</em>{13}$Mn$<em>{25}$Ga$</em>{20}$Cu$_{5}$</td>
<td>0.40</td>
<td>0.40</td>
</tr>
</tbody>
</table>

The local magnetic moments for Ni, Mn, and Co are summarized for Ni$_{50}$Mn$_{25}$Ga$_{25}$ without any doping, $x$ is the concentration of Co at Ni sites, $y$ is the concentration of Cu at Mn sites, and $z$ is the concentration of Ga at Cu sites, for the studied Ni$_{50-x}$Co$_x$Mn$_{25-y}$Ga$_{25-y}$Cu$_{y+z}$ alloy. This rule is valid for the whole concentration range used in this study. The volume decrease can be simply explained by the size difference between the host and alloying elements, with the exception of Co at Ni sites where magnetic effects probably affect the volume [26].

The equilibrium volume of the NM phase $V_{NM}$ is even smaller than $V_{0A}$, but the situation is slightly complicated. The concentration dependencies are still almost linear, but they follow a different rule, with the largest deviation being observed for Co doping. The reduction of volume is not as strong as in the case of austenite and $V_{NM}$ is somewhat larger than expected. This is probably due to the decreased equilibrium $(c/a)_{NM}$ of these alloys (see below), which pushes $V_{NM}$ higher. Similar trends are found in all other compositions containing Co but less significantly so.

The study of equilibrium volumes brings another finding. Although the energies along the tetragonal deformation path depend on atomic volume, their differences at $V_{0A}$ and $V_{NM}$ at the same composition are very small, especially for the small dopant concentrations ($x$, $y$, $z \lesssim 2.5\%$). Thus, these volume differences were neglected and the total energies were calculated at average volume between the $V_{0A}$ and $V_{NM}$ of alloy with given composition in all following calculations.

Similar linear trends are found also for the magnetic moments of austenite. However, the local magnetic moments do not differ more than about 0.1 $\mu_B$ in whole concentration range compared to nondoped Ni$_{50}$Mn$_{25}$Ga$_{25}$. The NM phase does not exhibit such strictly linear dependencies, which is caused by the varying equilibrium $(c/a)_{NM}$ for different concentrations. The magnetic moments of Co in this phase are $\approx 0.2$ $\mu_B$ smaller than for the austenite phase. The local magnetic moments for Ni, Mn, and Co are summarized in Table I for selected compositions. The table displays values for nondoped Ni$_{50}$Mn$_{25}$Ga$_{25}$ alloy and alloys where concentration of one of the doping elements is equal to 7.5%, which is the highest concentration used in this study.

\begin{align}
V_{0A} = V_{0A}^* - 0.0092x - 0.0155y - 0.0207z,
\end{align}

where $V_{0A}^*$ is the atomic volume of Ni$_{50}$Mn$_{25}$Ga$_{25}$ without any doping, $x$ is the concentration of Co at Ni sites, $y$ is the concentration of Cu at Mn sites, and $z$ is the concentration of Cu at Ga sites, for the studied Ni$_{50-x}$Co$_x$Mn$_{25-y}$Ga$_{25-y}$Cu$_{y+z}$ alloy. This rule is valid for the whole concentration range used in this study. The volume decrease can be simply explained by the size difference between the host and alloying elements, with the exception of Co at Ni sites where magnetic effects probably affect the volume [26].

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B. Single-element doping: Ni-Mn-Ga-Cu and Ni-Mn-Ga-Co alloys

First, we discuss Cu doping on Ga deficient alloy, i.e., the case where Cu atoms occupy the Ga sites. Figure 1(a) shows the total energy as a function of tetragonal ratio $c/a$...
for Ni₅₀Mn₂₅Ga₂₅₋ₓCuₓ alloys with tetragonally deformed L₂₁ structure with z between 0 and 7.5%. It can be seen from the figure that the Cu doping stabilizes the martensite phase because the minima corresponding to the NM phases are much deeper than for nondoped Ni₅₀Mn₂₅Ga₂₅ and ΔEₐ₋ₙM increases with increasing Cu concentration. For nondoped Ni₅₀Mn₂₅Ga₂₅, the ΔEₐ₋ₙM is equal to 0.379 mRy/atom (5.16 meV/atom). The increasing of the ΔEₐ₋ₙM approximately corresponds to 0.090 mRy/atom (1.22 meV/atom) for each 1% of added Cu. Because the experiments reveal that added Cu increase the Tₘ and stabilize the NM phase [20,21], our result supports the previous theoretical finding for nondoped off-stoichiometric Ni-Mn-Ga alloys, that a larger ΔEₐ₋ₙM corresponds to a higher Tₘ [34]. Addition of Cu has only a small effect on the position of equilibrium c/a, which stays almost unchanged or even slightly increases for a small concentration z [Fig. 1(a)].

For Cu doping at Mn sites (general formula Ni₅₀Mn₂₅₋ₓGaₓ₋ₙCuₓ), the alloy behaves differently, as shown in Fig. 1(b). The (c/a)ₙM slightly decreases with increasing Cu concentration. Surprisingly, this effect is weaker for larger y. The effect on the ΔEₐ₋ₙM is also very weak. The energy of NM martensite remains almost unchanged or even increases for y up to 2.5%. For larger y, the effect is more significant and the energy of the NM phase goes down, but still less than in the case of Ga deficient alloys. The effect of Cu on ΔEₐ₋ₙM is approximately two times stronger for Cu atoms at Ga sites than for Cu atoms at Mn sites. These results are in good agreement with a recently published study about Cu doping in Ni₂MnGa alloys, where a supercell approach was used and chemical disorder was not taken into account [46].

Co doping at Ni sites (Ni₅₀₋ₓCoₓMn₂₅Ga₂₅) has a much stronger effect on the equilibrium (c/a)ₙM [Fig. 1(c)] and even a low concentration of Co decreases (c/a)ₙM significantly and also noticeably decreases ΔEₐ₋ₙM. For alloys with the composition Ni₄₃Co₇Ni₅₂Mn₂₅ the values are (c/a)ₙM = 1.191 and ΔEₐ₋ₙM = 0.152 mRy/atom (2.07 meV/atom). If the concentration of Co is too high (x > 9%), the NM phase becomes less stable than austenite and a further increase of Co concentration results in unstable NM phase. This corresponds to the experimental result that increasing Co concentration stabilizes the cubic phase and decreases the Tₘ [14,23].

From the shape of the tetragonal deformation curves it can be seen that all types of doping lower the barrier between the austenite and martensite phases (Fig. 1). For doping by Cu, the barrier drops to zero for y ≈ 6% and z ≈ 4%. A new energy local minimum develops at c/a < 1 for z > 4% [see Fig. 1(a)]. The absence of a barrier means that the cubic phase loses its metastability, and becomes unstable at 0 K. It should be noted that vanishing of the barrier can involve also increasing of stability of the modulated phase with c/a < 1, but that problem is beyond the scope of this study. The height of the barrier measured from the cubic phase minimum is least affected by Co doping, where the barrier still exists even for higher x, where the austenite is a stable phase and the tetragonal martensite is metastable, although the barrier of course vanishes when the martensitic energy minimum is completely destabilized.

C. Two-element doping: Ni-Mn-Ga-Co-Cu alloys

From the single-element doping results presented above and from the experiments and reasoning in Ref. [4] it follows that a decrease in Tₘ by Co doping performed in order to decrease c/a can be compensated by simultaneous doping by Cu. We carried out calculations for simultaneous doping by Cu and Co to understand in which way the effects of individual elements are combined. Here, we present in detail only the case with Co at Ni sites and Cu at Ga sites since Cu at Ga sites appears to have a stronger effect. From the results presented in the following, it can be seen that the effects of Co and Cu are quite independent and the overall effect can be estimated rather precisely using linear superposition of the effects obtained by single-element doping.

Figure 2(a) shows the total energy of the Ni₄₅Co₇Mn₂₅Ga₂₅₋ₓCuₓ alloy as a function of tetragonal ratio c/a for different values of z. It is obvious that the decrease of ΔEₐ₋ₙM arising from doping by 5% of Co is now compensated by Cu doping since the energy of NM phase decreases and ΔEₐ₋ₙM grows. For example, the Ni₄₅Co₇Mn₂₅Ga₂₅Cu₃ alloys has ΔEₐ₋ₙM = 0.437 mRy/atom (5.94 meV/atom), whereas the ΔEₐ₋ₙM of Ni₄₅Co₇Mn₂₅Ga₂₅ (no Cu doping) is smaller by 0.285 mRy/atom (3.88 meV/atom). On the other hand, the equilibrium (c/a)ₙM is smaller due to the Co presence, but remains almost the same (1.190–1.200) for
all displayed curves, because the Cu itself has a negligible effect on $(c/a)_{\text{NM}}$.

A similar linear superposition of the effects of Cu and Co can be seen also for alloys with the general composition $\text{Ni}_{50-x}\text{Co}_x\text{Mn}_{25}\text{Ga}_{25}\text{Cu}_x$. The total energies as a function of $c/a$ are shown in Fig. 2(b) for the case where the concentration of Cu in the Ga sublattice is constant and the concentration of Co grows. Here, the energy difference $\Delta E_{A,\text{NM}}$ strongly decreases with increasing concentration of Co and simultaneously the equilibrium $(c/a)_{\text{NM}}$ decreases. $\Delta E_{A,\text{NM}}$ of the alloy $\text{Ni}_{45}\text{Co}_y\text{Mn}_{25}\text{Ga}_{25}\text{Cu}_y$ is smaller by 0.408 mRy/atom (5.50 meV/atom) than for $\text{Ni}_{50}\text{Mn}_{25}\text{Ga}_{25}\text{Cu}_5$ (without Co doping). However, both values are still larger than the value for nondoped $\text{Ni}_{50}\text{Mn}_{25}\text{Ga}_{25}$ due to the presence of Cu in the Ga sublattice.

Since all mentioned types of doping decrease the barrier between the austenite and the NM phase, the effect is correspondingly stronger for simultaneous doping by Co and Cu. The barrier vanishes for concentrations higher than $\sim 2.5\%$ of each doping element.

D. Distribution of Cu between Mn and Ga sublattices

The properties of the NM phase depend on the Cu distribution between Ga and Mn sites. This effect cannot be neglected because the difference in total energies of NM phase for edge cases is as large as 0.405 mRy/atom (5.50 meV/atom) for 5\% of Cu in the alloy. The dependence of $\Delta E_{A,\text{NM}}$ on the Cu distribution between the sites is linear with a minimum for all Cu at Mn sites and a maximum for all Cu at Ga sites. The effect is weaker for two-element doping when Co also resides at the Ni sites. The effect of the Cu distribution on $(c/a)_{\text{NM}}$ is very weak, with Cu at Mn sites decreasing the $(c/a)_{\text{NM}}$ slightly and Cu at Ga sites almost having no effect at all. Alloying with 5\% of Cu only causes a difference in $(c/a)_{\text{NM}}$ of 0.038 and additional Co doping further reduces the effect.

IV. DISCUSSION

The calculated results for $\Delta E_{A,\text{NM}}$ and $(c/a)_{\text{NM}}$ are summarized in Figs. 3 and 4. $\Delta E_{A,\text{NM}}$ decreases with increasing Co concentration at Ni sites and increases with increasing Cu

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**FIG. 3.** (Color online) Total energy differences between the austenite and NM phases $\Delta E_{A,\text{NM}}$ as a function of dopant concentration $x$, $y$, or $z$ for different alloy compositions. The horizontal thin line corresponds to values for the nondoped Ni-Mn-Ga alloy.

**FIG. 4.** (Color online) Equilibrium tetragonal ratio of the NM phase $(c/a)_{\text{NM}}$ as a function of dopant concentration $x$, $y$, or $z$ for different alloy composition. The horizontal thin line corresponds to the $(c/a)_{\text{NM}}$ for the nondoped Ni-Mn-Ga alloy.
concentration at Ga sites (Fig. 3). These trends can be seen also for combined two-element doping, with the contribution from each element approximately corresponding to its effect in single-element doping. The effect of Cu slightly dominates because the same concentrations of both doping elements increase $\Delta E_{\text{A,NM}}$ over the value for nondoped Ni-Mn-Ga. When Cu occupies Mn sites, $\Delta E_{\text{A,NM}}$ slightly decreases at first and then increases with increasing Cu concentration.

The results are in agreement with experimental findings, which show that Co at Ni sites decreases the $T_M$ [14] and Cu at Mn or Ga sites increases $T_M$ [20,21]. The previously published rule for off-stoichiometric, nondoped Ni-Mn-Ga alloys, which says that $T_M$ is correlated with $\Delta E_{\text{A,NM}}$, is valid also in the case of doped Ni-Mn-Ga alloys [34]. Our results also reflect the empirical rule that $T_M$, and consequently $\Delta E_{\text{A,NM}}$, should grow with increasing $e/\alpha [18,31-33]$. This quantity is shown in Fig. 5 for the same alloys as in Fig. 3. The only deviation from the empirical rule can be seen for small concentrations of Cu at Mn sites, the $e/\alpha$ grows but $\Delta E_{\text{A,NM}}$ decreases or remains the same, and only for larger $z$, $\Delta E_{\text{A,NM}}$ increases. Our results also agree with the previous theoretical finding that the tetragonally distorted structure is preferred in Heusler alloys only above certain $e/\alpha > 7.25-7.5$ [47], while the cubic structure is preferred below this $e/\alpha$ ratio. In our particular case, the cobalt doping decreases the $e/\alpha$, which results in unstable tetragonal structure when crossing the point $e/\alpha \approx 7.4$.

Note that for the calculation of $e/\alpha$, a different number of valence electrons was used than we have introduced in Sec. II as an input for EMTO calculations. In previous studies, only the $4s^2 4p^1$ orbitals were treated as valence states of Ga and $3d^{10}$ electrons were not included in this case [20,33]. For other elements, the number of valence electrons was the same as described in Sec. II.

Almost all compositions studied in this work decrease the equilibrium $(c/\alpha)_{\text{NM}}$ below the value for the nondoped alloy (Fig. 4), only simple doping by Cu in the Ga sublattice will increase it for small Cu concentrations, but for larger $z$, the value of $(c/\alpha)_{\text{NM}}$ is also smaller than for the nondoped alloy. A strong decrease can be seen for Co doping on Ni sites. If Cu is added instead of Ga to the alloy with Co, the $(c/\alpha)_{\text{NM}}$ increases, but never exceeds the value for the nondoped alloy. For alloys with the same concentration of doping elements (Ni$_{50-x}$Co$_x$Mn$_{25}$Ga$_{25}$, where $x = z$), the dependency is very similar to that of alloys with the compositions Ni$_{50-z}$Co$_z$Mn$_{25}$Ga$_{25}$ or Ni$_{50-z}$Co$_z$Mn$_{25}$Ga$_{25}$Cu$_y$, meaning that the effect of Co doping is fundamental for determination of $(c/\alpha)_{\text{NM}}$.

The effect of doping on the local stability of the austenite phase with respect to the tetragonal deformation (tetragonal shear modulus $C'$ softening or hardening) can be explained by an analysis of a pseudogap in the minority (spin-down) DOS about 0.05 Ry below the Fermi level $E_f$ and a small peak about 0.02 Ry below the $E_f$. The pseudogap arises from the covalent nature of bonding between Ni and Ga [48], whereas the peak is related to a Jahn-Teller instability. This peak splits when a tetragonal deformation is exerted on the L2$_1$ structure, which leads to a decrease of the DOS at the Fermi level $E_f$ [see Fig. 6(a)] and stabilization of the tetragonal martensitic phase [22,24,49-51]. Li et al. showed that doping by Co in the Ni sublattice and Cu in the Mn and Ga sublattices fills the pseudogap and decreases this peak in the cubic phase, which leads to a weaker Jahn-Teller instability. Furthermore, a shallower and narrower pseudogap compared to the Ni$_3$MnGa indicates a weaker covalent bonding. The overall stability of the austenite with respect to the tetragonal deformation is a result of competition between both described effects [26].

Additionally, the position of the energy barrier on the tetragonal deformation path is also related to the position of the Jahn-Teller peak with respect to the $E_f$. When the tetragonal distortion pushes the peak through the Fermi level, the DOS at $E_f$ initially increases, raising the energy until the peak is centered on $E_f$ [see Fig. 6(a)]. This corresponds to the top of the barrier. Further tetragonal deformation will again reduce the DOS at $E_f$ which makes tetragonal distortion energetically favorable. If the suppression of the Jahn-Teller effect by doping is very strong, the DOS at $E_f$ never grows up upon tetragonal deformation which results in a very flat profile of total energy.

FIG. 5. (Color online) Number of valence electrons per atom $e/\alpha$ as a function of dopant concentration $x, y, or z$ for different alloy compositions. The horizontal thin line corresponds to values for the nondoped Ni-Mn-Ga alloy.
around \( c/a = 1 \) and the barrier does not exist. In some cases, the change in number of electrons compared with the undoped case shifts the Fermi level very close to the peak or even below it [see Fig. 6(b)]. This shift of the peak results in a new position of the barrier closer to the cubic phase or it can even completely destabilize the cubic phase with respect to the tetragonal deformation.

The considerations related to the Jahn-Teller effect and the energy barrier are valid only near the austenite equilibrium geometry (around \( c/a = 1 \)). The stability of the NM phase is affected also by other modifications of the electronic structure occurring far below \( E_f \) (Fig. 6).

Figure 7 shows in detail our results for the minority (spin-down) DOS channel around \( E_f \) for the cubic L2\(_1\) austenite state without dopants and for a concentration of 5% of doping elements. All studied dopings decrease the peak size, with the strongest effect for Co at Ni sites and smallest effect for Cu doped in Ga sublattice. Also, the peak position with respect to \( E_f \) is changed, with the largest effect coming, in contrast, from Cu at Ga sites. Effect of doping on pseudogap shallowing and narrowing is weakest for Cu in the Ga site, but strongest for Cu in the Mn site.

When Cu is doped in the Ga sublattice, the shift of the Fermi level closer to the peak is very strong (filled red triangles in Fig. 7), thus enhancing the contribution of the Jahn-Teller effect to local destabilization of austenite (\( C' \) softening) \[26\] and also shifts the position of the barrier closer to the cubic phase, which results, for higher concentration of Cu, in absolute instability of cubic phase with respect to the tetragonal deformation and stabilization of a new structure with \( c/a < 1 \) [Fig. 1(a)].

Because all kinds of doping reduce the Jahn-Teller instability and fill the pseudogap, these effects are even more pronounced for simultaneous doping by both elements (open symbols in Fig. 7). As we mentioned above, the effects of each doping element are quite independent. However, the narrowing and shallowing of the pseudogap is more pronounced by doping than the reduction of the Jahn-Teller peak. It means that the local stability of the austenite phase with respect to the tetragonal deformation will be always reduced compared to nondoped Ni\(_2\)MnGa alloy. That corresponds to \( C' \) softening, which is seen from the more flat profile of energy around \( c/a = 1 \) in Fig. 7. On the other hand, the Jahn-Teller effect still persists and the \( E_f \) is shifted closer to the Jahn-Teller peak, which pushes the barrier on the tetragonal deformation path closer to the cubic structure. This effect is similar to the case when only Cu is used for doping in the Ga sublattice.

V. CONCLUSIONS

The Co and Cu doping of Ni-Mn-Ga Heusler alloys has been studied using the EMTO-CPA first-principles method. For Cu doping of a Ga-deficient alloy, we have found a strong increase in the energy difference between the austenite and the nonmodulated martensite phase \( \Delta E_{\text{A,NM}} \), but just a small change of equilibrium \( (c/a)_{\text{NM}} \) of nonmodulated martensite. If, on the other hand, Cu is instead doped at Mn sites, the increase of \( \Delta E_{\text{A,NM}} \) is much smaller and a slight decrease of \( (c/a)_{\text{NM}} \) is seen. Co doping at Ni sites has much stronger effects, with increasing concentration of Co strongly decreasing both \( \Delta E_{\text{A,NM}} \) and \( (c/a)_{\text{NM}} \). These theoretical results are in good agreement with previous experimental findings because Cu doped in the Ga or Mn sublattice will increase the martensitic transformation temperature \( T_M \) and Co in the Ni sublattice will decrease it. \( \Delta E_{\text{A,NM}} \) can be used as a qualitative indicator of \( T_M \) also for doped Ni-Mn-Ga alloys and not only for off-stoichiometric alloys. Our results also correspond to another empirical rule, namely, that both \( T_M \) and \( \Delta E_{\text{A,NM}} \) are correlated with the number of valence electrons per atom \( e/a \) in the alloy.
We have also investigated alloys where both elements Cu and Co were used in simultaneous doping. Our results show that the effects of simultaneous doping can be estimated using a linear superposition of the effects of individual dopants. This can be used for effective tuning of material properties; in particular, the decreasing of $\Delta E_{A,NM}$ (and $T_M$) arising from Co doping can be compensated by Cu doping at Ga sites. However, the reduction of $\langle c/a \rangle_{NM}$ due to the Co doping is preserved because the Cu doping has just a small effect on this quantity.

We have also analyzed the density of states to explain the stability of austenite state with respect to the tetragonal distortion and to explain the position of a barrier on the deformation path. The position of the barrier depends on the position of the peak related to the Jahn-Teller instability with respect to the Fermi level because it is influenced by the doping elements. The shift of the peak closer to the Fermi level results in the shift of the top of the barrier closer to the cubic structure.

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