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Gandalf: Learning Label-label Correlations in Extreme Multi-label Classification via Label Features

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# ABSTRACT

Extreme Multi-label Text Classification (XMC) involves learning a classifier that can assign an input with a subset of most relevant labels from millions of label choices. Recent works in this domain have increasingly focused on a symmetric problem setting where both input instances and label features are short-text in nature. Short-text XMC with label features has found numerous applications in areas such as query-to-ad-phrase matching in search ads, title-based product recommendation, prediction of related searches. In this paper, we propose Gandalf, a novel approach which makes use of a label co-occurrence graph to leverage label features as additional data points to supplement the training distribution. By exploiting the characteristics of the short-text XMC problem, it leverages the label features to construct valid training instances, and uses the label graph for generating the corresponding soft-label targets, hence effectively capturing the label-label correlations. Surprisingly, models trained on these new training instances, although being less than half of the original dataset, can outperform models trained on the original dataset, particularly on the PSP@k metric for tail labels. With this insight, we aim to train existing XMC algorithms on both, the original and new training instances, leading to an average 5% relative improvements for 6 state-of-the-art algorithms across 4 benchmark datasets consisting of up to 1.3M labels. GANDALF can be applied in a plug-and-play manner to various methods and thus forwards the state-of-the-art in the domain, without incurring any additional computational overheads. Code has been open-sourced at www.github.com/xmc-aalto/InceptionXML.

# **CCS CONCEPTS**

• Information systems → Top-k retrieval in databases; Novelty in information retrieval; Link and co-citation analysis; Recommender systems; Clustering and classification.



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# **KEYWORDS**

label-label correlations, multi-label classification, data augmentation, extreme classifiers, co-occurrence matrix, correlation graph

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# **1** INTRODUCTION

*Extreme Multilabel Classification* (XMC) has found numerous applications in the domains of related searches [15], dynamic search advertising [31] and recommendation tasks, which require predicting the most relevant results that frequently co-occur together [5, 13], or are highly correlated to the given product or search query. These tasks are often modeled through embedding-based retrieval-cum-ranking pipelines over millions of possible web page titles, products titles, or ad-phrase keywords forming the label space.

Going beyond conventional tagging tasks for long textual documents consisting of hundreds of words, such as articles in encyclopedia [30], and bio-medicine [39], contemporary research focus has also widened to settings in which the input is just a short phrase, such as a search query or product title. Propelled by the surge in online search, recommendation, and advertising, applications of short-text XMC ranging from query-to-ad-phrase prediction [9] to title-based product-to-product [27] recommendation have become increasingly prominent.

A major challenge across XMC problems is the extreme imbalance observed in their data distribution. Specifically, these datasets adhere to Zipf's law [1, 42], i.e., following a long-tailed distribution, where most labels are tail labels with very few ( $\leq$  5) positive datapoints in a training set spanning  $\geq$  10<sup>6</sup> total data points (Table 1). With so few positive examples, training a successful classifier on these labels purely from instance-to-label pairs seems an insurmountable challenge. Therefore, recent methods have begun to incorporate additional data sources.

Label features and label co-occurrence. In many of the settings listed above, labels are not just featureless integers, but do

Datasets	Ν	L	APpL	ALpP	AWpP
LF-AmazonTitles-131K	294,805	131,073	5.15	2.29	6.92
LF-WikiSeeAlsoTitles-320K	693,082	312,330	4.67	2.11	3.01
LF-WikiTitles-500K	1,813,391	501,070	17.15	4.74	3.10
LF-AmazonTitles-1.3M	2,248,619	1,305,265	38.24	22.20	8.74

Table 1: Details of short-text benchmarks with label features. APpL is the avg. points per label, ALpP being avg. labels per point and AWpP is the length i.e. avg. words per point.

have a semantic meaning in and of themselves. For example, when matching products, each product ID could be associated with the name of the product. This is particularly attractive in the short-text setting, when both inputs and labels come from the *same* space of short phrases. Consequently, while earlier work mostly focused on the nuances of short-text inputs [9, 21], more recent methods have successfully incorporated the short-text label descriptors into their pipeline [7, 8, 27, 28].

Yet, this still seems to underutilize the wealth of information present in label features. In particular, we demonstrate that it is possible to train a classifier using *only* label information, that is, without ever presenting to it any of the training instances, and *outperform* the same classifier trained on the original training data on tail labels. This surprising feat is enabled by the exploitation of label co-occurrence information.

In particular, using the interchangability of label features and instances, instead of aiming for contrastive learning [7], we want to use the label features as additional, supervised training points. However, this requires them to be associated with some apriori unknown label vector. In order to generate training targets, we make the assumption that the probability of a label *j* being relevant for the textual feature of another label *i*, is equal to the conditional probability of observing *j*, given that *i* is also a relevant label.

**Contributions.** This insight yields a simple method, *Gandalf* (Graph AugmeNted DAta with Label Features), which exploits the unique setting of short-text XMC in a novel manner to generate additional training data in order to alleviate the data scarcity problem. As a data-centric approach, it is independent of the specific model architecture, enabling its application to a wide range of both current and potential future state-of-the-art models. The unchanged model architecture also implies that not only the model inference latency remains unchanged, but also peak memory consumption required during training is unaffected, contrary to some model-based approaches that incorporate label metadata [6, 7, 27].

The additional training instances lead to overall longer training time. Nonetheless, when keeping the compute budget fixed, we can observe *Gandalf* significantly outperforming the original dataset. When trained until convergence, we show an average of 5% improvement on 5 state-of-the-art extreme classifiers across 4 public short-text benchmarks, with some settings seeing gains up to 30%. In this way, XMC methods which inherently do not leverage label features can beat or perform on par with strong baselines which either employ elaborate training pipelines [7], large transformer encoders [8, 43, 45] or make heavy architectural modifications [27, 28] to leverage label features.

Finally, we show that Gandalf could be considered an extension of the GLaS [11] regularizer to the label feature setting. We interpret it as tuning the bias-variance trade-off, where the additional error introduced by inaccurate additional training data is more then compensated for by the decrease is variance, especially for extremely noise tail labels [4].

# 2 PRELIMINARIES

For training, we have available a multi-label dataset  $\mathcal{D}$  =

 $\left(\{\mathbf{x}_{i}, \mathbf{y}_{i}\}_{i=1}^{N}, \{\mathbf{z}_{l}\}_{l=1}^{L}\right)$  comprising of *N* data points. Each  $i \in [N]$  is associated with a small ground truth label vector  $\mathbf{y}_{i} \in \{0, 1\}^{L}$  from  $L \sim 10^{6}$  possible labels. Further,  $\mathbf{x}_{i}, \mathbf{z}_{l} \in \mathcal{X}$  denote the textual descriptions of the data point *i* and the label *l* which, in this setting, derive from the same vocabulary universe  $\mathcal{V}$  [7]. The goal is to learn a parameterized function  $f: \mathbf{x}_{i} \mapsto \mathbf{y}_{i}$ .

**One-vs-All Classification (OvA).** A common strategy for handling this learning problem is to map instances and labels into a common Euclidean space  $\mathcal{E} = \mathbb{R}^d$ , in which the relevance  $s_l(\mathbf{x})$  of a label l to an instance is scored using an inner product,  $s_l(\mathbf{x}) = \langle \Phi(\mathbf{x}), \mathbf{w}_l \rangle$ . Here,  $\Phi(\mathbf{x})$  is the embedding of instance  $\mathbf{x}$ , and  $\mathbf{w}_l$  the l'th column of the weight matrix  $\mathbf{W}$ .

The prediction function selects the *k* highest-scoring labels,  $f(\mathbf{x}) = \operatorname{top}_k (\langle \Phi(\mathbf{x}), \mathbf{W} \rangle)$ . Training is usually handled using the *one-vs-all* paradigm, which applies a binary loss function  $\ell$  to each entry in the score vector. In practice, performing the sum over all labels for each instance is prohibitively expensive, so the sum is approximated by a shortlist of labels  $S(\mathbf{x}_i)$  that typically contains all the positive labels, and only those negative labels which are expected to be challenging for classification [7–9, 21, 45]:

$$\mathcal{L}_{\mathcal{D}}[\Phi, \mathbf{W}] = \sum_{i=1}^{N} \sum_{l=1}^{L} \ell(\mathbf{y}_{il}, \langle \Phi(\mathbf{x}), \mathbf{w}_{l} \rangle)$$

$$\approx \sum_{i=1}^{N} \sum_{l \in \mathcal{S}(\mathbf{x}_{i})} \ell(\mathbf{y}_{il}, \langle \Phi(\mathbf{x}), \mathbf{w}_{l} \rangle).$$
(1)

Even though these approaches have been used with success, they still struggle in learning good embeddings  $\mathbf{w}_l$  for tail labels: A classifier that learns solely based on instance-label pairs has little chance of learning similar label representations for labels that do not co-occur within the dataset, even though they might be semantically related. Consequently, training can easily lead to overfitting even with simple classifiers [11].

Label Features. To reduce the generalization gap, regularization needs to be applied to the label weights **W**, either explicitly as a new term in the loss function [11], or implicitly through the inductive biases of the network structure [27, 28] or by a learning algorithm [7, 8]. These approaches incorporate additional label metadata – *label features* – to generate the inductive biases. For short-text XMC, these features themselves are often short textual description, coming from the same space as the instances, as the following examples, taken from (i) LF-AmazonTitles-131K (recommend related products given a product name) and (ii) LF-WikiTitles-500K (predict relevant categories, given the title of a Wikipedia page) illustrate:



Figure 1: Gandalf augments the training dataset D by generating soft targets for each label based on label co-occurrence statistics. These additional datapoints Z are simply concatenated to the traditional dataset for training.

*Example 1:* For <u>"Mario Kart: Double Dash!!"</u> on Amazon, we have available: Mario Party 7 | Super Smash Bros Melee | Super Mario Sunshine | Super Mario Strikers as the recommended products.

*Example 2:* For the "2022 French presidential election" Wikipedia page, we have the available categories: April 2022 events in France | 2022 French presidential election | 2022 elections in France | Presidential elections in France. Further, a google search of the same query, leads to the following related searches - French election 2022 - The Economist | French presidential election coverage on FRANCE 24 | Presidential Election 2022: A Euroclash Between a "Liberal... | French polls, trends and election news for France, amongst others.

In view of these examples, one can affirm two important observations: (i) the short-text XMC problem indeed requires recommending similar items which are either highly correlated or co-occur frequently with the queried item, and (ii) the queried item and the corresponding label-features form an "equivalence class" and convey similar intent [7]. For example, a valid news headline search should either result in a page mentioning the same headline or similar headlines from other media outlets (see Example 2). As a result, it can be argued that data instances are interchangeable with their respective labels' features. Exploiting this interchangeability of label and instance text, Dahiya et al. [7, 8] proposes to tie encoder and decoder together and require  $\mathbf{w}_l = \Phi(\mathbf{z}_l)$ . While indeed yielding improved test performance, the condition  $\mathbf{w}_{l} = \Phi(\mathbf{z}_{l})$  turns out to be too strong, and it has to allow for some fine-tuning corrections  $\eta_l$ , yielding  $\mathbf{w}_l = \Phi(\mathbf{z}_l) + \eta_l$ . Consequently, training of SIAMESEXML and NGAME is done in two stages: a contrastive loss is minimized, followed by fine-tuning with a classification objective.

*Label correlations.* Label-label dependencies can appear in multi-label classification in two different forms: *Conditional* label correlations, and *marginal* label correlations [10]. In the conditional case, label dependencies are considered conditioned on each individual query, that is, they are independent if<sup>1</sup>

$$\mathbb{P}[\mathbf{Y} \mid X] = \prod_{j} \mathbb{P}[Y_j \mid X] .$$
<sup>(2)</sup>

As an example, consider the search query *"Jaguar*": If we know just this search term, the results pertaining to both, the car brand and the animal, are likely to be relevant. However, knowing that during a particular instance of this search, the user was interested in the animal, one can conclude that car-based labels are less likely to be relevant. In this way, the presence of one label gives information *beyond* what can be extracted just from the search query.

On the other hand, similar labels will generally appear together. Taking example 2 from the previous section, labels "2022 events in France" and "2022 elections in France" will have an above-random chance of occurring together; however, that information is already carried in the query "2022 French presidential election", so the presence of one of these labels doesn't provide any new information, given the query. In that sense, labels are marginally independent if

$$\mathbb{P}[\mathbf{Y}] = \prod_{j} \mathbb{P}[Y_{j}] . \tag{3}$$

Given an instance, OvA classifiers generate scores independently for all labels. Thus, they are *fundamentally incapable* of modelling conditional label dependence. However, as standard performance metrics (P@k, PSP@k) are also decomposable into independent contributions of each label, that is, they can be expressed purely in terms of label marginals, they are similarly incapable of detecting whether a classifier models conditional label dependence [10].

This means that, as long as we want to focus on these standard metrics (and not on inter-dependency aware losses such as Hüllermeier et al. [14]), we only need to care about marginal correlations. At first glance, this seems trivial: It can be shown that an OvA classifier, trained using a proper loss, is consistent for P@k [26, 40]. Unfortunately, consistency only tells us that, in the limit of infinite training data, we will get a Bayes-optimal classifier. However, in practice, the XMC setting is very far from infinite data—most tail labels will have less than five positive training examples.

Thus, the question we aim to tackle here is: *Can we exploit knowl-edge about marginal label correlations to improve training in the data-scarce regime of long-tailed multi-label problems?* 

 $<sup>^1\</sup>mathrm{Capital}\,X$  and Y denote the random variables associated with instance and labels, rsp.

		]	LF-Amaz	zonTitles-	131K	LF-WikiSeeAlsoTitles-320K						
Training Data	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5
original ${\cal D}$	35.62	24.13	17.35	27.53	33.06	37.50	21.53	14.19	10.66	13.06	14.87	16.33
surrogate ${\cal Z}$	29.68	21.47	16.04	28.76	33.75	38.27	22.88	16.02	12.44	22.03	23.69	25.55
$\mathcal{G} = \mathcal{Z} \cup \mathcal{D}$	43.52	29.23	20.92	36.96	42.71	47.64	31.31	21.38	16.22	24.31	26.79	28.83
$\mathcal{U}(\mathcal{G},N)$	38.46	25.81	18.52	32.29	37.17	41.59	25.93	17.54	13.34	19.75	21.76	23.57
$\mathcal{Z}^1 \cup \mathcal{D}$	37.59	25.25	18.18	30.75	35.54	40.06	24.43	16.16	12.15	16.89	18.45	20.02
$\mathcal{G}, y_{ll'} = \sigma(S_{ll'})$	42.80	28.64	20.49	37.01	42.07	46.73	30.28	21.15	15.43	23.97	25.16	28.45

Table 2: Experiments showing the quality of the datasets created with label features on InceptionXML. While the baseline is surpassed by training on the combined dataset G, it is also beaten by training on Z, where |Z| < |N|/2, underscoring its quality.

# 3 GANDALF: LEARNING FROM LABEL-LABEL CORRELATIONS

By combining marginal label correlations with label features, we can extend the *self-annotation postulate* of Dahiya et al. [7] to:

**Postulate 3.1.** Label-feature Annotation: Given a label j with label-features  $z_j$ , we posit that if these features are posed as a data point, its labels should follow the marginal label correlations, that is

$$\mathbb{P}\left[Y_i = 1 \mid X = \mathbf{z}_j\right] \approx \mathbb{P}\left[Y_i = 1 \mid Y_j = 1\right] . \tag{4}$$

Note that this reduces to self-annotation by setting i = j, in which case equation 4 becomes  $\mathbb{P}[Y_j | \mathbf{z}_j] \approx \mathbb{P}[Y_j | Y_j] = 1$ .

In words, this means that, if the presence of label j indicates that label i would occur with a certain probability for that same instance, then we assume that this probability is also how likely that label i is to be relevant to a data point that consists of the label features of label j. The right side of equation 4 can be written as

$$\mathbb{P}[Y_i = 1 \mid Y_j = 1] = \mathbb{P}[Y_i = 1, Y_j = 1] / \mathbb{P}[Y_j = 1] .$$
 (5)

Thus, we can use the co-occurrence statistics  $G_{ij} := \mathbb{P}[Y_i = 1, Y_j = 1]$  to calculate the conditionals, and thus apply a plug-in approach using empirical co-occurrence:

$$\mathbb{P}\left[Y_i = 1 \mid Y_j = 1\right] \approx \frac{\hat{G}_{ij}}{\hat{G}_{jj}}, \text{ where, } \hat{G}_{ij} \coloneqq \sum_{s=1}^n y_{si} y_{sj}.$$

Of course, in the data-scarce XMC regime, the co-occurrence matrix G will be very noisy. In practice, we empirically find it beneficial to threshold the soft labels at  $\delta$ , so that label features as data-points are annotated by:

$$y_{ij}^{\rm G} \coloneqq \begin{cases} \hat{G}_{ij} / \hat{G}_{jj} \text{ if } & \hat{G}_{ij} / \hat{G}_{jj} > \delta \\ 0 & \text{otherwise} \end{cases}$$
(6)

By approximating the left-hand side of equation 4 using a parameterized model  $\Psi$ , and taking the empirical co-occurrence as a noise estimate for the right-hand side, we can turn this equation into a (surrogate) machine-learning task. This is the same problem as the original XMC task equation 1, applied to a different dataset  $\mathcal{Z} = \{(z_i, y_i^G)\}_{i=1}^L$ . That is, we want to optimize

$$\mathcal{L}_{\mathcal{Z}}[\Psi, \mathbf{W}] \coloneqq \sum_{i,j=1}^{L} y_{ij}^{\mathrm{G}}, \langle \Psi(\mathbf{z}_{j}), \mathbf{w}_{i} \rangle ).$$
(7)

In Table 2, we present results for training on this surrogate task (row "Training on  $\mathbb{Z}$ "), when evaluating the resulting classifier on the original test set. The results are striking, and provide a strong confirmation of the equivalence principle between label features and input texts: Even though this model has *never* seen any actual training instance, it performs adequate (AmazonTitles) or better (WikiSeeAlsoTitles) than the original model in terms of precision at k. Looking at PSP, which gives more weight to tail labels, it actually outperforms the original model, in some cases with a large margin.

This tells us that we can, in fact, identify the two encoders in equations 1 and 7,  $\Psi \equiv \Phi$ , and train a single model on the combined dataset  $\mathcal{G} = \mathcal{D} \cup \mathcal{Z}$ , as illustrated in Figure 1. This combination of data yields strong improvements on both regular and tail-label performance metrics.

### 3.1 Bias-Variance Trade-off

This improvement cannot be explained by the increased training set size  $|\mathcal{G}| = N + L$  alone, as we can show with the following simple experiment: We generate a new dataset  $\mathcal{G}' \sim \mathcal{U}(\mathcal{G}, N)$  by uniformly sampling (without replacement) from the combined dataset a subset that has the same size as the original training set  $|\mathcal{D}| = N$ . Table 2 shows that this already leads to significant improvements over the original training set.

To explain this phenomenon, we note that this augmented data is qualitatively slightly different from the original training instances: the empirical co-occurrence matrix  $\hat{G}$  provides *soft* labels  $\mathbf{y}_i^{\mathrm{G}}$  as training targets. XMC dataset exhibit high variance [3, 4] because of the long tail labels, whereas the soft labels of the augmented points provide a much smoother training signal. On the other hand, they are based on the approximation of Postulate 3.1, and as such, will introduce some additional bias into the method, essentially leading to a highly favourable bias-variance trade-off.

In fact, the reduction in variance is so helpful to the training process that even switching out equation 4 with one-hot labels based purely on the self-annotation principle  $(y_{ij}^{SA} \coloneqq \mathbb{1}[i = j]$  such that  $\mathcal{Z}^1 = \{(\mathbf{z}_i, \mathbf{y}_i^{SA})\}_{i=1}^L$ ), thus considerably increasing the bias in the generated data, we still get significant improvements over just using the original training data (Table 2).

#### 3.2 Connection to GLaS regularization

In order to derive a model for  $\mathbb{P}[Y_{l'} = 1 \mid X = z_l]$ , we can take inspiration from the GLAS regularizer [11]. This regularizer tries to



(a) Results on LF-AmazonTitles-131K

(b) Results on LF-WikiSeeAlsoTitiles-320K

Figure 2: GANDALF demonstrating improvements on the P@5 metric across various methods, separated into tail, torso and head labels. On the x axis, the middle row indicates the number of labels in the bin, and the lowest row denotes the average number of positives per label in that bin. Improvements in earlier bins (5 - 3) denote gains in tail label performance.

make the Gram matrix of the label embeddings  $\langle \mathbf{w}_i, \mathbf{w}_j \rangle$  reproduce the co-occurrence statistics of the labels S,

$$\mathcal{R}_{\text{GLaS}}[\mathbf{W}] = L^{-2} \sum_{i=1}^{L} \sum_{j=1}^{L} \left( \langle \mathbf{w}_i, \mathbf{w}_j \rangle - S_{ij} \right)^2.$$
(8)

Here, S denotes the symmetrized conditional probabilities,

$$S_{ij} \coloneqq 0.5(\mathbb{P}[Y_i = 1 \mid Y_j = 1] + \mathbb{P}[Y_j = 1 \mid Y_i = 1]) \\\approx 0.5(\hat{G}_{ij}/\hat{G}_{jj} + \hat{G}_{ij}/\hat{G}_{ii}).$$
(9)

By the self-proximity postulate [7], we can assume  $\mathbf{w}_l \approx \Phi(\mathbf{z}_l)$ . For a given label feature instance with target soft-label  $(\mathbf{z}_l, y_{ll'}^{\text{GLaS}})$ , the training will try to minimize  $\ell(\langle \Phi(\mathbf{z}_l), \mathbf{w}_{l'} \rangle, y_{ll'}^{\text{GLaS}})$ . To be consistent with Equation 8, we therefore want to choose  $y_{ll'}^{\text{GLaS}}$  such that  $S_{ll'} = \arg\min \ell(\langle y_{ll'}^{\text{GLaS}})$ . This is fulfilled for  $y_{ll'}^{\text{GLaS}} = \sigma(S_{ll'})$  for  $\ell$  being binary cross-entropy, where  $\sigma$  denotes the logistic function.

While the soft targets generated this way slightly differ from the ones of equation 6, as already observed, the bias introduced by mildly incorrect training targets is offset by far by the variance reduction, and we find that this version performs only slightly worse than *Gandalf* (Table 2).

## 4 EXPERIMENTS

**Benchmarks, Baseline and Metrics**. We benchmark our experiments on 4 standard public datasets, the details of which are mentioned in Table 1. To test the generality and effectiveness of our proposed *Gandalf*, we apply the algorithm across a variety of state-of-the-art short-text extreme classifiers. These consist of (i) base frugal models -ASTEC [9] and INCEPTIONXML [21] - which do not, by default, leverage label text information, (ii) DECAF [27], ECLARE [28] and INCEPTIONXML-LF which equip the base models with additional encoders to make use of label text and label correlation

information and, (iii) NGAME + RENEE - consisting of RENEE [17], which makes CUDA optimizations to train BCE loss over a classifier for *L* labels without a shortlist. The transformer encoder is initialized with pre-trained NGAME (M1, dual encoder) [8]. We measure the performance using standard metrics P@k, its propensity-scored variant, PSP@k [16, 32], and coverage@k [37, 38].

#### 4.1 Main Results

**Improvements on tail labels**. We perform a quantile analysis across 2 datasets – LF-AmazonTitles-131K and the LF-WikiSeeAlso-Titles-320K (Figure 2) with INCEPTIONXML – where we examine performance (contribution to P@5 metric) over 5 equi-voluminous bins based on increasing order of mean label frequency in the training dataset. Consequently, performance on head labels can be captured by the bin #1 and that of tail labels by bin #5. We note that introducing the additional training data with *Gandalf* consistently improves the performance across all label frequencies, with more profound gains on bins with more tail labels. This is further verified by significant performance boosts, with base models showing upto 11% improvements in the PSP@k metrics in Table 3.

**Gandalf vs Architectural Additions (LTE, GALE).** The first formal attempt to externally imbue the model with label information was made with DECAF, which essentially equips the base model ASTEC with another base encoder (*LTE*) to learn label text ( $z_l$ ) embeddings along with the classifier. The second attempt, in the form of ECLARE, builds upon DECAF by adding another base encoder (*GALE*) to process and *externally* capture label correlation information. To make our claim more general, we also evaluate on INCEPTIONXML-LF, which consist of the same extensions on a more recent base model INCEPTIONXML [21] with *LTE* and *GALE* components (just as ECLARE adds *LTE* and *GALE* to ASTEC). While such architectural modifications help capture higher order query-label

Method	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5				
	LF-AmazonTitles-131K							LF-AmazonTitles-1.3M								
SiameseXML	41.42	30.19	21.21	35.80	40.96	46.19	49.02	42.72	38.52	27.12	30.43	32.52				
Astec + Gandalf	37.12	25.20	18.24	29.22 37.40	34.64 43.03	39.49 48 31	48.82	42.62	38.44 41.37	21.47	25.41 31.20	27.86				
DECAE	38.40	25.84	18.65	30.85	36.44	41 42	50.67	44.49	40.35	22.07	26.54	29.30				
+ Gandalf	42.43	28.96	20.90	35.22	42.12	47.61	53.02	46.65	42.25	25.47	30.14	32.83				
Eclare	40.46	27.54	19.63	33.18	39.55	44.10	50.14	44.09	40.00	23.43	27.90	30.56				
+ Gandalf	42.51	28.89	20.81	35.72	42.19	47.46	53.87	47.45	43.00	28.86	32.90	35.20				
InceptionXML	36.79	24.94	17.95	28.50	34.15	38.79	48.21	42.47	38.59	20.72	24.94	27.52				
+ Gandalf	44.67	30.00	21.50	37.98	43.83	48.93	50.80	44.54	40.25	25.49	29.42	31.59				
INCEPTIONXML-LF	40.74	27.24	19.57	34.52	39.40	44.13	49.01	42.97	39.46	24.56	28.37	31.67				
+ Gandalf	43.84	29.59	21.30	38.22	43.90	49.03	52.91	47.23	42.84	30.02	33.18	35.56				
Ngame + Renee	46.05	30.81	22.04	38.47	44.87	50.33	56.04	49.91	45.32	28.54	33.38	36.14				
+ Gandalf	45.86	30.53	21.79	40.49	45.83	50.96	56.88	50.24	45.47	26.56	31.69	34.60				
		LF	WikiSe	eAlsoTitle	es-320K		LF-WikiTitles-500K									
SiameseXML	31.97	21.43	16.24	26.82	28.42	30.36	42.08	22.80	16.01	23.53	21.64	21.41				
Astec	22.72	15.12	11.43	13.69	15.81	17.50	44.40	24.69	17.49	18.31	18.25	18.56				
+ Gandalf	31.10	21.54	16.53	23.60	26.48	28.80	45.24	25.45	18.57	21.72	20.99	21.16				
Decaf	25.14	16.90	12.86	16.73	18.99	21.01	44.21	24.64	17.36	19.29	19.82	19.96				
+ Gandalf	31.10	21.60	16.31	24.83	27.18	29.29	45.27	25.09	17.67	22.51	21.63	21.43				
Eclare	29.35	19.83	15.05	22.01	24.23	26.27	44.36	24.29	16.91	21.58	20.39	19.84				
+ Gandalf	31.33	21.40	16.31	24.83	27.18	29.29	45.12	24.45	17.05	24.22	21.41	20.55				
InceptionXML	23.10	15.54	11.52	14.15	16.71	17.39	44.61	24.79	19.52	18.65	18.70	18.94				
+ Gandalf	32.54	22.15	16.86	25.27	27.76	30.03	45.93	25.81	20.36	21.89	21.54	22.56				
INCEPTIONXML-LF	28.99	19.53	14.79	21.45	23.65	25.65	44.89	25.71	18.23	23.88	22.58	22.50				
+ Gandalf	33.12	22.70	17.29	26.68	29.03	31.27	47.13	26.87	19.03	24.12	23.92	23.82				
Ngame + Renee	30.79	20.65	15.57	20.81	24.46	27.05	-	-	-	-	-	-				
+ Gandalf	33.92	23.11	17.58	24.15	26.23	30.89	-	-	-	-	-	-				

Table 3: Results showing the effectiveness of *Gandalf* on state-of-the-art extreme classifiers. The best results are in bold. Results for NGAME + RENEE have been used from their publication, however, have not been reported for LF-WikiTitles-500K.

relations and increase empirical performance, they also increase both, training time and the peak GPU memory required during training by  $\sim 3\times$ .

As *Gandalf* is a data-centric approach, the memory overhead is eliminated by default. Further, we find that (i) DECAF and ECLARE still benefit from using *Gandalf* augmented data implying architectural modifications are complementary to *Gandalf*. However, (ii) simply using *Gandalf* augmented data enables base models ASTEC and INCEPTIONXML outperform themselves by up to 30% and perform nearly at par with their more architecturally equipped counter parts ECLARE and INCEPTIONXML-LF. While we posit that *Gandalf* and *GALE* learn complementary data relations, both our quantitative (Table 3) and qualitative (Table 5, Figure 2) results show that *Gandalf* is more effective and efficient at capturing these relations (specifically, label correlations) compared to the latter. **Beyond model performances**. We can also extract dataset specific insights with GANDALF from Table 3. Significant improvements on top of the base algorithm are particularly observed on LF-AmazonTitles-131K and LF-WikiSeeAlsoTitles-320K. In contrast, improvements on LF-WikiTitles-500K remain relatively mild. We attribute this to the density of the datasets. Specifically, while the former datasets consist of ~5 training instances per label, the latter consists of ~17. We posit a higher query-label density enables algorithms to inherently learn sufficient label-label correlations from existing data. However, we further see that using *Gandalf* is effective for LF-AmazonTitles-1.3M, the largest public benchmark for XMC with label features. Here, even though average training instances per label is ~38, the average number of labels per instance is ~22, as compared to maximum of ~4 on other datasets.

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Figure 3: The (a) P@1 and (b) PSP@5 metric plotted against iterations for InceptionXML with and without *Gandalf*. The effect of subsampling labels for *Gandalf* on the (c) P@1 and (d) PSP@5 metric. Both results are on the LF-AmazonTitles-131K dataset.

**Gandalf vs Siamese Learning**. Consequently, the third attempt made at capturing label correlations via SIAMESEXML, which essentially replaces the surrogate training task in ASTEC with a two-tower siamese learning framework. As argued in section 2, the condition  $\mathbf{w}_l = \Phi(\mathbf{z}_l)$  turns out to be too strong, and consequently training of SIAMESEXML and NGAME is done in two stages. Initially, a contrastive loss needs to be minimized, followed by fine-tuning with a classification objective which allows for some fine-tuning corrections  $\eta_l$ , yielding  $\mathbf{w}_l = \Phi(\mathbf{z}_l) + \eta_l$ . On the other hand, *Gandalf* simply extends training data to learn from a-priori label cooccurrence data in a supervised manner. Notably (from Table 3), ASTEC + *Gandalf* outperforms SIAMESEXML by 5-10% on Amazon datasets, while performing at par on Wikipedia datasets.

**Applying Gandalf to Two-tower approaches**. Although we propose GANDALF as a method suitable for training classifiers, it can also be used leveraged alongside two-tower approaches, like NGAME. This is done by first extending the dual encoder with a scalable classifier with RENEE, which simply trains OvA classifiers on top of the base model. Using GANDALF augmented data during this extension leads to significant improvements, more prominently on the LF-WikiSeeAlsoTitles-320K and LF-AmazonTitles-131K datasets.

**Coverage Results**. Coverage is an important metric in XMC as it demonstrates the ability of the model to predict tail labels effectively. We provide coverage results on InceptionXML in Table 4, demonstrating that Gandalf learns to predict labels which were previously not being predicted at all. This phenomenon can also be seen in the qualitative results Table 5.

Method	C@1	C@3	C@5	C@1	C@3	C@5			
	LF-An	nazonTit	tles-131K	LF-WikiSeeAlsoTitles-320					
InceptionXML + Gandalf	22.33	39.98 51.63	46.29	7.54	15.11 26.01	18.93 32 21			
+ Gandali	51.04	51.65	56.05	15.20	26.01	52.21			

Table 4: Coverage Results on InceptionXML with GANDALF.

#### 4.2 Ablations & Computational Analysis

*Gandalf*, is a data-centric approach that does not increase the computational cost during inference. While the inclusion of label features - which can often run in the order of millions - as additional data points might seem to increase the computational cost during training, through a series of observations, we show that this is in fact not the case. On the contrary, *Gandalf* can help in reducing the memory footprint while training, enabling researchers to use smaller GPUs, and reallocating their compute budget towards longer training schedules. Secondly, we also study the effect of subsampling the labels used for *Gandalf* to demonstrate how learning even some of the label-label correlations is beneficial for XMC models. This observation is particularly useful when inclusion of all label-features as data points becomes intractable due to its scale.

**Computational Costs during Training.** For the LF-Amazon-Titles-131K dataset, we plot the P@1 and the PSP@5 metric against iterations for InceptionXML, trained with and without Gandalf in Figure 3. As can be seen, using *Gandalf* gives better performance, even on tail labels, right from the beginning. Moreover, where the performance of InceptionXML saturates, the performance of *Gandalf* continues to scale with increasing compute. Therefore, given a fixed computational budget, a model trained with *Gandalf* will outperform one trained without it. This can also be seen in Table 2 where training on  $\mathcal{U}(\mathcal{G}, N)$ , i.e., under the exact same computational budget as training on the the original dataset gives performance improvements. In the same table, we can also observe improvements when training on *less than half* the original compute with  $\mathcal{Z}^2$ . These observations firmly place *Gandalf* as a computeefficient method of leveraging label-features in XMC models.

*Effect of Subsampling Labels.* We demonstrate the effect of subsampling labels used for *Gandalf* under two schemes, (a) Randomly sampling an expected percentage subset of labels and (b) randomly sampling this subset from equi-voluminous bins of increasing label frequency, i.e., prioritising tail labels for lower percentages. These results are shown for the P@1 and PSP@5 metric on the LF-AmazonTitles-131K dataset in Figure 3.

Both the metrics grow linearly as the percentage sampled labels are increased in steps of 25%. This goes ahead to show the lack of label-label correlations being captured in existing methods, and how learning even on a subset can be useful. Further, prioritising tail-labels consistently outperforms the random sampling baseline, underscoring the data-scarcity issue in XMC.

*Qualitative Results*. We further analyse qualitative examples via the top 5 predictions obtained by training the base encoders

<sup>&</sup>lt;sup>2</sup>These notations have been defined in Equation 2

Method	Datapoint	Baseline Predictions	Gandalf Predictions
INCEPTIONXML-LF		Pontryagin duality. Topological order, Topological quantum field theory, Topological quantum number, Quantum topology	Compact group, Haar measure, Lie group, Algebraic group, Topological ring
Decaf	Topological group         Topological quantum computer, Topological order, Topological quantum field theory, Topological quantum number, Quantum topology		Compact group, Haar measure, Lie group, Algebraic group, Topological ring
Eclare		Topological quantum computer, Topological order, Topological quantum field theory, Topological quantum number, Quantum topology	Compact group, Topological order, Lie group, Algebraic group, Topological ring
INCEPTIONXML-LF		List of lighthouses in Scotland, List of Northern Lighthouse Board light- houses, Oatcake, Communes of the Finistere department, Oat milk	Oatcake, Oatmeal, Oat milk, Porridge, Rolled oats
Decaf	Oat	Oatcake, Oatmeal, Design for All (in ICT), Oatley Point Reserve, Oatley Pleasure Grounds	Oatcake, Oatmeal, Oat milk, Porridge, Rolled oats
Eclare		<b>Oatmeal, Oat milk,</b> Parks in Sydney, Oatley Point Reserve, Oatley Pleasure Grounds	Oatcake, Porridge, Rolled oats, Oatley Point Reserve, Oatley Pleasure Grounds
INCEPTIONXML-LF		Lunar Orbiter Image Recovery Project, Lunar Orbiter 3, Lunar Orbiter 5, Chinese Lunar Exploration Program, List of future lunar missions	Surveyor program, Luna programme, Lunar Orbiter Image Recovery Project, Lunar Orbiter 3, Lunar Orbiter 5
Decaf	Lunar Orbiter program         Exploration of the Moon, List of man-made objects on the Moon, Lunar Orbiter Image Recovery Project, Lunar Orbiter 3, Lunar Orbiter 5		Exploration of the Moon, Apollo program, Surveyor program, Luna programme, Lunar Orbiter program
Eclare		Exploration of the Moon, Lunar Orbiter program, Lunar Orbiter Image Recovery Project, Lunar Orbiter 3, Lunar Orbiter 5	Exploration of the Moon, Pioneer program, Surveyor program, Luna programme, Lunar Orbiter program
INCEPTIONXML-LF		Colorado metropolitan areas, Front Range Urban Corridor, Outline of Colorado, Index of Colorado-related articles, State of Colorado	Colorado metropolitan areas, Outline of Colorado, Index of Colorado-related articles, Colorado cities and towns, Colorado counties
Decaf	Grand Lake, Colorado	Colorado metropolitan areas, Front Range Urban Corridor, State of Col- orado, Colorado municipalities, National Register of Historic Places listings in Grand County, Colorado	Outline of Colorado, State of Colorado, Colorado cities and towns, Colorado municipalities, Colorado counties
Eclare		State of Colorado, Colorado cities and towns, Colorado counties, National Register of Historic Places listings in Grand County, Colorado, Grand County, Colorado	Outline of Colorado, Index of Colorado-related articles, State of Colorado, Colorado cities and towns, Colorado counties
INCEPTIONXML-LF		Royal Saudi Air Defense, Royal Saudi Strategic Missile Force, Saudi Royal Guard Regiment, Terrorism in Saudi Arabia, Capital punishment in Saudi Arabia	Military of Saudi Arabia, Royal Saudi Air Force, Royal Saudi Air Defense, Royal Saudi Strategic Missile Force, King Khalid Military City
DECAF	Armed Forces of Saudi Arabia	Saudi Arabian-led intervention in Yemen, Saudi-led intervention in Bahrain, Human rights in Saudi Arabia, Legal system of Saudi Arabia, Joint Chiefs of Staff (Saudi Arabia)	Royal Saudi Air Force, Royal Saudi Navy, Royal Saudi Air Defense, Royal Saudi Strategic Missile Force, Saudi Arabian National Guard
Eclare		List of armed groups in the Syrian Civil War, Military of Saudi Arabia, Royal Saudi Strategic Missile Force, King Khalid Military City, Joint Chiefs of Staff (Saudi Arabia)	Military of Saudi Arabia, Royal Saudi Air Defense, Royal Saudi Strategic Missile Force, King Khalid Military City, Saudi Royal Guard Regiment

Table 5: Qualitative predictions from the LF-WikiSeeAlsoTitles-320K dataset. Labels indicate mispredictions.

with and without *Gandalf* augmented data points in Table 5. Notably, we can observe that queries with even a single keyword (*Oat*), which have no correct predictions without GANDALF, result in 100% correct predictions with it. Furthermore, even the quality of incorrect predictions improves and we suspect these labels are more likely to be *missed true positives*. [16] For example, in case of "Lunar Orbiter program", the only incorrect *Gandalf* predictions are "Lunar Orbiter 3", "Lunar Orbiter 5" and "Pioneer program" (US lunar and planetary space programs). Additionally, we show semantic similarity between the annotated labels with *G*, and the original label in Figure 4 in Appendix A.

**Comparison against conventional data augmentation strategies.** We compare GANDALF with with existing data augmentation techniques in Table 6. While no such techniques exist specifically for XMC, we use three baselines: synonym replacement(randomly replacing words in the input text with their synonyms, chosen via BERT similarity), MixUp and Label-MixUp. While the first two are standard data augmentations in NLP, Label-Mixup is a modified version of MixUp that combines the feature of a label feature and input datapoint, which is more suitable for XMC. Notably, Gandalf outperforms all of them with a significant margin:

Method	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5					
	LF-AmazonTitles-131K										
InceptionXML	35.62	24.13	17.35	27.53	33.06	37.50					
+ Synonym Replacement	35.07	23.71	17.08	27.20	32.41	36.77					
+ MixUp	35.63	24.15	17.37	27.55	33.00	37.63					
+ Label-MixUp	37.25	25.02	17.98	29.25	34.58	39.09					
+ Gandalf	43.52	29.23	20.92	36.96	42.71	47.64					
		LF	WikiSe	eAlsoTitle	es-320K						
InceptionXML	21.53	14.19	10.66	13.06	14.87	16.33					
+ Synonym Replacement	20.08	13.13	9.92	12.00	13.50	14.90					
+ MixUp	21.62	14.15	10.65	13.13	14.99	16.36					
+ Label-MixUp	23.90	16.10	12.28	15.20	17.60	19.56					
+ Gandalf	31.31	21.38	16.22	24.31	26.79	28.83					

Table	6: (	Comp	arison	of	convent	ional	data	augm	entation
strate	gies	with	the pro	pos	sed Gani	DALF n	netho	od.	

**Sensitivity to**  $\delta$ . We examine *Gandalf*'s sensitivity to  $\delta$  by training INCEPTIONXML-LF on data generated with varying values of  $\delta$ . As shown in Table 7, the empirical performance peaks at a  $\delta$  value of 0.1 which is sufficient to suppress the impact of noisy correlations. Higher values of  $\delta$  tend to suppress useful information.

Method	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5	P@1	P@3	P@5	PSP@1	PSP@3	PSP@5			
		LF-AmazonTitles-131K							LF-WikiSeeAlsoTitles-320K						
InceptionXML	35.62	24.13	17.35	27.53	33.06	37.50	21.53	14.19	10.66	13.06	14.87	16.33			
+ Gandalf $\mathcal{G}$	43.71	29.30	21.14	37.25	43.01	47.89	31.42	21.54	16.37	24.78	27.36	28.98			
+ Gandalf (G + Random Walk [28])	43.52	29.23	20.92	36.96	42.71	47.64	31.31	21.38	16.22	24.31	26.79	28.83			
INCEPTIONXML-LF	40.74	27.24	19.57	34.52	39.40	44.13	49.01	42.97	39.46	24.56	28.37	31.67			
+ Gandalf ( $\delta = 0.0$ )	41.71	28.03	20.14	36.94	41.93	46.64	31.40	21.56	16.53	26.01	27.89	29.99			
+ Gandalf ( $\delta = 0.1$ )	42.09	28.38	20.45	37.09	42.19	47.04	32.20	21.86	16.60	26.06	28.01	30.03			
+ Gandalf ( $\delta$ = 0.2)	41.73	28.10	20.18	37.01	41.99	46.67	31.29	21.35	16.28	25.68	27.59	29.65			

Table 7: Results demonstrating the effectiveness of *Gandalf* using both, a statistical co-occurrence matrix ( $\mathcal{G}$ ) and it's modified version using a random walk as in [28]. The table also shows the method's sensitivity to  $\delta$ , as defined in Equation 6.

**Choice of label co-occurrence graph** G. While with GANDALF, we leverage a statistical measure for G, we can also estimate it with random walks [28] (used for *GALE*). We find that our method is not significantly affected by this choice, with the co-occurrence graph giving slightly enhanced performance(Table 7). We hypothesise this happens due to the noise introduced via random walks. While both variants aim to model similar information, their differing usage determines their overall effectiveness. In particular, leveraging it for GANDALF helps learn sufficient information on top of *GALE*. Moreover, as discussed previously, our results are also not significantly affected by using the a symmetric variant of the graph, consistent with the GLaS regularizer, shown in Table 2.

#### **5 OTHER RELATED WORK**

Prior works in XMC focused on annotating long-text documents, consisting of hundreds of word tokens, such as those encountered in tagging for Wikipedia [2, 20, 36, 43] with numeric label IDs. Most recent works under this setting were aimed towards scaling up transformer encoders for the XMC task [22, 45].

Exploiting Correlations in XMC. For XMC datasets endowed with label features, there exist three correlations that can be exploited for better representation learning : (i) query-label, (ii) queryquery, and (iii) label-label correlations. Recent works have been successful in leveraging label features and pushing state-of-the-art by exploiting the first two correlations. For example, SIAMESEXML and NGAME [7, 8] employ a two-tower pre-training stage applying contrastive learning between an input text and its corresponding label features. GALAXC [35] & PINA [6], motivated by graph convolutional networks, create a combined query-label bipartite graph to aggregate predicted instance neighbourhood. This approach, however, leads to a multifold increase in the memory footprint. DECAF and ECLARE [27, 28] make architectural additions to embed label-text embeddings (LTE) and graph-augmented label embeddings (GALE) in each label's OVA classifier to exploit higher order correlations from the random walk graph. PINA, in its pre-training step, leverages label features as data points, but does so by expanding the label space  $\{0, 1\}^L$  to also include instances as  $\{0, 1\}^{L+N}$ leveraging the self-annotation property of labels [7] and inverting the initial instance-label mappings to have instances  $\mathbf{x}_i$  as labels for label features  $z_l$  as data points. This, however, leads to an explosion in an already enormous label space. In this work, we find that a

significant amount of information can be learned by modelling label-label correlations, which existing methods fail to leverage.

Two-tower Models & Classifier Learning. Typically, due to the single-annotation nature of most dense retrieval datasets [18, 24, 29], two-tower models [19] solving this task eliminate classifiers in favour of modelling implicit correlations by bringing querydocument embeddings closer in the latent space of the encoders. These works are conventionally aimed at improving encoder representations by innovating on hard-negative mining [25, 41, 44], teacher-model distillation [33, 34] and combined dense-sparse training strategies [23]. While these approaches result in enhanced encoders, the multilabel nature of XMC makes them, in itself, insufficient for this domain. This has been demonstrated in two-stage XMC works like Dahiya et al. [7, 8], Jain et al. [17] where these frameworks go beyond two-tower training and train classifiers with a frozen encoder in the second stage for better empirical performance. While a concurrent work [12] does show that dual-encoder XMC models can outperform classifiers, but requires significant computational resources to scale the contrastive loss across the entire label space.

## 6 CONCLUSION

In this paper, we proposed *Gandalf*, a strategy to learn label correlations, a notoriously difficult challenge. In contrast to previous works which model these correlations implicitly through model training, we propose a supervised approach to explicitly learn them by leveraging the inherent query-label symmetry in short-text extreme classification. We further performed extensive experimentation by implementing on various SOTA XMC methods and demonstrated dramatic increases in prediction performances uniformly across all methods. Moreover, this is achieved with frugal architectures without incurring any computational overheads in inference latency or training memory footprint. We hope our treatment of label correlations in this domain will spur further research towards crafting data-points with more expressive annotations, and further extend it to long-text XMC approaches where the instance-label symmetry is quite ambiguous.

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### REFERENCES

- Lada A Adamic and Bernardo A Huberman. 2002. Zipf's law and the Internet. Glottometrics 3, 1 (2002), 143–150.
- [2] R. Babbar and B. Schölkopf. 2017. DiSMEC: Distributed Sparse Machines for Extreme Multi-label Classification. In WSDM.
- [3] R. Babbar and B. Schölkopf. 2019. Data scarcity, robustness and extreme multilabel classification. *Machine Learning* 108 (2019), 1329–1351.
- [4] Anirudh Buvanesh, Rahul Chand, Jatin Prakash, Bhawna Paliwal, Mudit Dhawan, Neelabh Madan, Deepesh Hada, Vidit Jain, SONU MEHTA, Yashoteja Prabhu, Manish Gupta, Ramachandran Ramjee, and Manik Varma. 2024. Enhancing Tail Performance in Extreme Classifiers by Label Variance Reduction. In *The Twelfth International Conference on Learning Representations*. https://openreview.net/ forum?id=6ARlSgun7J
- [5] Wei-Lin Chiang, Xuanqing Liu, Si Si, Yang Li, Samy Bengio, and Cho-Jui Hsieh. 2019. Cluster-GCN: An Efficient Algorithm for Training Deep and Large Graph Convolutional Networks. In Proceedings of the 25th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining (Anchorage, AK, USA) (KDD '19). Association for Computing Machinery, New York, NY, USA, 257–266. https: //doi.org/10.1145/3292500.3330925
- [6] Eli Chien, Jiong Zhang, Cho-Jui Hsieh, Jyun-Yu Jiang, Wei-Cheng Chang, Olgica Milenkovic, and Hsiang-Fu Yu. 2023. PINA: Leveraging Side Information in eXtreme Multi-label Classification via Predicted Instance Neighborhood Aggregation. arXiv preprint arXiv:2305.12349 (2023).
- [7] Kunal Dahiya, Ananye Agarwal, Deepak Saini, Gururaj K, Jian Jiao, Amit Singh, Sumeet Agarwal, Purushottam Kar, and Manik Varma. 2021. SiameseXML: Siamese Networks meet Extreme Classifiers with 100M Labels. In Proceedings of the 38th International Conference on Machine Learning (Proceedings of Machine Learning Research, Vol. 139). PMLR, 2330–2340. https://proceedings.mlr.press/ v139/dahiya21a.html
- [8] Kunal Dahiya, Nilesh Gupta, Deepak Saini, Akshay Soni, Yajun Wang, Kushal Dave, Jian Jiao, Gururaj K, Prasenjit Dey, Amit Singh, et al. 2023. NGAME: Negative Mining-aware Mini-batching for Extreme Classification. In Proceedings of the Sixteenth ACM International Conference on Web Search and Data Mining. 258–266.
- [9] Kunal Dahiya, Deepak Saini, Anshul Mittal, Ankush Shaw, Kushal Dave, Akshay Soni, Himanshu Jain, Sumeet Agarwal, and Manik Varma. 2021. DeepXML: A Deep Extreme Multi-Label Learning Framework Applied to Short Text Documents. In Proceedings of the 14th ACM International Conference on Web Search and Data Mining (Virtual Event, Israel) (WSDM '21). Association for Computing Machinery, New York, NY, USA, 31–39. https://doi.org/10.1145/3437963.3441810
- [10] Krzysztof Dembczyński, Willem Waegeman, Weiwei Cheng, and Eyke Hüllermeier. 2012. On label dependence and loss minimization in multi-label classification. *Machine Learning* 88 (2012), 5–45.
- [11] C. Guo, A. Mousavi, X. Wu, Daniel N. Holtmann-Rice, S. Kale, S. Reddi, and S. Kumar. 2019. Breaking the Glass Ceiling for Embedding-Based Classifiers for Large Output Spaces. In *NeurIPS*.
- [12] Nilesh Gupta, Devvrit Khatri, Ankit S Rawat, Srinadh Bhojanapalli, Prateek Jain, and Inderjit S Dhillon. 2023. Efficacy of Dual-Encoders for Extreme Multi-Label Classification. arXiv:2310.10636 [cs.LG]
- [13] Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele Catasta, and Jure Leskovec. 2020. Open Graph Benchmark: Datasets for Machine Learning on Graphs. In Proceedings of the 34th International Conference on Neural Information Processing Systems (Vancouver, BC, Canada) (NIPS'20). Curran Associates Inc., Red Hook, NY, USA, Article 1855, 16 pages.
- [14] Eyke Hüllermeier, Marcel Wever, Eneldo Loza Mencia, Johannes Fürnkranz, and Michael Rapp. 2022. A flexible class of dependence-aware multi-label loss functions. *Machine Learning* 111, 2 (2022), 713–737.
- [15] Himanshu Jain, Venkatesh Balasubramanian, Bhanu Chunduri, and Manik Varma. 2019. Slice: Scalable Linear Extreme Classifiers Trained on 100 Million Labels for Related Searches. Proceedings of the Twelfth ACM International Conference on Web Search and Data Mining (2019).
- [16] Himanshu Jain, Yashoteja Prabhu, and Manik Varma. 2016. Extreme multilabel loss functions for recommendation, tagging, ranking & other missing label applications. In KDD. 935–944.
- [17] Vidit Jain, Jatin Prakash, Deepak Saini, Jian Jiao, Ramachandran Ramjee, and Manik Varma. 2023. Renee: End-to-end training of extreme classification models. Proceedings of Machine Learning and Systems (2023).
- [18] Mandar Joshi, Eunsol Choi, Daniel Weld, and Luke Zettlemoyer. 2017. TriviaQA: A Large Scale Distantly Supervised Challenge Dataset for Reading Comprehension. In Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers). Association for Computational Linguistics, Vancouver, Canada, 1601–1611. https://doi.org/10.18653/v1/P17-1147
- [19] Vladimir Karpukhin, Barlas Oğuz, Sewon Min, Patrick Lewis, Ledell Wu, Sergey Edunov, Danqi Chen, and Wen-tau Yih. 2020. Dense passage retrieval for opendomain question answering. arXiv preprint arXiv:2004.04906 (2020).
- [20] S. Khandagale, H. Xiao, and R. Babbar. 2020. Bonsai: diverse and shallow trees for extreme multi-label classification. *Machine Learning* 109, 11 (2020), 2099–2119.

- [21] Siddhant Kharbanda, Atmadeep Banerjee, Devaansh Gupta, Akash Palrecha, and Rohit Babbar. 2023. InceptionXML: A Lightweight Framework with Synchronized Negative Sampling for Short Text Extreme Classification. In Proceedings of the 46th International ACM SIGIR Conference on Research and Development in Information Retrieval (Taipei, Taiwan) (SIGIR '23). Association for Computing Machinery, Taipei, Taiwan, 760–769. https://doi.org/10.1145/3539618.3591699
- [22] Siddhant Kharbanda, Atmadeep Banerjee, Erik Schultheis, and Rohit Babbar. 2022. CascadeXML: Rethinking Transformers for End-to-end Multiresolution Training in Extreme Multi-label Classification. In Advances in Neural Information Processing Systems, Vol. 35. Curran Associates, Inc., 2074–2087. https://proceedings.neurips.cc/paper\_files/paper/2022/file/ 0e0157ce5ea15831072be4744cbd5334-Paper-Conference.pdf
- [23] Omar Khattab and Matei Zaharia. 2020. Colbert: Efficient and effective passage search via contextualized late interaction over bert. In Proceedings of the 43rd International ACM SIGIR conference on research and development in Information Retrieval. 39–48.
- [24] Tom Kwiatkowski, Jennimaria Palomaki, Olivia Redfield, Michael Collins, Ankur Parikh, Chris Alberti, Danielle Epstein, Illia Polosukhin, Jacob Devlin, Kenton Lee, Kristina Toutanova, Llion Jones, Matthew Kelcey, Ming-Wei Chang, Andrew M. Dai, Jakob Uszkoreit, Quoc Le, and Slav Petrov. 2019. Natural Questions: A Benchmark for Question Answering Research. *Transactions of the Association for Computational Linguistics* 7 (2019), 452–466. https://doi.org/10.1162/tacl\_a\_00276
- [25] Yuxiang Lu, Yiding Liu, Jiaxiang Liu, Yunsheng Shi, Zhengjie Huang, Shikun Feng Yu Sun, Hao Tian, Hua Wu, Shuaiqiang Wang, Dawei Yin, et al. 2022. Erniesearch: Bridging cross-encoder with dual-encoder via self on-the-fly distillation for dense passage retrieval. arXiv preprint arXiv:2205.09153 (2022).
- [26] Aditya K Menon, Ankit Singh Rawat, Sashank Reddi, and Sanjiv Kumar. 2019. Multilabel reductions: what is my loss optimising?. In Advances in Neural Information Processing Systems, H. Wallach, H. Larochelle, A. Beygelzimer, F. d'Alché-Buc, E. Fox, and R. Garnett (Eds.), Vol. 32. Curran Associates, Inc. https://proceedings.neurips.cc/paper\_files/paper/2019/file/ da647c549dde572c2c5edc4f5bef039c-Paper.pdf
- [27] Anshul Mittal, Kunal Dahiya, Sheshansh Agrawal, Deepak Saini, Sumeet Agarwal, Purushottam Kar, and Manik Varma. 2021. DECAF: Deep Extreme Classification with Label Features. In Proceedings of the 14th ACM International Conference on Web Search and Data Mining (Virtual Event, Israel) (WSDM '21). Association for Computing Machinery, New York, NY, USA, 49–57. https://doi.org/10.1145/ 3437963.3441807
- [28] Anshul Mittal, Noveen Sachdeva, Sheshansh Agrawal, Sumeet Agarwal, Purushottam Kar, and Manik Varma. 2021. ECLARE: Extreme Classification with Label Graph Correlations. In Proceedings of the Web Conference 2021 (Ljubljana, Slovenia) (WWW '21). Association for Computing Machinery, New York, NY, USA, 3721–3732. https://doi.org/10.1145/3442381.3449815
- [29] Tri Nguyen, Mir Rosenberg, Xia Song, Jianfeng Gao, Saurabh Tiwary, Rangan Majumder, and Li Deng. 2016. Ms marco: A human-generated machine reading comprehension dataset. (2016).
- [30] Ioannis Partalas, Aris Kosmopoulos, Nicolas Baskiotis, Thierry Artieres, George Paliouras, Eric Gaussier, Ion Androutsopoulos, Massih-Reza Amini, and Patrick Galinari. 2015. Lshtc: A benchmark for large-scale text classification. arXiv preprint arXiv:1503.08581 (2015).
- [31] Yashoteja Prabhu, Anil Kag, Shrutendra Harsola, Rahul Agrawal, and Manik Varma. 2018. Parabel: Partitioned Label Trees for Extreme Classification with Application to Dynamic Search Advertising. In Proceedings of the 2018 World Wide Web Conference (Lyon, France) (WWW '18). International World Wide Web Conferences Steering Committee, Republic and Canton of Geneva, CHE, 993–1002. https://doi.org/10.1145/3178876.3185998
- [32] Mohammadreza Qaraei, Erik Schultheis, Priyanshu Gupta, and Rohit Babbar. 2021. Convex Surrogates for Unbiased Loss Functions in Extreme Classification With Missing Labels. In Proceedings of the Web Conference 2021. 3711–3720.
- [33] Yingqi Qu, Yuchen Ding, Jing Liu, Kai Liu, Ruiyang Ren, Wayne Xin Zhao, Daxiang Dong, Hua Wu, and Haifeng Wang. 2021. RocketQA: An Optimized Training Approach to Dense Passage Retrieval for Open-Domain Question Answering. In Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies. Association for Computational Linguistics, Online, 5835–5847. https: //doi.org/10.18653/v1/2021.naacl-main.466
- [34] Ruiyang Ren, Yingqi Qu, Jing Liu, Wayne Xin Zhao, QiaoQiao She, Hua Wu, Haifeng Wang, and Ji-Rong Wen. 2021. RocketQAv2: A Joint Training Method for Dense Passage Retrieval and Passage Re-ranking. In Proceedings of the 2021 Conference on Empirical Methods in Natural Language Processing. Association for Computational Linguistics, Online and Punta Cana, Dominican Republic, 2825–2835. https://doi.org/10.18653/v1/2021.emnlp-main.224
- [35] Deepak Saini, Arnav Kumar Jain, Kushal Dave, Jian Jiao, Amit Singh, Ruofei Zhang, and Manik Varma. 2021. GalaXC: Graph neural networks with labelwise attention for extreme classification. In ACM International World Wide Web Conference. https://www.microsoft.com/en-us/research/publication/galaxc/
- [36] Erik Schultheis and Rohit Babbar. 2022. Speeding-up one-versus-all training for extreme classification via mean-separating initialization. *Machine Learning* 111, 11 (2022), 3953–3976.

- [37] Erik Schultheis, Marek Wydmuch, Rohit Babbar, and Krzysztof Dembczynski. 2022. On missing labels, long-tails and propensities in extreme multi-label classification. In Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining. 1547–1557.
- [38] Erik Schultheis, Marek Wydmuch, Wojciech Kotlowski, Rohit Babbar, and Krzysztof Dembczynski. 2024. Generalized test utilities for long-tail performance in extreme multi-label classification. Advances in Neural Information Processing Systems 36 (2024).
- [39] George Tsatsaronis, Georgios Balikas, Prodromos Malakasiotis, Ioannis Partalas, Matthias Zschunke, Michael R Alvers, Dirk Weissenborn, Anastasia Krithara, Sergios Petridis, Dimitris Polychronopoulos, et al. 2015. An overview of the BIOASQ large-scale biomedical semantic indexing and question answering competition. *BMC bioinformatics* 16, 1 (2015), 1–28.
- [40] M. Wydmuch, K. Jasinska, M. Kuznetsov, R. Busa-Fekete, and K. Dembczynski. 2018. A no-regret generalization of hierarchical softmax to extreme multi-label classification. In *NIPS*.
- [41] Lee Xiong, Chenyan Xiong, Ye Li, Kwok-Fung Tang, Jialin Liu, Paul N. Bennett, Junaid Ahmed, and Arnold Overwijk. 2021. Approximate Nearest Neighbor Negative Contrastive Learning for Dense Text Retrieval. In *International Conference* on Learning Representations. https://openreview.net/forum?id=zeFrfgyZln
- [42] H. Ye, Z. Chen, D.-H. Wang, and Davison B. D. 2020. Pretrained Generalized Autoregressive Model with Adaptive Probabilistic Label Clusters for Extreme Multi-label Text Classification. In *ICML*.
- [43] R. You, Z. Zhang, Z. Wang, S. Dai, H. Mamitsuka, and S. Zhu. 2019. Attentionxml: Label tree-based attention-aware deep model for high-performance extreme multi-label text classification. In *NeurIPS*.
- [44] Hang Zhang, Yeyun Gong, Yelong Shen, Jiancheng Lv, Nan Duan, and Weizhu Chen. 2021. Adversarial retriever-ranker for dense text retrieval. arXiv preprint arXiv:2110.03611 (2021).
- [45] Jiong Zhang, Wei-Cheng Chang, Hsiang-Fu Yu, and Inderjit S Dhillon. 2021. Fast Multi-Resolution Transformer Fine-tuning for Extreme Multi-label Text Classification. In Advances in Neural Information Processing Systems. https: //openreview.net/forum?id=gjBz22V93a

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Figure 4: Correlations between labels and their first-order neighbours, as found by the label co-occurrence on the LF-WikiTitles-500K dataset. The legend shows the label in question, the bar chart shows the degree of correlation with its neighbouring labels. Correlated labels often share tokens with each other and/or may be used in the same context.

### A ADDITIONAL VISUALIZATIONS

*Similarity between Labels and their Annotations.* Each label and their annotations, as discovered by the co-occurrence graph, are

semantically similar; in that they share tokens with one another and can be used in the same context. We show this pictorially by plotting the labels and their annotations in order of their co-occurrence in Figure 4.