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Tuning the S = 1/2 square-lattice antiferromagnet $Sr_2Cu(Te_{1-x}W_x)O_6$ from Néel order to quantum disorder to columnar order

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The spin-1/2 square-lattice Heisenberg model is predicted to have a quantum disordered ground state when magnetic frustration is maximized by competing nearest-neighbor J_1 and next-nearest-neighbor J_2 interactions $(J_2/J_1 \approx 0.5)$. The double perovskites Sr₂CuTeO₆ and Sr₂CuWO₆ are isostructural spin-1/2 square-lattice antiferromagnets with Néel (J_1 dominates) and columnar (J_2 dominates) magnetic order, respectively. Here we characterize the full isostructural solid-solution series Sr₂Cu(Te_{1-x}W_x)O₆ ($0 \leq x \leq 1$) tunable from Néel order to quantum disorder to columnar order. A spin-liquid-like ground state was previously observed for the x = 0.5 phase, but we show that the magnetic order is suppressed below 1.5 K in a much wider region of $x \approx 0.1$ –0.6. This coincides with significant *T*-linear terms in the low-temperature specific heat. However, density-functional theory calculations predict most of the materials are not in the highly frustrated $J_2/J_1 \approx 0.5$ region square-lattice Heisenberg model. Thus, a combination of both magnetic frustration and quenched disorder is the likely origin of the spin-liquid-like state in x = 0.5.

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I. INTRODUCTION

Square-lattice antiferromagnets (AFMs) can be described using the Heisenberg J_1 - J_2 model with two interactions: nearest neighbor J_1 (side of the square) and next-nearest neighbor J_2 (diagonal of the square). The phase diagram of the model is shown in Fig. 1(a). The classical ground states for the J_1 - J_2 model are ferromagnetic order, Néel AFM order, and columnar AFM order [1]. Dominating antiferromagnetic J_1 ($J_2/J_1 \ll 0.5$) leads to Néel order and dominating J_2 $(J_2/J_1 \gg 0.5)$ to columnar order. And erson [2] first proposed that by frustrating the Néel order in an S = 1/2 square-lattice AFM, i.e., by introducing an antiferromagnetic J_2 interaction, a quantum spin-liquid (QSL) state might emerge. Quantum spin liquids are highly entangled quantum states with exotic excitations, in which spins remain dynamic and do not order even at absolute zero [3-5]. The QSL state on the square lattice is predicted to occur in a narrow parameter range between $J_2/J_1 \approx 0.4$ -0.6, where the magnetic frustration due to competing antiferromagnetic J_1 and J_2 interactions is maximized [6–8]. A limited number of model compounds that realize the S = 1/2 square-lattice Heisenberg model are known [9–19], but none of them are in the spin-liquid region of the phase diagram [Fig. 1(a)].

Recently, *B*-site ordered $A_2B'B''O_6$ double perovskites Sr₂CuTeO₆ and Sr₂CuWO₆ were shown to be near-ideal realizations of the S = 1/2 square-lattice J_1 - J_2 model with

highly two-dimensional magnetic interactions [20-23]. These two compounds are unique among the known J_1 - J_2 model compounds, because they are isostructural yet on the opposite sides of the phase diagram: the magnetic ordering is Néel type in Sr₂CuTeO₆ $(J_2/J_1 = 0.03)$ and columnar in Sr₂CuWO₆ $(J_2/J_1 = 7.92)$ [22–25]. The crystal structure is tetragonal with a rocksalt ordering of B' (Cu²⁺) and B'' (Te⁶⁺/W⁶⁺) sites [26-28], see Fig. 1(b). The copper cations form a square in the *ab* plane, and the diamagnetic Te^{6+}/W^{6+} cations are located in the middle of the square, as shown in Fig. 1(c). The diamagnetic B'' cation controls the extended superexchange pathways between the copper cations: W^{6+} 5d⁰ hybridizes strongly with O 2p and allows 180° Cu-O-W-O-Cu (J_2) superexchange, which is not possible with the $4d^{10}$ Te⁶⁺ cations which favor J_1 [22,29,30]. As a result, the two compounds are in different regions of the J_1 - J_2 phase diagram despite being isostructural.

The solid solution $Sr_2Cu(Te_{1-x}W_x)O_6$ is a unique system for studying frustrated square-lattice antiferromagnetism as it can be tuned from Néel (x = 0) to columnar order (x = 1) by varying the composition. Additionally, the similar size of Te^{6+} and W^{6+} cations means that little change is expected in the crystal structure [31]. Very recently, we showed that $Sr_2Cu(Te_{0.5}W_{0.5})O_6$ (x = 0.5) has a spin-liquid-like ground state [32], which exhibits many of the properties of the QSL state: magnetism was found to be entirely dynamic down to 19 mK and a plateau was observed in the low-temperature muon spin-relaxation rate. Moreover, the magnetic specific heat showed a strong *T*-linear relationship at low temperatures indicating gapless excitations [32].

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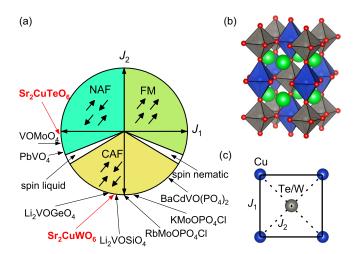


FIG. 1. (a) Phase diagram of the spin-1/2 square-lattice Heisenberg model as a function of J_2/J_1 , where J_1 is the nearest neighbor and J_2 is the next-nearest-neighbor interaction [13,18,51]. Known compounds realizing the model are placed at their respective positions. The classical ground states of the model are ferromagnetic order, Néel antiferromagnetic (NAF) order, and columnar antiferromagnetic (CAF) order. A quantum spin-liquid state has been predicted for $J_2/J_1 \approx 0.4$ –0.6 at the NAF-CAF boundary. Isostructural double perovskites Sr₂CuTeO₆ and Sr₂CuWO₆ are in the NAF and CAF regions, respectively. (b) The *B*-site ordered double-perovskite structure of Sr₂CuTeO₆ and Sr₂CuWO₆ [24,25]. (c) The square of S = 1/2 Cu²⁺ cations in the *ab* plane of Sr₂CuTeO₆ and Sr₂CuWO₆ with the view down the *c* axis. The Te/W cation in the center of the Cu²⁺ square determines whether J_1 or J_2 interaction dominates.

The origin of the spin-liquid-like ground state in $Sr_2Cu(Te_{0.5}W_{0.5})O_6$ (x = 0.5) is not known. The QSL state expected from the J_1 - J_2 model requires a good match of the magnetic interactions J_1 and J_2 [6–8]. Thus, it is expected to be stable only in a narrow composition range in $Sr_2Cu(Te_{1-x}W_x)O_6$. To illustrate this point we can, as a first approximation, interpolate the exchange interactions in the $Sr_2Cu(Te_{1-x}W_x)O_6$ solid solution from the end members Sr_2CuTeO_6 ($J_1 = -7.18 \text{ meV}$, $J_2 = -0.21 \text{ meV}$) and Sr_2CuWO_6 ($J_1 = -1.2 \text{ meV}$, $J_2 = -9.5 \text{ meV}$) assuming a linear dependence on x [22,23]. In such a case, the highly frustrated region with $J_2/J_1 \approx 0.4-0.6$ would correspond to a rather narrow composition range of $x \approx 0.23$ –0.33. However, the $Sr_2Cu(Te_{1-x}W_x)O_6$ solid-solution system has significant quenched disorder in the magnetic interactions that is not included in the J_1 - J_2 model. This is due to Te⁶⁺/W⁶⁺ disorder on the B'' site in the middle of each square of Cu^{2+} ions [Fig. 1(c)], which affects whether J_1 or J_2 is dominant locally. This quenched disorder could help to stabilize a QSL [33-36] or a QSL-like random-singlet state [37–41].

Here we investigate the properties of the full solid-solution series $Sr_2Cu(Te_{1-x}W_x)O_6$ ($0 \le x \le 1$). Our magnetic susceptibility measurements suggest a maximum in frustration near $x \approx 0.4$ –0.5, whereas low-temperature specific heat measurements show a *T*-linear term typical of QSLs or spin glasses in a wide composition range of $x \approx 0.1$ –0.7. Similarly, muon spin relaxation and rotation measurements reveal that magnetic order is significantly suppressed not only in x = 0.5 but for $x \approx 0.1$ –0.6. Whether the QSL-like state of x = 0.5 occurs for this entire composition range or another ground state such as spin glass forms is not known at this time. Densityfunctional theory (DFT) calculations suggest a crossover from Néel ($J_2/J_1 < 0.5$) to columnar ($J_2/J_1 > 0.5$) region occurs already at $x \approx 0.2$ placing most samples in the columnar region. Thus, magnetic frustration from competing interactions on its own does not explain the suppression of magnetic order in this system: a combination of both magnetic frustration and quenched disorder is required.

II. EXPERIMENTAL DETAILS

The solid-solution series $\text{Sr}_2\text{Cu}(\text{Te}_{1-x}W_x)O_6$ ($0 \le x \le 1$) was synthesized by conventional solid-state synthesis. Stoichiometric amounts of SrCO₃, CuO, TeO₂, and WO₃ were ground in an agate mortar with ethanol. The precursor mixture was calcined at 900 °C for 12 h, pelletized, and repeatedly fired at 1050 °C in air for a total of 72 h with intermittent grindings. The synthesis temperature was of special importance on the Te-rich side (x < 0.5), as too high a temperature was found to result in the formation of an unknown impurity phase with main reflections at 2θ (Cu $K_{\alpha 1}$) 30.56° and 30.76°. At the same time, the synthesis temperature needed to be high enough to form a well-crystallized double-perovskite phase. We found no positive effect from using excess TeO₂ in contrast to an earlier report on Sr₂CuTeO₆ [27].

Phase purity and crystal structure of the samples were analyzed by powder x-ray diffraction (Panalytical X'Pert Pro MPD, Cu $K_{\alpha 1}$ radiation). Rietveld refinements were carried out using FULLPROF software [42]. Line-broadening analysis was performed as described in Ref. [43]. Instrumental broadening was determined with a LaB₆ standard (NIST SRM 660b). The crystal structures were visualized using VESTA 3 [44].

Magnetic properties were measured with a Quantum Design MPMS XL magnetometer. The samples were measured in gelatin capsules placed inside plastic straws. Magnetic susceptibility was measured from 5 to 300 K in an applied field of 1 T. Specific heat was measured with a Quantum Design PPMS instrument. The data were collected between 2 and 150 K using a thermal relaxation method.

Muon spin rotation and relaxation (μ SR) for polycrystalline powders with compositions x = 0.1, 0.2, 0.3, 0.4, 0.6, 0.7, 0.8, and 0.9 were measured at the Dolly and GPS installations of the Swiss Muon Source at Paul Scherrer Institut, Switzerland, using 100% spin-polarized positive muons. Sample temperatures were varied down to 1.5 K. The x = 0.5 sample was previously measured down to 19 mK at the Low Temperature Facility (LTF) installation [32]. Measurements were performed in zero-field (ZF) and weak transverse-field (wTF) mode (5 mT applied perpendicular to initial muon spin direction).

Density-functional theory calculations were used to evaluate the relative stabilities of different magnetic orderings in the full composition range $0 \le x \le 1$ in steps of 1/8 in *x*. We have previously shown that our computational approach works well for Sr₂CuWO₆ and gives a good estimate of the exchange-coupling constants [23]. The calculations were carried out with the full-potential linearized augmented planewave ELK code [45] using the generalized gradient approximation functionals by Perdew, Burke, and Ernzerhof [46]. Electron correlation effects of the 3*d* copper orbitals were included with a DFT+*U* approach using the fully localized limit double-counting correction [47]. We used a Hubbard *U* value of U = 8 eV typical of copper [47–49] (with Hund's rule coupling J = 0.9 eV corresponding to $U_{\text{eff}} = 7.1 \text{ eV}$), which was also the optimal value for Sr₂CuWO₆ [23]. The calculations were carried out using $2 \times 2 \times 1$ supercells with ferromagnetic, Néel, or columnar antiferromagnetic order [23]. The experimental crystal structures were used without lattice relaxation. Only one supercell was used for each composition with an equal number of Te and W nearest neighbors for x =0.5 (Supplemental Material [50]). We used a *k*-point grid of $4 \times$ 4×6 and a plane-wave cutoff of $|G + k|_{\text{max}} = 8/R_{\text{MT}}$ a.u.⁻¹, where R_{MT} is the average muffin-tin radii.

III. RESULTS

A. Crystal structure

We were able to synthesize the full solid-solution series $Sr_2Cu(Te_{1-x}W_x)O_6$ ($0 \le x \le 1$) using a conventional solidstate reaction method. Powder x-ray diffraction revealed the samples to be of high quality with trace quantities (less than 1%) of a SrWO₄ impurity. Rietveld refinement revealed that all the samples crystallize in the B-site ordered double-perovskite structure of the parent phases (Supplemental Material [50]). The space group is I4/m for all samples. Since Te⁶⁺ and W⁶⁺ cations have very similar sizes [31], we see only small changes in the lattice parameters. The main changes are seen in the c parameter, which decreases with increasing x. However, small changes are also observed in the *a* parameter: it stays relatively constant below x = 0.5 and then starts to decrease very slightly with increasing x. The unit-cell volume changes linearly and follows Vegard's law, which shows that we have prepared a true solid solution. The changes in atomic positions are minor. The B' (Cu²⁺) and B'' (Te⁶⁺/W⁶⁺) cations appear fully ordered, but there is no sign of Te⁶⁺ and W⁶⁺ ordering on the B" site consistent with our previous paper on x = 0.5 [32]. The structural disorder on the B'' cation site, which determines whether J_1 or J_2 dominates, inevitably leads to some quenched disorder in the magnetic interactions between the Cu^{2+} sites.

B. Magnetic properties

Magnetic susceptibility in all samples features a broad maximum [Fig. 2(a)]. While the end members Sr_2CuWO_6 and Sr₂CuTeO₆ order antiferromagnetically, the Néel temperatures cannot be determined from the susceptibility as no cusp is observed [21,24]. The broad maximum is expected behavior for a J_1 - J_2 model square-lattice antiferromagnet. It can be characterized by its position T_{max} and height χ_{max} . Theoretical studies on magnetic susceptibility in the J_1 - J_2 model as a function of J_2/J_1 indicate that T_{max} should have a minimum at $J_2/J_1 = 0.5$ and a χ_{max} should have a maximum at the same J_2/J_1 ratio [51,52]. We see a similar effect in $Sr_2Cu(Te_{1-x}W_x)O_6$ [Fig. 2(b)]: T_{max} has a minimum at $x \approx$ 0.4–0.6 whereas χ_{max} has a maximum at $x \approx 0.4$, see Table I. This suggests that the magnetic frustration is at its highest near $x \approx 0.4-0.5$. As we have previously shown, x = 0.5 has a spinliquid-like ground state [32]. The behaviors of T_{max} and χ_{max} in the $Sr_2Cu(Te_{1-x}W_x)O_6$ series are clearly different from the

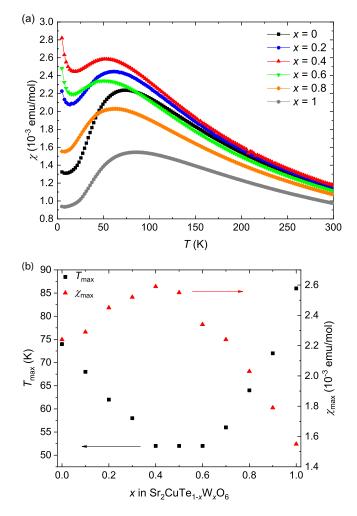


FIG. 2. (a) Magnetic susceptibility of selected samples as a function of temperature. Zero-field cooled and field-cooled data overlap and only the former is shown. (b) The position T_{max} and height χ_{max} of the broad maximum in magnetic susceptibility as a function of x in Sr₂Cu(Te_{1-x}W_x)O₆.

analogous molybdenum-based series $Sr_2Cu(Mo_{1-x}W_x)O_6$, where both depend linearly on composition [53]. This difference is expected, since Sr_2CuTeO_6 has Néel order [22,24] but both Sr_2CuWO_6 and Sr_2CuMoO_6 have columnar order [21,23,25], resulting in little magnetic frustration in $Sr_2Cu(Mo_{1-x}W_x)O_6$. Additionally, low-temperature Curie tails are observed for the samples x = 0.1-0.7.

In order to evaluate the overall strength of magnetic interactions in the materials, the Curie-Weiss temperatures Θ_{CW} were obtained by fitting the magnetic susceptibilities to the Curie-Weiss law $\chi = C/(T \cdot \Theta_{CW})$. The data were fitted in the temperature range 250–300 K. As shown in Table I, the Curie-Weiss temperatures Θ_{CW} for all samples are negative, indicating antiferromagnetic interactions. The overall strengths of magnetic interactions in the Te-rich side (x < 0.5) are very similar to each other but slightly weaker than in Sr₂CuTeO₆ as indicated by the lower $\Theta_{CW} \approx -60$ K. In the W-rich side the interactions become stronger with increasing x with the strongest AFM interactions in Sr₂CuWO₆ ($\Theta_{CW} = -165$ K). This trend corresponds to the minor changes observed in the

TABLE I. Magnetic and thermodynamic properties of $Sr_2Cu(Te_{1-x}W_x)O_6$.	
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x	0 ^{a,b}	0.1	0.2	0.3	0.4	0.5 ^a	0.6	0.7	0.8	0.9	1 ^{a,c}
$\mu_{ m eff}(\mu_{ m B})$	1.87	1.8	1.84	1.82	1.85	1.87	1.84	1.88	1.87	1.9	1.9
$\Theta_{\rm CW}({\rm K})$	-80	-64	-66	-62	-63	-71	-80	-96	-109	-138	-165
$T_{\rm max}$ (K)	74	68	62	58	52	52	52	56	64	72	86
$\chi_{\rm max}$ (10 ⁻³ emu/mol)	2.24	2.29	2.45	2.52	2.59	2.55	2.34	2.24	2.03	1.79	1.55
γ (mJ/mol K ²)	2.2	31.7	41.4	51.1	54.0	54.2	46.9	31.6	13.4	3.5	0.7
$\theta_{\rm D}({\rm K})$	381	409	390	436	411	395	396	357	343	353	361
$T_{\rm N}({\rm K})$	29	<1.5	<1.8	<1.6	<1.8	< 0.019	<1.8	7	11	15	24
$f = \Theta_{\rm CW} /T_{\rm N}$	2.8	>42	>36	>34	>35	>3700	>44	13.7	9.9	9.2	6.9

^aReference [32].

^bReference [24].

^cReference [21].

lattice parameter *a*, which is directly related to the $Cu^{2+}-Cu^{2+}$ distance in the *ab* plane. The effective paramagnetic moments obtained from the fits were similar for all samples and typical for Cu^{2+} compounds.

C. Specific heat

Specific heat of selected samples is shown in Fig. 3(a). No λ anomalies expected for long-range magnetic ordering at $T_{\rm N}$ are observed in any of the samples. The main differences between the samples are in the low-temperature specific heat. In order to evaluate the temperature dependence we plot the reduced low-temperature specific heat as a function of T^2 [Fig. 3(b)]. A strong T-linear γ term in specific heat is expected for a QSL. This T-linear term is related to excitations of highly entangled spins. For x = 0, 0.9, and 1 the reduced specific heat approaches zero with decreasing temperature. This lack of a T-linear term is expected behavior in long-range ordered antiferromagnetic insulators. For the other samples (x = 0.1-0.8) we observe behavior indicating a *T*-linear term, but at very low temperatures some differences are observed. In x = 0.7 and 0.8 the reduced specific heat has an additional small downturn at very low temperatures, suggesting that the T-linear γ term could be significantly smaller or even zero in these samples. In the x = 0.1-0.6 samples the reduced specific

heat either remains linear or has a slight upturn at very low temperatures.

The specific heat data below 10 K were fitted using the function $C_p = \gamma T + \beta_D T^3$, where C_p is the specific heat, γ is the electronic *T*-linear term, and β_D is the phononic term. We previously found very small γ terms for Sr₂CuTeO₆ and Sr₂CuWO₆, but a significant one for x = 0.5, which is typical for gapless spin-liquid-like states [54] and spin glasses [55]. For the full series we find a significant γ term at a very wide composition range of x = 0.1-0.7 [Fig. 3(c)]. This result suggests that the spin-liquid-like state could be present in a wide composition range, although a spin-glass ground state cannot be ruled out for compositions other than x = 0.5. The largest electronic contribution occurs at x = 0.5 in line with the magnetic susceptibility results.

D. Muon spin rotation and relaxation

ZF μ SR on Sr₂CuWO₆ (x = 1) has been reported to exhibit spontaneous rotation signals revealing long-range magnetic order below $T_N = 24$ K with a single rotation frequency following a typical temperature dependency curve [21]. Our ZF spectra for x = 0.9, 0.8, and 0.7 are presented in Figs. 4(a)– 4(c), where we plot the time-dependent polarization $G_z(t)$ of the muon spins measured via the asymmetry of decay positron count rates $A(t)/A(0) = G_z(t)$ after muon implantation at

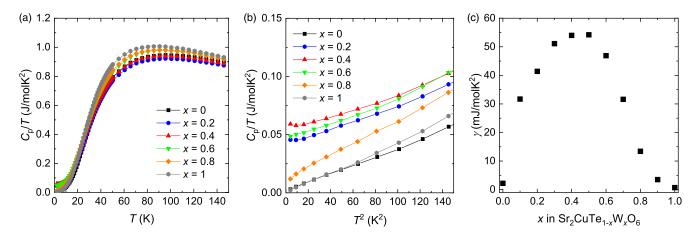


FIG. 3. (a) Reduced specific heat of selected samples as a function of temperature. (b) Low-temperature $C_p/T-T^2$ plot showing the *T*-linear relationship of most samples as indicated by a non-zero *y*-intercept. (c) *T*-linear term γ of specific heat as a function of *x* in Sr₂Cu(Te_{1-x}W_x)O₆.

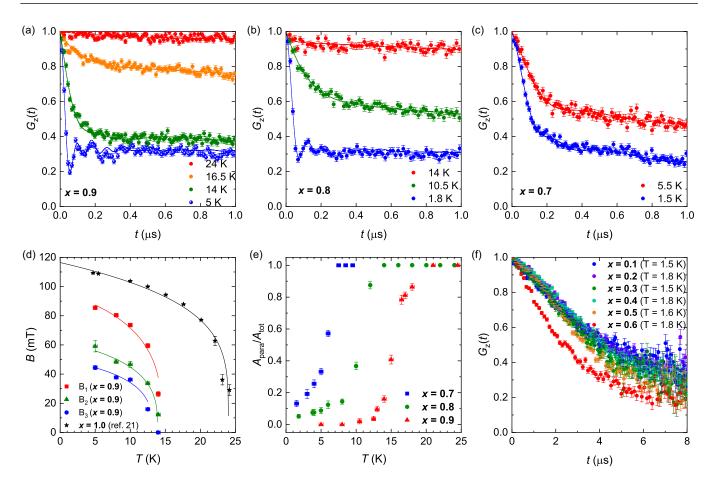


FIG. 4. Zero-field spectra of $Sr_2Cu(Te_{1-x}W_x)O_6$ with (a) x = 0.9 and (b) x = 0.8 showing spontaneous rotation signals in the magnetically ordered state. (c) Zero-field spectra of x = 0.7 at 5.5 and 1.5 K revealing only weak rotation signals and considerable dynamic damping. (d) Comparison of the temperature-dependent local fields B_i for x = 0.9 and x = 1 (data from Ref. [21]). Drawn lines are interpolations using a standard approximation as described in the main text. (e) Temperature dependence of ratio between paramagnetic and total asymmetries measured in a weak transverse field of 5 mT for x = 0.7, 0.8, 0.9. (f) Zero-field spectra for x = 0.1, 0.2, 0.3, 0.4, 0.5, 0.6 at 1.5–1.8 K showing no indication of magnetic ordering or static magnetism.

t = 0. Similar to x = 1, these spectra also show spontaneous rotations indicative of long-range order. However, these are strongly damped and with the onsets at clearly lower temperatures, around 15 and 11 for x = 0.9 and 0.8, respectively. For x = 0.7 the oscillations are less clearly visible, and the onset of magnetic order around 7 K can better be traced from wTF experiments, as will be described below. In contrast to x = 1 where only a single rotation signal was sufficient to yield good fits to the data, we need three signals for x = 0.9, 0.8, and 0.7 with different temperature-independent asymmetries A_i , temperature-dependent frequencies f_i , and transverse and longitudinal damping factors λ_{ti} and λ_{li} (i = 1, 2, 3). While usually rotation signals present cosine shape, we had to use zeroth-order Bessel functions J_0 for the best fits.

The total asymmetry is thus given by

$$A_{\text{tot}} = \sum_{i} A_{i} \cdot G_{zi} \cdot G_{\text{KT}i}, \qquad (1)$$

where

$$G_{zi} = 2/3 \exp(-\lambda_{\rm ti} t) J_{\rm o}(2\pi f_{\rm i} t) + 1/3 \exp(-\lambda_{\rm li} t)$$
 (2)

represents the rotations and dampings caused by magnetic fields of electronic origin. While the damping λ_{ti} of the oscillating signals is mainly caused by inhomogeneous static fields, the damping λ_{li} of 1/3 of asymmetry (second term) is caused by dynamic spin relaxation. The local magnetic fields B_i acting at the muon sites are related to the rotation frequencies f_i via

$$B_i = (2\pi/\gamma_\mu) \cdot f_i, \tag{3}$$

where $\gamma_{\mu}/2\pi = 135.5 \text{ MHz/T}$ is the muon gyromagnetic ratio. G_{KTi} is a so-called static Kubo-Toyabe function representing the depolarization due to a distribution of static nuclear dipolar fields:

$$G_{KTi} = (2/3)(1 - \sigma^2 t^2) \exp\left(-\frac{\sigma^2 t^2}{2}\right) + 1/3,$$
 (4)

where σ is the width of a Gaussian distribution of static fields. For x = 0.9, 0.8, and 0.7 we use $\sigma = 0.07, 0.06$, and 0.04 μs^{-1} , respectively, as estimated from damping functions obtained at high temperature where damping from electronic origin is negligible.

The observation of Bessel-shaped rotation signals is typical for a wide distribution of frequencies and is often observed in materials with incommensurately modulated spin structures [56,57]. The derived internal fields B_i are corresponding to the maximum cutoff frequencies f_i of the frequency distribution. In our present case, we use Bessel-shaped rotation signals simply as a heuristic approximation to a complex distribution. A more detailed description of analysis and discussion will be given elsewhere. For the present considerations, we restrict ourselves to a qualitative discussion of the μ SR data. In Fig. 4(d) we compare the temperature-dependent local fields B_i obtained for x = 0.9 with those of x = 1 from Ref. [21]. It is clear that the ordering temperature and local fields are reduced for x = 0.9 compared to x = 1. This is further seen in the local fields derived for x = 0.8 and 0.7 shown in Supplemental Material [50]. For a rough estimate of the ordering temperatures $T_{\rm N}$ we have extrapolated the $B_i(T)$ using the relation

$$B_i(T) = B_0 \left[1 - \left(\frac{T}{T_N}\right)^{\alpha} \right]^{\beta} , \qquad (5)$$

with $\alpha = 1.33$, and $\beta = 0.5$ for x = 0.7 and 0.8, and $\beta = 0.3$ for x = 0.9. Especially for x = 0.7 and 0.8 the extrapolations give varying values for the different B_i at one concentration indicating a range of ordering temperatures. For the schematic phase diagram in the Discussion and Table I we use the T_N values derived from the signals A_1 that are best resolved and strongest, yielding $T_N = 7$, 11, and 15 K for x = 0.7, 0.8, and 0.9, respectively.

While the transverse damping for x = 0.8 and 0.9 is strong below the magnetic ordering temperature due to static field distributions, the longitudinal damping affecting only the 1/3 "tail" is nearly vanishing as expected for static magnetic order. The behavior of the x = 0.7 sample is different: from the spectrum in Fig. 4(c) we can see that $G_z(t)$ is clearly decreasing below 1/3 at long times (measured up to 9 μ s, not shown in the figure), i.e., there is considerable longitudinal damping due to fluctuating local fields. We interpret this as the partial presence of dynamic short-range order.

Further support for the suppression of magnetic order can be traced from the wTF experiments. In the paramagnetic regime the applied magnetic field leads to rotation signals with an asymmetry that corresponds to $A_{\text{para}} = A_{\text{tot}}$. When entering the magnetically ordered regime the randomly acting local fields in polycrystalline material will be much stronger than the weak applied field and lead to very strong damping of the oscillating signal from the applied field. This results in a reduction of the oscillating asymmetry A_{para} . By following the ratio $A_{\text{para}}(T)/A_{\text{tot}}$ we can trace the vanishing of the paramagnetic volume fraction upon lowering temperature. From Fig. 4(e) we can see that the transitions for x = 0.9, 0.8, and 0.7 are not sharp. The suppression of A_{para} for x = 0.9 and 0.8 occurs close to, yet lower than those temperatures where spontaneous rotations could be resolved, which indicates inhomogeneous order with contributions from short-range order. For x = 0.7about 12% of volume stays paramagnetic even at 1.5 K, consistent with our previous observation of strong longitudinal relaxation.

For all other concentrations x = 0.1-0.6 we could not trace a reduction of asymmetry under wTF down to 1.5 K (for x = 0.5 down to 19 mK as reported in Ref. [32]).

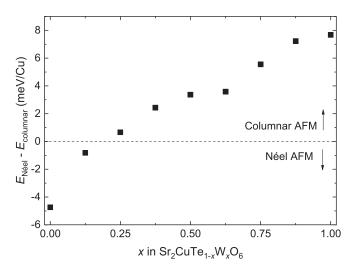


FIG. 5. Energy difference between Néel and columnar antiferromagnetic order as a function of composition in $Sr_2Cu(Te_{1-x}W_x)O_6$ calculated using GGA+U.

ZF spectra [Fig. 4(f)] show no indications of spontaneous muon spin rotation and longitudinal damping stays finite, confirming a paramagnetic state down to the lowest temperatures measured for these compositions x. All ZF spectra reveal nearly identical depolarization except for the x = 0.6 sample, which has a clearly faster decay of asymmetry. Depolarization from nuclear dipolar fields is expected to be similar for all compositions x, therefore the reason has to lie in an additional dynamic contribution to relaxation. Whether this is caused by a close-lying critical point or the development of a small order parameter with an eventual spin-glass-like depolarization needs further experimental investigation.

E. DFT calculations

One of the main questions in understanding the origin of the spin-liquid-like state is the position of the materials in the J_1 - J_2 phase diagram, i.e., whether they are in the Néel, columnar, or highly frustrated region. We utilized *ab initio* density-functional theory calculations to evaluate the relative stability of Néel and columnar orderings in Sr₂Cu(Te_{1-x}W_x)O₆. This is an extension of our previous DFT work on Sr₂CuWO₆ [23]. It should be noted that the structural disorder on the Te/W *B*["] site is not included in the DFT calculations as they require a periodic system.

The Néel and columnar-type orders are more stable than the ferromagnetic order for all compositions, see Supplemental Material [50]. This shows that both J_1 and J_2 are antiferromagnetic, and that there is magnetic frustration. In Fig. 5 we show the relative stability of Néel order compared to columnar order as a function of x in Sr₂Cu(Te_{1-x}W_x)O₆. As expected, at x = 0 Néel order is clearly favored and at x = 1 columnar order is clearly favored. Notably, very little W⁶⁺ is needed to destabilize Néel order in Sr₂Cu(Te_{1-x}W_x)O₆: the crossover from Néel to columnar order occurs already at $x \approx 0.2$. A comparison of energies to a ferromagnetic state reveals that W⁶⁺ destabilizes Néel order more strongly than it stabilizes columnar order, suggesting that the average J_1 is strongly reduced by W⁶⁺ in addition to a weaker increase in average J_2 .

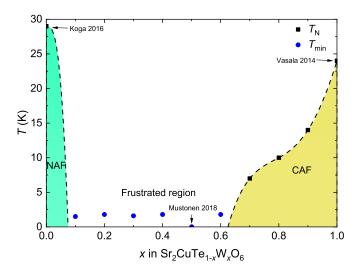


FIG. 6. Schematic phase diagram of $Sr_2Cu(Te_{1-x}W_x)O_6$. The black squares represent measured Néel temperatures and the blue circles represent the lowest temperature measured for samples that remain entirely dynamic and do not order.

At x = 0.5, where we previously established a spin-liquid-like ground state, columnar order is favored, indicating a dominant antiferromagnetic J_2 interaction ($J_2/J_1 > 0.5$). Thus, our calculations suggest that the origin of the spin-liquid-like state is not solely in the magnetic frustration of competing antiferromagnetic J_1 and J_2 interactions on the square lattice. In contrast to x = 0, the columnar order of x = 1 is quite stable toward Te⁶⁺ substitution. Columnar order is expected to be very stable at least down to x = 0.75 in agreement with the μ SR results.

Partial density of states were also investigated for x = 0, 0.5, and 1, see Supplemental Material [50]. The W⁶⁺ 5d⁰ hybridization with O 2p was observed in x = 1 similar to previous DFT studies on W⁶⁺/Te⁶⁺ compounds [29,30]. This explains the strong 180° superexchange (J_2) via Cu-O-W-O-Cu favoring columnar order in the W-rich compounds. We also observe modest Te 5p-O2p hybridization in x = 0, which is in agreement with a previous DFT study on Sr₂CuTeO₆ [29]. In x = 0.5 we see both effects with significant W 5d⁰-O 2p hybridization and modest Te 5p - O 2p hybridization.

IV. DISCUSSION

A schematic phase diagram for $Sr_2Cu(Te_{1-x}W_x)O_6$ based on the μ SR results and previous literature [24,25,32] is presented in Fig. 6. Néel order is significantly suppressed already at x = 0.1 in accordance with the DFT results. On the W-rich side, T_N is gradually suppressed from 24 K at x = 1 to 7 K at x = 0.7. This is consistent with the DFT results, which predict that columnar antiferromagnetic order is very stable when x = 0.75-1. Of most importance is the wide frustrated region x = 0.1-0.6, where no magnetic order is observed at the lowest temperatures measured. These samples also have significant T-linear terms in the low-temperature specific heat as expected in a gapless QSL or a spin glass. We previously showed that x = 0.5 has a spin-liquid-like ground state with dynamic magnetism down to 19 mK. Our μ SR evidence for a QSL-like state in the wider x = 0.1-0.6 region is not conclusive, as we could only measure down to 1.5–1.8 K. Consequently, we are not able to show a plateau in the muon spin-relaxation rate expected in a QSL for these compositions and a spin-glass ground state cannot be ruled out. The suppression of magnetic order in such a wide composition range does, however, indicate that the origin of the spin-liquid-like state is linked to both magnetic frustration and quenched disorder in the material.

The role of quenched disorder, inevitably present in a real material, is a nontrivial question in spin-liquid physics [4]. Furukawa *et al.* [33] were able to induce a gapless spin-liquid state in an organic triangular-lattice Cu^{2+} salt by introducing disorder. Irradiation with x rays created defects and disorder that drove the material from a magnetically ordered state into a spin liquid [33]. Disorder-induced spin-liquid states were also observed in non-Kramers ion pyrochlores $Pr_2Zr_2O_7$ and $Tb_2Hf_2O_7$ [34–36]. In comparison to these three compounds, the $Sr_2Cu(Te_{1-x}W_x)O_6$ series has even more quenched disorder due to being a solid solution.

Theoretical calculations by Kawamura and coworkers [37–40] predict the formation of disorder-induced QSL-like random singlet state on S = 1/2 triangular, kagome, and honeycomb lattices. In the random singlet state, or valence bond glass, the quenched randomness in exchange interactions induces the formation of local spin singlets of varying strength with gapless excitations. In the honeycomb J_1 - J_2 model, in which J_1 and J_2 compete similar to the square model, the random singlet state was stabilized in a wide parameter range in the presence of sufficient disorder [40]. Very recently, these theoretical calculations were extended to the square lattice [58]. For $J_2/J_1 = 0.5$, the ground state changes from a gapped spin liquid to a gapless random singlet state as quenched disorder is increased. The random singlet state is stabilized for a wide J_2/J_1 range for significant disorder. For $J_2/J_1 = 0.7$ in the columnar region, a spin-glass state related to columnar magnetic order is stabilized for strong disorder. This stripe glass might be the ground state of x = 0.6. The experimental evidence previously presented for x = 0.5 is consistent with a random singlet state. The model is also consistent with a random singlet ground state for x = 0.1-0.4, as the spin glass is only stabilized close to columnar magnetic order in the phase diagram.

Other theoretical investigations of the effect of disorder on the square lattice are also known. In the unfrustrated case with only an antiferromagnetic J_1 interaction, Néel order is expected to be robust against bond disorder [38,59]. Richter [60] studied the effect of ferromagnetic inhomogeneities in the frustrated J_1 - J_2 model. These were found to widen the quantum disordered region from $J_2/J_1 = 0.4$ -0.6 to 0.15-0.6, i.e., Néel order was destabilized but little effect was found on long-range order in the columnar region. This is quite different from the case in Sr₂Cu(Te_{1-x}W_x)O₆, where the frustrated region is widened toward the columnar region $(J_2/J_1 > 0.5; x > 0.2)$.

V. CONCLUSIONS

The entire solid-solution series $Sr_2Cu(Te_{1-x}W_x)O_6$ ($0 \le x \le 1$) was synthesized, the end members of the series being

spin-1/2 square-lattice antiferromagnets with Néel (x = 0) and columnar (x = 1) order. Magnetic susceptibility measurements suggest a maximum in frustration occurs near $x \approx 0.5$, where a spin-liquid-like ground state was previously observed. In the specific heat, a T-linear term typical of gapless QSLs or spin glasses is observed for a wide composition range of x = 0.1-0.7. Muon spin rotation and relaxation measurements indicate that long-range magnetic order is suppressed at least down to 1.5–1.8 K for a similar composition range of x =0.1–0.6. These results suggest that the spin-liquid-like ground state of x = 0.5 could be stabilized for a wide composition range, although a spin-glass ground state cannot be ruled out. The Néel magnetic order of x = 0 is destabilized with just 10% of Te-for-W substitution. In contrast, a gradual decrease in T_N from 24 to 7 K was found from x = 1 to 0.7 in the columnar side. Density-functional theory calculations indicate that the compounds with x > 0.2 are all in the columnar region. Thus, magnetic frustration arising from competing J_1 and J_2 interactions alone cannot explain the suppression of magnetic order for x = 0.1-0.6 and the spin-liquid-

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like ground state of x = 0.5; a combination of frustration and the quenched disorder present in this solid solution is required.

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