Ylä-Oijala, Pasi; Tzarouchis, Dimitrios; Wallén, Henrik; Sihvola, Ari

Spurious-Free Surface Integral Equation Characteristic Mode Formulation for Dielectric Bodies

Published in:

DOI:
10.1109/APUSNCURSINRSM.2018.8608430

Published: 01/01/2018

Document Version
Peer reviewed version

Please cite the original version:
Spurious-Free Surface Integral Equation
Characteristic Mode Formulation for
Dielectric Bodies

Pasi Ylä-Oijala, Dimitrios C. Tzarouchis, Henrik Wallén and Ari Sihvola
Department of Electronics and Nanoengineering
Aalto University, Espoo, Finland, pasi.yla-oijala@aalto.fi

Abstract—A new surface integral equation based formulation for computing characteristic modes of lossless and lossy dielectric and magneto-dielectric bodies is presented. For lossy objects, the imaginary part of an eigenvalue gives the ratio of the dissipated and radiated power, while the real part is connected to the ratio of the reactive and radiated power.

I. INTRODUCTION

The theory of characteristic modes (TCM) has recently attained a lot of interest in the antenna community. TCM provides excitation-independent eigensolutions that depend only on the shape and material of the structure. This allows analysis of the fundamental scattering and radiation properties of arbitrarily shaped structures.

The theoretical background of the TCM for PEC structures has been established [1], and refined for the electric field integral operator (EFIO) [2], already in the 1970's. For the magnetic and combined field integral operators (MFIO, CFIO), TCM has been developed only very recently [3]. The particularly important outcome of [3] is that, in order to obtain the same eigenvalues and eigencurrents as with the EFIO-based TCM, the roles of the real and imaginary parts of the MFIO appearing in the eigenvalue equation should be swapped.

For penetrable bodies the situation is more complicated, since the surface integral equation formulations typically include both the interior and exterior integral operators, and both electric and magnetic fields and currents. In [3] TCM was formulated for the symmetrical PMCHWT equations. This formulation, however, has been found to produce spurious modes [4]. Several alternative TCM formulations for dielectric bodies have been proposed [7], [8], [9], [10]. All these formulations, however, still either couple the internal and external equations and/or formulate the eigenvalue equation by interpreting the associated integral operator as an impedance-type operator.

We present a new surface integral equation-based TCM formulation that is free of spurious modes for lossless and lossy dielectric and magneto-dielectric bodies without requiring any additional postprocessing techniques [11].

II. FORMULATION

To formulate the new TCM formulation, let us start with the EFIE (without the excitation) written in the exterior (j = 1)

\[ \eta_1 T_1[J] - (K_1 + \frac{1}{2} n \times)[M] = 0, \]  \hspace{1cm} (1)

and the MFIE written in the interior (j = 2)

\[ \frac{1}{\eta_2} T_2[M] + (K_2 - \frac{1}{2} n \times)[J] = 0. \]  \hspace{1cm} (2)

Here \( T_j \) and \( K_j \) are the tangential EFIO and MFIO (without the residue term) of region \( j \). Next eliminate \( M \) from the equations by expressing it in terms of \( J \)

\[ M = \eta_2 (T_2)(K_2 + \frac{1}{2}n \times)[J] = P[J]. \]  \hspace{1cm} (3)

By substituting this into (1), gives an integral equation expressed solely in terms of the electric current

\[ \left( \eta_1 T_1 - (K_1 + \frac{1}{2} n \times) \right)[J] = 0. \]  \hspace{1cm} (4)

This equation is similar to the generalized impedance boundary condition formulation for conducting bodies [6].

We note that equation (4) contains two parts, one related to the electric field radiated by an electric current, operator \( Z_1' = \eta_1 T_1 \), and the other one related to the field radiated by the magnetic current, operator \( Z_M' = -(K_1 + 1/2n \times) \).

Consequently, the TCM eigenvalue equation for (4) reads

\[ \left( Z_1' + Z_M' P \right)[J_n] = (1 - i\lambda_n) \left( R_1' + iX_M' P \right)[J_n]. \]  \hspace{1cm} (5)

To avoid also the internal resonances associated with the EFIE-type formulation, a combined formulation is needed [11].

III. NUMERICAL RESULTS

For numerical solutions the surfaces are discretized with planar triangular elements and the equations are discretized with Galerkin’s method and RWG basis and test functions.

Consider first a lossless dielectric sphere with radius 4.6mm and \( \varepsilon_r = 40, \mu_r = 1 \). Fig. 1 shows the magnitudes of the eigenvalues of the three lowest order TE and TM modes computed with [3] and with analytical formulas [11].

The next example, Figs. 2 and 3 shows the real and imaginary parts of the eigenvalues for a lossy dielectric sphere with radius 4.6mm and \( \varepsilon_r = 40 + 2i, \mu_r = 1 \). The last example in Figure 4 shows the eigenvalues for a magneto-dielectric sphere with \( r = 4.6 \text{mm} \) and \( \varepsilon_r = 40, \mu_r = 3.5 \).
Fig. 1. Magnitudes of the eigenvalues for a lossless dielectric sphere, radius 4.6mm, \( \varepsilon_r = 40, \mu_r = 1 \). Numerical results are plotted with solid lines and analytical ones with symbols.

Fig. 2. Magnitudes of the real parts of the eigenvalues for a lossy dielectric sphere, radius 4.6mm, \( \varepsilon_r = 40 + 2i, \mu_r = 1 \), similarly as in Fig. 1.

Fig. 3. Magnitudes of the imaginary parts of the eigenvalues for a lossy dielectric sphere, radius 4.6mm, \( \varepsilon_r = 40 + 2i, \mu_r = 1 \), similarly as in Fig. 1.

Fig. 4. Magnitudes of the eigenvalues for a lossless magneto-dielectric sphere, radius 4.6mm, \( \varepsilon_r = 40, \mu_r = 3.5 \), similarly as in Fig. 1.

IV. CONCLUSION

A new spurious-free TCM formulation for lossless and lossy penetrable bodies is presented. In the formulation, the internal equations are only used to eliminate one of the currents from the equations and the required eigenvalue equation is formulated so that the obtained eigenvalues are related to the radiated power and have clear physical interpretation \([\text{11}]\). To avoid also the internal resonances associated with the EFIE-type formulation, a combined formulation is needed \([\text{11}]\).

REFERENCES


