Postfiltering Using Log-Magnitude Spectrum for Speech and Audio Coding

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Abstract

Advanced coding algorithms yield high quality signals with good coding efficiency within their target bit-rate ranges, but their performance suffer outside the target range. At lower bitrates, the degradation in performance is because the decoded signals are sparse, which gives a perceptually muffled and distorted characteristic to the signal. Standard codecs reduce such distortions by applying noise filling and post-filtering methods. In this paper, we propose a post-processing method based on modeling the inherent time-frequency correlation in the log-magnitude spectrum. The goal is to improve the perceptual SNR of the decoded signals and, to reduce the distortions caused by signal sparsity. Objective measures show an average improvement of 1.5 dB for input perceptual SNR in range 4 to 18 dB. The improvement is especially prominent in components which had been quantized to zero.

Index Terms: Quantization noise, Speech modelling, postfiltering, noise filling, Time-Frequency correlation

1. Introduction

Speech and audio codecs are integral parts of most audio processing applications and recently we have seen rapid development in coding standards, such as MPEG USAC [1, 2], and 3GPP EVS [3]. These standards have moved towards unifying audio and speech coding, enabling the coding of super wide band and full band speech signals as well as added support of voice over IP. The core coding algorithms within these codecs, ACELP and TCX, yield perceptually transparent quality at moderate to high bitrates within their target bitrate ranges. However, the performance degrades when the codecs operate outside this range. Specifically, for low-bitrate coding in the frequency-domain, the decline in performance is because fewer bits are at disposal for encoding, whereby areas with lower energy are quantized to zero. Such spectral holes in the decoded signal renders a perceptually distorted and muffled characteristic to the signal, which can be annoying for the listener.

To obtain satisfactory performance outside target bitrate ranges, standard codecs like CELP employ pre- and post-processing methods, which are largely based on heuristics. In particular, to reduce the distortion caused by quantization-noise at low bitrates, codecs implement methods either in the coding process or strictly as a post-filter at the decoder. Formant enhancement and bass post-filters are common methods [4] which modify the decoded signal based on the knowledge of how and where quantization noise perceptually distorts the signal. Formant enhancement shapes the codebook to intrinsically have less energy in areas prone to noise and is applied both at the encoder and decoder. In contrast, bass post-filter removes the noise like component between harmonic lines and is implemented only in the decoder.

Another commonly used method is noise filling, where pseudo-random noise is added to the signal [2], since accurate encoding of noise-like components is not essential for perception. In addition, the approach aids in reducing the perceptual effect of distortions caused by sparsity on the signal. The quality of noise-filling can be improved by parameterizing the noise-like signal, for example, by its gain, at the encoder and transmitting the gain to the decoder.

The advantage of post-filtering methods over the other methods is that they are only implemented in the decoder, whereby they do not require any modifications to the encoder-decoder structure, nor do they need any side information to be transmitted. However, most of these methods focus on solving the effect of the problem, rather than address the cause.

In this paper, we propose a post-processing method to improve signal quality at low bitrates, by modeling the inherent time-frequency correlation in speech magnitude spectrum and, investigating the potential of using this information to reduce quantization noise. The advantages of this approach are that it does not require the transmission of any side information and operates using solely the quantized signal as the observation and the speech models trained offline; Since it is applied at the decoder after the decoding process, it does not require any changes to the core structure of the codec; The approach addresses the signal distortions by estimating the information lost during the coding process using a source model. The novelties of this work lies in (i) incorporating the formant information in speech signals using log-magnitude modeling, (ii) representing the inherent contextual information in the spectral magnitude of speech in the log-domain as a multivariate Gaussian distribution (iii) finding the optimum, for the estimation of true speech, as the expected likelihood of a truncated Gaussian distribution.

2. Speech Magnitude Spectrum Models

Formants are the fundamental indicator of linguistic content in speech and are manifested by the spectral magnitude envelope of speech, therefore the magnitude spectrum is an important part of source modeling [5, 6]. Prior research has shown that frequency coefficients of speech are best represented by a Laplacian or Gamma distribution [7, 8, 9, 10]. Hence, the magnitude-spectrum of speech is an exponential distribution, as

![Figure 1: Context neighborhood of size C = 10. The previous estimated bins are chosen and ordered based on the distance from the current sample.](Image)
Our objective is to estimate the clean speech signal from the observation of the noisy decoded signal using the statistical priors. To this end, we formulate the problem as the maximum likelihood (ML) of the current sample given the observation and the previous estimates. Assume a sample $x$ has been quantized to a quantization level $Q \in [l, u]$. We can then express our optimization problem as:

$$\hat{x} = \arg \max_x P(X|X_c = \hat{x}_c) \quad \text{subject to,} \quad l \leq X \leq u,$$

where $\hat{x}$ is the estimate of the current sample, $l$ and $u$ are the lower and upper limits of the current quantization bin, respectively, and, $P(a_1|a_2)$ is the conditional probability of $a_2$, given $a_1$. $\hat{x}_c$ is the estimated context vector. Fig. 1 illustrates the construction of a context vector of size $C = 10$, wherein the numbers represent the order in which the frequency bins are incorporated. We obtain the quantization levels from the decoded signal and from our knowledge of the quantization method used in the codec, we can define the quantization limits; the lower and upper limits of a specific quantization level is defined midway between previous and subsequent levels, respectively.

To illustrate the performance of Eq. 1, we solved it using generic numerical methods. Fig. 4 illustrates the results through distributions of the true speech (a) and estimated speech (b), in bins quantized to zero. We scale the bins such that the varying $l$ and $u$ are fixed to 0,1, respectively, in order to analyze and compare the relative distribution of the estimates within a quantization bin. In (b) we observe a high data density around the estimated-speech and the true-speech distributions. Finally, to mitigate this problem, we define the speech estimate as the expected likelihood (EL) [15, 16], as follows:

$$\hat{x} = E[P(X|X_c = \hat{x}_c)] \quad \text{subject to,} \quad l \leq X \leq u$$

The resulting speech distribution using EL is demonstrated in Fig. 4 c, indicating a relatively better match between the estimated-speech and the true-speech distributions. Finally, to obtain an analytical solution, we incorporate the constraint condition into the modeling itself, whereby we model the distribution as a truncated Gaussian PDF [17]. In appendices A & B, we demonstrate how the solution can be obtained as a truncated Gaussian. Algorithm. 1 presents an overview of the estimation method.

4. Experiments and Results

Our objective is to evaluate the advantage of modeling the log-magnitude spectrum. Since envelope models are the main method for modeling the magnitude spectrum in conventional codecs, we evaluate the effect of statistical priors both in terms of the whole spectrum as well as only for the envelope. Therefore, besides evaluating the proposed method for the estimation...
Input pSNR (dB)
Output pSNR (dB)
Input C=1 C=4 C=8 C=10 C=14 C=20 C=40
(a) Input Vs Output pSNR (Spectrum)

Figure 5: Plots representing the improvement in SNR using the proposed method for different context sizes.

Algorithm 1 Estimation of signal from quantized observation

Require: Quantized signal \( Y \), prior-models \( C \)

function ESTIMATION(\( Y, C \))
  for frame = 1 : N do
    for b = 1 : Length(\( Y(\text{frame}) \)) do
      \( \mu_{up}, \sigma_{up} \leftarrow \text{UpdateStatistics}(C, X_{prev}) \)
      pdf \leftarrow \text{TruncateGaussian}(\mu_{up}, \sigma_{up}, l(b), u(b))
      \( X \leftarrow \text{Expectation}(pdf) \)
  for b = 1 : Length(\( Y(\text{frame}) \)) do
    \( \mu_{up}, \sigma_{up} \leftarrow \text{UpdateStatistics}(C, X_{prev}) \)
    pdf \leftarrow \text{TruncateGaussian}(\mu_{up}, \sigma_{up}, l(b), u(b))
  \end{algorithm}

4.2. Experimental setup

For training we use 250 speech samples from the training set of the TIMIT database [19]. The block diagram of the training process is presented in Fig. 3. For testing, 10 speech samples were randomly chosen from the test set of the database. The codec is based on the EVS codec [20] in TCX mode and we chose the codec parameters such that the perceptual SNR (pSNR) [20, 4] is in the range typical to codecs. Therefore, we simulated coding at 12 different bitrates between 9.6 to 128 kbps, which gives pSNR values in the approximate range of 4 and 18 dB. Note that the TCX mode of EVS does not incorporate post-filtering. For each test case, we apply the post-filter to the decoded signal with context sizes \( \{1, 4, 8, 10, 14, 20, 40\} \). The context vectors are obtained as per the description in Sec. 2 and illustration in Fig. 1. For tests using the magnitude spectrum, the pSNR of the post-processed signal is compared against the pSNR of the noisy quantized signal. For spectral envelope based tests, the signal-to-Noise Ratio (SNR) between the true and the estimated envelope is used as the quantitative measure.

4.3. Results and analysis

The average of the qualitative measures over the 10 speech samples are plotted in Fig. 5. Plots (a) and (b) represent the evaluation results using the magnitude spectrum and, plots (c) and (d) correspond to the spectral envelope tests. For both, the spectrum and the envelope, incorporation of contextual information shows a consistent improvement in the SNR. The degree of improvement is illustrated in plots (b) and (d). For magnitude spectrum, the improvement ranges between 1.5 and 2.2 dB over all the context at low input pSNR, and from 0.2 to 1.2 dB higher input pSNR. For spectral envelopes, the trend is similar; the improvement over context is between 1.25 to 2.75 dB at lower input pSNR, and from 0.5 to 2.25 at higher input SNR. At around 10dB input SNR, the improvement peaks for all context sizes.

For the magnitude spectrum, the improvement in quality between context size 1 and 4 is significantly large, approximately 0.5 dB over all input pSNRs. By increasing the context size we can further improve the pSNR, but the rate of improvement is relatively lower for sizes from 4 to 40. Also, the improvement is considerably lower at higher input pSNRs. We conclude that a context size around 10 samples is a good compromise between accuracy and complexity. However, the choice of context size can also depend on the target device for processing. For instance, if the device has computational resources at disposal, a high context size can be employed for maximum improvement.

Performance of the proposed method is further illustrated in Figs. 7-8, with an input pSNR of 8.2 dB. A prominent observation from all plots in Fig. 7 is that, particularly in bins...
quantized to zero the proposed method is able to estimate magnitude which is close to the true magnitude. Additionally from Fig. 7 (ii), the estimates seem to follow the spectral envelope, whereby we can conclude that Gaussian distributions pre-dominantly incorporate spectral envelope information and not so much of pitch information. Hence, additional modeling methods for the pitch will be addressed in future work.

The scatter plots in Fig. 8 represent the correlation between the true, estimated and quantized speech magnitude in zero-quantized bins for $C = 1$ and $C = 40$. These plots further demonstrate that context is useful in estimating speech in bins where no information exists. Thus this method can be beneficial in estimating spectral magnitudes in noise-filling algorithms. In the scatter plots, the quantized, true and estimated speech magnitude spectrum are represented by red, black and blue points, respectively; We observe that while the correlation is positive for both sizes, the correlation is significantly higher and more defined for $C = 40$.

### 5. Discussion and Conclusion

In this work, we investigated the use of contextual information inherent in speech for the reduction of quantization noise. We propose a post-processing method with focus on estimating speech samples at the decoder, from the quantized signal using statistical priors. Results indicate that including speech correlation not only improves the pSNR, but also provide spectral magnitude estimates for noise filling algorithms. While the focus of this paper was modeling the spectral magnitude, a joint magnitude-phase modeling method, based on current insights and the results from an accompanying paper [21], is the natural next step.

This work also begins to tread on spectral envelope restoration from highly quantized noisy envelopes by incorporating information for the context neighborhood. In future work we should explore the interaction between our method and quantization of conventional envelope parameterizations. Additionally, since this method has shown a capacity to restore information from areas where no information exists at all, it will be interesting to see the application of this method to packet-loss concealment.

![Sample plots depicting the true, quantized and estimated speech signal](image)

**Figure 7:** Sample plots depicting the true, quantized and the estimated speech signal (i) in a fixed frequency band over all time frames (ii) in a fixed time frame over all frequency bands.

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### A. Truncated Gaussian PDF

Let us define $f_1(a) = e^{-(a-\mu)^2/(2\sigma^2)}$ and $f_2(a) = \text{erf}(\frac{a-\mu}{\sigma \sqrt{2}})$, where $\mu, \sigma$ are the statistical parameters of the distribution and erf is the error function. Then, expectation of a univariate Gaussian random variable $X$ is computed as:

$$E[X]_{-\infty}^{\infty} = \frac{1}{\sqrt{2\pi}\sigma^2} \int_{-\infty}^{\infty} x f_1(x) dx, \quad (3)$$

Conventionally, when $X \in [-\infty, \infty]$, solving Eq. 3 results in $E(X) = \mu$. However, for a truncated Gaussian random variable, with $l < X < u$, the relation is

$$E(X|l < X < u) = \frac{\int_{l}^{u} x P(x) dx}{\int_{l}^{u} P(x) dx} = \int_{l}^{u} f_1(x) dx \int_{l}^{u} f_1(x) dx^{-1} \quad (4)$$

which yields the following equation to compute the expectation of a truncated univariate Gaussian random variable:

$$E(X|l < X < u) = \mu - \sigma \sqrt{\frac{2}{\pi}} \left[ \Phi\left( \frac{lu}{\sigma \sqrt{2}} \right) - \Phi\left( \frac{fu}{\sigma \sqrt{2}} \right) \right] \quad (5)$$

### B. Conditional Gaussian parameters

Let the context vector be defined as $x = [x_1, x_2]^T$, wherein $x_1 \in \mathbb{R}^{1 \times 1}$ represents the current bin under consideration, and $x_2 \in \mathbb{R}^{C \times 1}$ is the context. Thus, $x \in \mathbb{R}^{(C+1) \times 1}$, where $C$ is the context size. The statistical models are represented by the mean vector $\mu \in \mathbb{R}^{(C+1) \times 1}$, and the covariance matrix $\Sigma \in \mathbb{R}^{(C+1) \times (C+1)}$, such that $\mu = [\mu_1, \mu_2]^T$ with dimensions same as $x_1$ and $x_2$, and the covariance as

$$\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}. \quad (6)$$

$\Sigma_{11}$ are partitions of $\Sigma$ with dimensions $\Sigma_{11} \in \mathbb{R}^{1 \times 1}$, $\Sigma_{22} \in \mathbb{R}^{C \times C}$, $\Sigma_{12} \in \mathbb{R}^{1 \times C}$ and $\Sigma_{21} \in \mathbb{R}^{C \times 1}$. Thus, the updated statistics of the distribution of the current bin based on the estimated context is [22]:

$$\mu_{np} = \mu_1 + \Sigma_{12} \Sigma_{22}^{-1}(\hat{x} - \mu_2) \quad (7)$$

$$\sigma_{np} = \Sigma_{11} - \Sigma_{12} \Sigma_{22}^{-1} \Sigma_{21}. \quad (8)$$

![Scatter plots of the true, quantized and estimated speech in zero-quantized bins for (a) $C = 1$, (b) $C = 40$. The plots demonstrate the correlation between the estimated and true speech.](image)

**Figure 8:** Scatter plots of the true, quantized and estimated speech signal (i) in a fixed frequency band over all time frames (ii) in a fixed time frame over all frequency bands.
7. References


