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**Simulation of the interactions between hydraulic and natural fractures using a fracture mechanics approach**

*Published in:*
JOURNAL OF ROCK MECHANICS AND GEOTECHNICAL ENGINEERING

**DOI:**
10.1016/j.jrmge.2019.07.004

Published: 03/12/2019

*Document Version*
Publisher's PDF, also known as Version of record

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1. Introduction

The intermittent nature of some renewable energy sources derives from their over-supply during the low season and under-supply during the peak season. The solution is to accumulate and store the surplus energy seasonally and use it in times of high demand and low supply. HYDROCK is a method for storage and extraction of thermal energy in an artificially fractured hard rock aquifer developed in Sweden (Eriksson et al., 1983; Larson et al., 1983; Larson; Sundquist and Wallroth, 1990; Hellström and Larson, 2001). The HYDROCK method requires multiple parallel fracture planes of a sufficient radius at 2 m spacing are required. In addition, a sufficient hydraulic conductivity of the induced fractures is required to facilitate the hydraulic connection between the injection and extraction wells. Thus, the overall success of HYDROCK is reflected by the ability to construct a system with a sufficient number of parallel, induced fracture planes of a sufficient radial extent and hydraulic conductivity.

Hydraulic fracturing was first introduced for stimulation of wells in oil reservoirs (Clark, 1949). Since then, it has been used extensively for the extraction of shale gas (Wang et al., 2014), extraction of water from hard crystalline rocks (Less and Andersen, 1994; Joshi, 1996; Cobbing and Dochartaigh, 2007; dos Santos et al., 2011; Hart, 2016), and reservoir stimulation of enhanced...
geothermal systems (Pine and Batchelor, 1984; McClure and Horne, 2014; Olasolo et al., 2016). Other applications include in situ rock stress measurements (Amadei and Stephansson, 1997) and preconditioning of rock in block cave mining (He et al., 2016). Hubbert and Willis (1957) first postulated that the orientation of an induced hydraulic fracture follows the path of least resistance. Thus, it initiates in the plane perpendicular to the axis of the minimum principal in situ rock stress. However, away from the drill hole, a fracture driven by fluid flow is influenced by the local geology and the hydraulic fracture may alter its orientation if discontinuities or flaws disturb the local stress orientation. Fracture branching, offset crossing and non-planar fracture growth were frequently observed in laboratory and field experiments on hydraulic fracturing in rocks with pre-existing discontinuities (Lamont and Jensen, 1963; Blanton, 1982, 1986; Warpinski and Teufel, 1987; Jeffrey, 1996; Cheng et al., 2014; Dehghan et al., 2015).

In view of that, the presence of the pre-existing fractures in the rock mass may arrest or divert the induced hydraulic fracture leading to a more complex fracture network in comparison with the ideal, sub-horizontal fracture planes as assumed in the HYDROCK concept presented by Hellström and Larson (2001). Therefore, understanding of the complex interaction mechanisms between hydraulic and natural fractures is necessary for a successful implementation of the HYDROCK method.

Many authors provide analytical models capable of predicting whether the crossing of a natural fracture by an induced fracture will occur based on laboratory observations (Blanton, 1982, 1986; Warpinski and Teufel, 1987; Renshaw and Pollard, 1995; Gu and Weng, 2010; Cheng et al., 2014; Liu et al., 2014; Sarmadivaleh and Rasouli, 2014). The criteria are based on several factors, such as the differential stress, the approach angle between the hydraulic and natural fractures, and the properties of the pre-existing fracture. Sarmadivaleh and Rasouli (2014) provided a comprehensive summary of the available analytical criteria for fracture crossing.

However, due to the inherent complexity of the hydraulic fracturing process and the interactions between induced and pre-existing fractures, laboratory investigations and analytical criteria have limited applicability attributable to their inherent assumptions and simplifications. Therefore, numerical methods that enable hydro-mechanical (HM) coupling of the fluid flow and the mechanical response of the rock mass are used extensively to simulate the hydraulic fracturing process in the presence of pre-existing discontinuities. The commonly used numerical methods for simulation of hydraulic fracturing in fractured rock masses include the finite element method (FEM) (e.g. Xu et al., 2015), the extended finite element method (XFEM) (e.g. Dahi-Taleghani, 2009; Shi et al., 2017), and the boundary element method (BEM) including the displacement discontinuity method (DDM) (e.g. Zhang and Jeffrey, 2006, 2008; Zhang et al., 2007, 2009; Kresse et al., 2013; Kear et al., 2017; Xu et al., 2019), distinct element method (DEM) (e.g. Yoon et al., 2014, 2015a, b; Zangeneh et al., 2015; Damjanac and Cundall, 2016; Zhang et al., 2018), and hybrid finite-distinct element method (FDEM) (e.g. Lisjak et al., 2017).

In this study, we aim to investigate the interactions between hydraulic and natural fractures in low permeability granitic rock using a numerical model developed in FRACOD2D (fracture propagation code), a two-dimensional (2D) boundary element code based on the DDM principles with integrated fracture mechanics approach (Shen et al., 2014). The added value of using FRACOD in this study is that it can simulate the explicit fracturing of brittle rocks. FRACOD has been used extensively for modelling of rock fracturing processes in numerous applications (e.g. Rinne et al., 2013; Shen, 2014; Shen et al., 2014, 2015; Barton and Shen, 2017), including coupled HM simulations of hydraulic fracturing (Shen and Shi, 2016; Xie et al., 2016; Janiszewski et al., 2018). Xie et al. (2016) presented a validation case of the hydraulic fracture simulator in FRACOD and demonstrated an example of the interaction between hydraulic and natural fractures. However, only one case with a low approach angle was tested. Hence, the first objective of this study is to test whether the realistic interaction mechanisms at different approach angles can be reproduced in FRACOD enhanced by the new fracture crossing function. The second objective is to validate the FRACOD model against the analytical criterion for fracture crossing by Sarmadivaleh and Rasouli (2014).

The structure of this paper is as follows. First, we introduce a brief summary of FRACOD theory and the new functionality of FRACOD that enables crossing of natural fractures by an approaching hydraulic fracture. Then, we test the new FRACOD improvement in a series of coupled HM models simulating an interaction between hydraulic and natural fractures in granitic rock for a range of approach angles. We discuss the implications of the fracture interaction on the HYDROCK method. Next, we validate the FRACOD model against an analytical criterion for fracture crossing. Finally, we investigate the evolution of the interaction mechanisms as a function of the controlling parameters.

2. Theoretical background of FRACOD

FRACOD uses an indirect boundary element technique — DDM for stress analysis, with fracture mechanics theory integrated into it. FRACOD is based on analytical solutions of displacements and stresses that are produced by a constant displacement discontinuity over a finite crack element in an infinite elastic body. The DDM method helps to find the discrete approximation of the smooth distribution of relative displacement presented in real cracks (Shen et al., 2014).

FRACOD uses the F-criterion for fracture propagation that was first proposed by Shen and Stephansson (1994) as a modified
maximise strain energy release rate criterion (G-criterion). The F-criterion is capable of simulating mode I (tension) and mode II (shear) fracture propagation independently, along with mixed mode (mode I-II) fracture propagation taking place concurrently. The F-criterion is used to determine the propagation direction $\phi$ of the fracture and the failure load by calculating the sum of strain energy release rate for both mode I ($G_I$) and mode II ($G_{II}$), normalised by the critical strain energy release rates $G_{IC}$ and $G_{IC}$.

Fracture propagation takes place when the following equation is satisfied:

$$F(\phi) = \frac{G_I(\phi)}{G_{IC}} + \frac{G_{II}(\phi)}{G_{IC}} \geq 1 \quad (1)$$

Fracture initiation in the intact rock can take place in tension or shear. For mode I tensile fractures, one of the criteria that can be used is the tensile stress criterion, which predicts that fracture initiation will occur when the tensile stress is larger than or equal to the tensile strength of rock:

$$\sigma_t \geq T_0 \quad (2)$$

where $\sigma_t$ is the tensile stress, and $T_0$ is the tensile strength of rock.

The other failure criterion that can be used for tensile fracture initiation is the extensional strain criterion (Barton and Shen, 2017). The generated mode I fracture is perpendicular to the maximum tensile stress (or extensional strain).

For mode II shear fractures, one of the criteria that can be used is the Mohr-Coulomb criterion, which predicts that fracture initiation will occur when the shear stress is larger than or equal to the shear strength of rock:

$$\sigma_s \geq \sigma_n \tan \varphi + c \quad (3)$$

where $\sigma_s$ is the shear stress, $\sigma_n$ is the normal stress, $\varphi$ is the internal friction angle of intact rock, and $c$ is the cohesion of intact rock.

Another shear criterion that can be used is the modified non-linear Mohr-Coulomb criterion (Shen et al., 2018). Mode II fractures are generated in the direction of the predicted shear failure plane.

FRACOD can simulate the bidirectional HM coupling using an explicit approach, where both the deformation with fracture propagation and the fluid flow are simulated using the time marching iteration scheme. The fluid flow in fractures is fully dynamic and governed by the cubic law. The use of cubic law and laminar flow is based on an assumption that the flow plane is narrow and the flow speed is relatively low, and hence the turbulent flow can be neglected. A more detailed description of the HM coupling in FRACOD, as well as a validation case of hydraulic fracturing simulator, was given by Xie et al. (2016).

As the hydraulic fracture is propagating horizontally, the fracture tips will reach the inclined pre-existing fracture and will lose the fracture tip. Hence the fracture criterion, i.e. the F-criterion, is no longer applicable. Therefore, new functionality is added to FRACOD to allow for the crossing of pre-existing fractures by the propagating hydraulic fracture. The FRACOD code is enhanced by checking the stress state at the surface of the fracture and then determining whether a fracture initiation is possible using the stress-based initiation criterion (i.e. the tensile stress criterion for tensile failure (Eq. (2))) and the Mohr-Coulomb criterion for shear failure (Eq. (3)).

### 3. Modelling the interactions between hydraulic and natural fractures in FRACOD

#### 3.1. Adaptive modelling approach

This study can be considered as a data-limited problem because no experimental data were produced, and the amount of information from the literature was limited. The rock mass is a highly non-uniform material, and thus the outcomes from one site may not apply to another location. Hence, the adaptive modelling approach suggested by Starfield and Cundall (1988) was employed to overcome the difficulties of a data-limited problem:

1. **The aim of modelling.** The aim of modelling is to study the interaction between induced hydraulic fracture and pre-existing natural fracture that may arrest the induced fracture and inhibit its growth, which could lead to problems with permeability enhancement of the rock mass.

2. **Conceptual model.** The model represents a 2D section of the rock mass characterised by high differential rock stress where $\sigma_{xx} > \sigma_{yy}$ with a single injection well generating the hydraulic fracture that is propagating horizontally, until it approaches and interacts with the natural fracture (see Fig. 2).

3. **Mechanics of the problem.** The induced hydraulic fracture may interact with the natural fracture that lies on its propagation path and five types of geomechanical interaction mechanisms are possible, i.e. crossing, arresting (no crossing), dilation, activation, and offset crossing. Additionally, mixed mechanisms are also possible. The development of those mechanisms is depicted in Fig. 3. A more comprehensive description of the possible interactions was given by Cheng et al. (2015).

4. **Experiment.** The approach angle was varied to test if the realistic interaction mechanisms described in the previous steps can be reproduced numerically. Results are compared to analytical criteria from the literature and discussed in relation to HYDROCK method.

5. **Increasing complexity.** Once the simple model has been explored and the lessons are learned, the complexity can be increased in order to study other aspects of geology that have been omitted, for example, more extensive fracture network consisting of one or more joint sets. However, this study only considered a single hydraulic fracture interacting with a natural fracture.
3.2. Model setup in FRACOD

The numerical model was developed in FRACOD according to the conceptual model given in Fig. 2. The 2D model consisted of an injection well of 0.1 m diameter with a pre-existing fracture extending from the borehole as a kink for simplifying fracture propagation. A natural fracture of 0.3 m in length was placed to the right of the borehole at a distance of 0.2 m. The model was symmetrical against the central point (X = 0 m, Y = 0 m). A grid size of 0.01 m was used. A series of models was prepared with the approach angle \( \theta \) ranging between 90° and 40° at 10° interval. An example of the model geometry with the approach angle equal to 60° is shown in Fig. 4. It has to be noted that the model represented a vertical section of the rock mass with the source of fluid pressure modelled as a circle. Also, the geometry of 0.5 m \( \times \) 0.5 m was only used for plotting the results, and the actual model geometry extended infinitely according to the principles of the BEM where only the inner boundary problem was simulated.

To simulate hydraulic fracturing, a synthetic granitic rock mass was assumed that reflects the realistic geomechanical properties of the Bohus granite, which hosted the first HYDROCK field experiment conducted by Larson et al. (1983). The input properties used for the numerical model are given in Table 1. The assumed values aimed to reflect the typical properties of granitic rock. The far-field in situ rock stresses were assumed to be 8 MPa and 1.5 MPa in the horizontal and vertical directions, respectively.

The tensile stress criterion (Eq. (2)) was used for tensile fracture initiation and the Mohr–Coulomb failure criterion (Eq. (3)) for shear fracture initiation, which allows fracture initiation at fracture surfaces to fracture crossing. The fluid flow was fully dynamic with a constant injection pressure of 8 MPa assigned to the borehole boundary. Water at a temperature of 20 °C with a bulk modulus of 2 GPa and a dynamic viscosity of 0.001 Pa s was used as the fracturing fluid in the simulation.

4. Results of the interactions for a series of approach angles

The modelling results of the interactions between hydraulic and natural fractures are shown in Figs. 5 and 6. It can be observed that the interactions between hydraulic and natural fractures are dependent on the approach angle.

The models containing natural fracture at large approach angles (\( \theta \geq 70° \)) (Fig. 5a–c) simulated the crossing interaction mechanism as shown in Fig. 3b. The natural fracture was also dilated and sheared in the vicinity of the intersection point due to induced stresses ahead of the hydraulic fracture tip (dilation). Nevertheless, the fracturing fluid did not penetrate the natural fracture within the given time period and only followed the path of the propagating hydraulic fracture that crossed the natural fracture (Fig. 6a). This can be explained by the very low aperture of the natural fracture (1 \( \mu m \)) and high horizontal stress resulting in high normal stresses acting on the natural fracture surface, which prevented complete opening of the natural fracture and the fluid pressure build-up in the tight fracture. The induced fracture was hydraulically conductive (Fig. 6d) and hence, the presence of natural fracture situated at large angles with respect to the hydraulic fracture appears not to impair the construction process of the HYDROCK method.
At an approach angle equal to 60° (Figs. 5d and 6b), the model reproduced the activation and offset crossing interaction mechanism as shown in Fig. 3e. Due to the lower normal stress acting on the natural fracture surface, the natural fracture experienced shear displacement that caused its activation and mode I fracture initiation from its upper tip in the direction of the maximum horizontal stress. In addition, the shear movement of the natural fracture resulted in stress concentration and offset crossing of the hydraulic fracture.

The models containing the natural fracture at low approach angles ($\theta \leq 50°$) (Fig. 5e and f) simulated the arresting and activation of hydraulic and natural fracture interaction as shown in Fig. 3d. The slippage of the natural fracture resulted in mode I fracture initiated at the upper tip of the natural fracture that propagated into the rock mass as a dry wing-shaped fracture (Fig. 5f). Then, the fracturing fluid penetrated the newly formed tensile fracture and propagated it further in the direction of the maximum horizontal stress (Fig. 6c). This type of wing-shaped fracture is identical to wing-fractures generated in the laboratory by loading rock specimens with inclined fracture (Shen et al., 1995). This outcome agrees well with the results of PFC2D numerical simulations of hydraulic and natural fracture interactions by Yoon et al. (2017) and Zhang et al. (2018) who observed similar fractures in their numerical models. Arresting, activation and propagation of the wing-shaped tensile fractures result in a more complex fracture propagation path, which differs from the ideal sub-horizontal fracture that was assumed in the ideal HYDROCK case described by Hellström and Larson (2001). Even though the

### Table 1
Input parameters for the numerical model that reflect a granitic rock mass of low permeability.

<table>
<thead>
<tr>
<th>Input parameter</th>
<th>Value</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rock type</td>
<td>Bohus granite</td>
<td>Larsson (1983)</td>
</tr>
<tr>
<td>Intact rock tensile strength, $\sigma_t$ (MPa)</td>
<td>10.5</td>
<td></td>
</tr>
<tr>
<td>Intact rock friction angle, $\phi$ (°)</td>
<td>45</td>
<td>Assumed</td>
</tr>
<tr>
<td>Intact rock cohesion, $c$ (MPa)</td>
<td>25</td>
<td></td>
</tr>
<tr>
<td>Elastic modulus, $E$ (GPa)</td>
<td>53</td>
<td>Larsson (1983)</td>
</tr>
<tr>
<td>Poisson’s ratio, $\nu$</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Mode I fracture toughness, $K_{IC}$</td>
<td>1.8</td>
<td>Liu et al. (2010)</td>
</tr>
<tr>
<td>Mode II fracture toughness, $K_{IIC}$</td>
<td>4</td>
<td>Assumed</td>
</tr>
<tr>
<td>(MPa m$^{1/2}$)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Horizontal in situ stress, $\sigma_{XX}$ (MPa)</td>
<td>-8</td>
<td>Larsson (1983)</td>
</tr>
<tr>
<td>Vertical in situ stress, $\sigma_{YY}$ (MPa)</td>
<td>-1.5</td>
<td></td>
</tr>
<tr>
<td>Fracture shear stiffness, $k_s$ (GPa/m)</td>
<td>3099</td>
<td>Shen et al. (2011)</td>
</tr>
<tr>
<td>Fracture normal stiffness, $k_n$ (GPa/m)</td>
<td>13,800</td>
<td></td>
</tr>
<tr>
<td>Fracture friction angle, $\phi_f$ (°)</td>
<td>45</td>
<td>From intact rock strength</td>
</tr>
<tr>
<td>Fracture cohesion, $c_f$ (MPa)</td>
<td>0</td>
<td>Assumed</td>
</tr>
<tr>
<td>Fracture dilation angle, $\phi_d$ (°)</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>In situ hydraulic conductivity, $K_{is}$ (m/s)</td>
<td>$1 \times 10^{-19}$</td>
<td></td>
</tr>
<tr>
<td>Fracture initial aperture, $a_{initial}$ (μm)</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Fracture residual aperture, $a_{residual}$ (μm)</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Fluid injection pressure, $P_{in}$ (MPa)</td>
<td>8</td>
<td></td>
</tr>
<tr>
<td>Fluid bulk modulus, $E_w$ (GPa)</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>Fluid viscosity, $\mu$ (Pa s)</td>
<td>0.001</td>
<td></td>
</tr>
<tr>
<td>Fluid density, $\rho$ (kg/m$^3$)</td>
<td>1000</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 5. FRACOD modelling results of the interactions with a natural fracture. (a–c) At approach angles $\theta = 90°$, 80°, and 70°, the hydraulic fracture crossed the natural fracture and propagated further into the rock mass; (d) At $\theta = 60°$, the hydraulic fracture crossed the natureal fracture at an offset and activated the natural fracture due to shear slippage causing propagation from the tip of the natural fracture; (e, f) At $\theta = 50°$ and 40°, the hydraulic fracture was arrested at the natural fracture, causing its activation and opening by the penetrating fluid that resulted in further propagation from the upper tip of the natural fracture.
Fractures are hydraulically conductive (Fig. 6e and f), coalescence of multiple fracture planes could occur at different depths that would reduce the total heat exchange area, decreasing the thermal performance of the HYDROCK method.

The obtained results of the dependency of the interaction between hydraulic and natural fractures on the approach angle are in good agreement with previous experimental (e.g. Zhou et al., 2008; Cheng et al., 2014) and numerical studies (e.g. Yoon et al., 2017; Zhang et al., 2018). FRACOD is able to simulate all interaction mechanisms, such as crossing, arresting, dilation, activation, and offset crossing, which were described by Cheng et al. (2015).

Nevertheless, some differences were observed in the branching of the fractures from the tip of the natural fracture compared to the schematic representation of interaction mechanisms depicted in Fig. 3d, e and g. Due to the displacement of the block below the right wing of the hydraulic fracture (Fig. 7a), the bottom half of the natural fracture is closed, resulting in very low aperture (Fig. 7b), so that the fluid can only penetrate the upper part of the natural fracture (Fig. 7c). An analogous result was obtained by Xie et al. (2016), where no bifurcation of the flow was observed in FRACOD model of hydraulic and natural fracture interaction, even though the natural fracture had an initial aperture of 100 μm. However, no fracture crossing function was used in their study and only one approach angle was tested. This behaviour can differ if the initial aperture of the natural fracture is larger, as the used value of 1 μm represents a very low permeability fracture. Higher fracture

![Figure 6. Modelling results depicting fluid pressure distribution (a–c) and hydraulic conductivity (d–f) for three different interaction mechanisms of the hydraulic and natural fractures: (a–c) Fluid pressure distribution within the fractures for approach angles $\theta = 90^\circ$, 60°, and 40°, respectively; and (d–f) Hydraulic conductivity of fractures for approach angles $\theta = 90^\circ$, 60°, and 40°, respectively.](image)

![Figure 7. Close-up view of simulated interaction from Fig. 5f at approach angle equal to 40°: (a) Displacement distribution, (b) Fracture aperture, and (c) Fluid pressure distribution. Due to the displacement of the block below the right wing of the hydraulic fracture (a), the bottom half of the natural fracture is closed, resulting in very low aperture (b), so that the fluid can only penetrate the upper part of the natural fracture (c).](image)
 aperture could allow the fluid to penetrate and dilate the natural fracture, resulting in the bifurcation of the flow. This problem is addressed in Section 5, where the interactions of hydraulic fracture with a pre-existing natural fracture of larger aperture are tested.

It also has to be noted that the results presented in this study are limited to a 2D case of the hydraulic and natural fracture interaction, e.g. the horizontal hydraulic fracture interacting with the dipping natural fracture, which neglects the influence of the natural fracture strike angle. A criterion that addresses this problem in three-dimensional (3D) space was given by Cheng et al. (2014), which states that crossing can take place only at large approach and strike angles. In addition, the fracture propagation and release of the hydraulic pressure in 3D space will tend to follow the path of least resistance and can propagate also in the out-of-plane direction, where there is no discontinuity that disturbs the stress field ahead of the fracture tip. Therefore, it is recommended to study this problem in future using a numerical code that is capable of coupled HM simulations in 3D space.

Results of the simulations were compared to the modified Renshaw and Pollard analytical criterion by Sarmadivaleh and Rasouli (2014). The criterion predicts whether the induced fracture will cross the interface or become arrested at the interface. The crossing occurs when the following equation is satisfied (Sarmadivaleh and Rasouli, 2014):

$$\frac{\theta_0 - \sigma_T}{\tau_0 - \sigma_n} = \left(1 - \sin^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \alpha}}}}}}{1 + \sin^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \alpha}}}}}}\right)^2$$

(4)

where $\mu_f^2$ is an imaginary friction coefficient, $\sigma_T$ is the tangential stress applied on the natural fracture surface (Jaeger et al., 2007), and $\alpha$ is a coefficient. These parameters can be calculated as follows:

$$\mu_f^2 = \mu_f + \frac{\tau_0/\sigma_n}{1 - \sin^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \frac{\mu_f^2}{\cos^2 \alpha}}}}}} - 1$$

(5)

$$\sigma_n = \frac{\sigma_{xx} + \sigma_{yy}}{2} + \frac{\sigma_{xx} - \sigma_{yy}}{2} \cos(\pi - 2\theta)$$

(6)

$$\sigma_T = \frac{\sigma_{xx} + \sigma_{yy}}{2} - \frac{\sigma_{xx} - \sigma_{yy}}{2} \cos(\pi - 2\theta)$$

(7)

$$\alpha = \frac{\tau}{\cos(\theta/2) \left[1 + \sin(\theta/2 \sin(\theta/2)) \right]}$$

(8)

where $\tau$ is the shear stress applied along the natural fracture (Jaeger et al., 2007), $\tau_0$ is the Mohr-Coulomb joint shear strength, and $\mu_f$ is the friction coefficient.

The results of the comparison are shown in Table 2. It can be observed that FRACOD predicts the same type of interaction as the analytical criterion does. Only in one case — when the approach angle is equal to 60°, the FRACOD model simulates activation and offset crossing, whereas the analytical criterion predicts crossing. However, it should be noted that the analytical criterion can only predict whether the hydraulic fracture will cross the natural fracture and cannot predict any complex interactions, such as the mixed activation and offset crossing mode. Hence, it can be concluded that the numerical predictions obtained from FRACOD agree with the analytical predictions.

### 5. Investigation of the evolution of the interaction mechanisms as a function of controlling parameters

Several scenarios were prepared to test the influence of other controlling parameters on the evolution of the interaction mechanisms between the propagating hydraulic fracture and the pre-existing natural fracture.

#### 5.1. The effect of fracture aperture

The fracture aperture dictates its permeability so that a larger aperture results in an easier penetration of the fracturing fluid. To test the effect of the natural fracture’s aperture on the crossing behaviour, the pre-existing fracture’s aperture was varied between 1 μm, 10 μm, 25 μm and 50 μm, respectively. The dip angles of the natural fracture equal to 90°, 60° and 40° were used to reproduce multiple interaction mechanisms. All parameters were set the same as those in Table 1. The modelling results are given in Fig. 8. It can be seen that in models with the natural fracture dipping at 90° (Fig. 8a–d), the larger the aperture is, the easier the fracturing fluid penetrates and opens the fracture. However, increasing the aperture did not change the fracturing pattern, because the natural fracture’s tips were not activated and the hydraulic fracture simply crossed the natural fracture with the same propagation path. In models with the natural fracture dipping at 60° (Fig. 8e–h), the interaction mechanisms changed with the increased fracture aperture. When the aperture was equal to 1 μm (Fig. 8e), the hydraulic fracture crossed the natural fracture at a small offset because the fluid could not penetrate the natural fracture. As the aperture increased (Fig. 8f and g), the fluid penetrated the natural fracture and then crossed the natural fracture at a point located further away from the intersection when compared to the previous
Fig. 8. Modelling results depicting fracturing pattern and fluid pressure distribution as a function of the natural fracture’s aperture equal to 1 μm, 10 μm, 25 μm and 50 μm, respectively; (a–d) Approach angle $\theta = 90^\circ$, (e–h) $\theta = 60^\circ$, and (i–l) $\theta = 40^\circ$. A general observation is that the larger the fracture aperture, the easier the fracturing fluid infiltrates the pre-existing fracture and changes the interaction mechanism.
case. At the same time, the upper tip of the natural fracture was activated and mode I fracture initiation occurred in the direction of maximum horizontal stress. The hydraulic fracture ultimately coalesced with this fracture creating a similar fracture pattern as arresting and activation type of hydraulic and natural fracture interaction mechanism shown in Fig. 3d. In models with the approach angle of 40° (Fig. 8i–l), the increase of fracture aperture did not change the arresting and activation interaction mechanism. However, the larger the aperture, the easier the fluid permeates the natural fracture, resulting in the bifurcation of the flow and branching of the hydraulic fracture from both tips of the natural fracture (Fig. 8l).

5.2. The effect of fracture cohesion

The effect of increased shear strength of the pre-existing fracture was tested by setting the cohesion of the natural fracture to 1 MPa (Fig. 9d–f) and comparing it with the cohesionless case where fracture cohesion was 0 MPa (Fig. 9a–c). All parameters were set the same as those in Table 1, except the aperture of the natural fracture, which was set to 10 μm.

Here, the difference was most visible in the scenario with approach angle of 60°, where the increased shear strength of the natural fracture promoted the crossing interaction mechanism (Fig. 9e) compared to the arresting and offset crossing interaction mechanism in the cohesionless case (Fig. 9b). In the model with natural fracture dipping at 40° (Fig. 9c and f), the only difference was a slight change of the path of the wing-shaped mode I fracture that propagated from the tip of the natural fracture. These results are in line with the observations in the literature, for example, PFC2D models made by Zhang et al. (2018).

5.3. The effect of differential in situ rock stress

The differential in situ rock stress is one of the factors in the analytical criteria for fracture crossing prediction (e.g., Sarmadiane and Rasouli, 2014). To test the interactions of hydraulic and natural fractures in a less anisotropic in situ rock stress environment in FRACOD, the vertical in situ rock stresses was increased to 4 MPa (Fig. 10d–f) while keeping the horizontal stress at 8 MPa. All other parameters were set the same as those in Table 1, except the aperture of the natural fracture that was set to 10 μm. The injection pressure in the models with the lower differential stress was increased to 14.5 MPa to enable propagation of the hydraulic fracture. The modelling results are depicted in Fig. 10.

The difference in the interaction behaviour is most visible in the scenario with the approach angle of 60° (Fig. 10e), which resulted in the crossing interaction mechanism, as opposed to the model with more anisotropic in situ rock stresses that resulted in activation and offset crossing interaction mechanism (Fig. 10b). The difference can be attributed to the higher value of vertical stress, which resulted in greater normal stress acting on the natural fracture. Hence the crossing was more plausible and the propagation path was different.

5.4. The effect of fluid viscosity

Ishida et al. (2004) and Chen et al. (2015) observed in laboratory experiments of hydraulic fracturing in granitic specimens that
Fig. 10. Modelling results depicting fracturing pattern and fluid pressure distribution as a function of the in situ rock stresses acting in X and Y directions: (a–c) Horizontal stress $\sigma_{XX} = 8$ MPa and vertical stress $\sigma_{YY} = 15$ MPa, (d–f) $\sigma_{XX} = 8$ MPa and $\sigma_{YY} = 0.5$ MPa, and (g–i) $\sigma_{XX} = 8$ MPa and $\sigma_{YY} = 4$ MPa, for approach angles $\theta = 90^\circ$, 60$^\circ$, and 40$^\circ$, respectively.

Fig. 11. Modelling results depicting fracturing pattern and fluid pressure distribution as a function of fluid viscosity: (a–c) Low viscosity, and (d–f) High viscosity, for approach angles $\theta = 90^\circ$, 60$^\circ$, and 40$^\circ$, respectively. The fractures that propagated with high viscosity oil are less convoluted compared to the fractures propagating with water. At approach angle equal to 60$^\circ$, fluid viscosity has an influence on the type of interaction between the hydraulic and natural fractures.
modifying the fracturing fluid viscosity influences the pattern of fracture propagation path so that a lower viscosity fracturing fluid creates a more convoluted fracture network with more branching. To test the influence of fluid viscosity on the interactions between hydraulic and natural fractures in FRACOD, the fluid viscosity of the fracturing fluid was set to 0.001 Pa s and 0.08 Pa s, which correspond to water and oil used by Ishida et al. (2004), respectively. All other parameters were set the same as those in Table 1, except the aperture of the natural fracture that was set to 10 μm. The modelling results are given in Fig. 11.

The difference between the hydraulic and natural fracture interaction with low and high viscosity fracturing fluids was most pronounced in the model with approach angle of 60°. Fracturing with water resulted in the arresting and offset crossing type of interaction mechanism and a more convoluted fracturing pattern (Fig. 11b). The hydraulic fracture crossed the natural fracture at an offset that later coalesced with the dry wing-shaped fracture that propagated from the natural fracture tip. In contrast, fracture with viscous oil resulted in the crossing type of interaction with a planar crack propagating directly across the natural fracture in the direction of horizontal stress (Fig. 11e). The results may be explained by the lower velocity of the high viscosity fluid that enabled faster pressure build-up required for crossing and created a more planar fracture. This result is consistent with laboratory observations by Ishida et al. (2004) and Chen et al. (2015) who also observed that high viscosity fracturing fluid creates more planar and smooth fractures. At approach angle equal to 40° (Fig. 11c and f), the same type of hydraulic and natural fracture interaction was observed. Even though the hydraulic fracture that propagated from the tip of the natural fracture with high viscosity fluid appeared as more planar (Fig. 11f), the differences were less pronounced. At approach angle equal to 90° (Fig. 11a and d), no differences were observed.

6. Conclusions

In this study, we briefly describe the new functionality of the fracture propagation code FRACOD that allows for fracture initiation from the fracture surface when a hydraulically driven fracture intersects a pre-existing natural fracture. We developed a series of coupled HM numerical models to simulate the interaction between hydraulic and natural fractures to study their implications on an artificially fractured hard rock aquifer for thermal energy storage. Based on the simulation results, the following conclusions are drawn:

1. FRACOD, enhanced by the new crossing fracture functionality, can simulate all the interactions between induced hydraulic and natural fractures, including crossing, arresting, dilation, activation and offset crossing, as well as their combination. At large approach angles, the hydraulic fracture can cross the natural fracture and propagate further into the rock mass without changing the original propagation path. At small approach angles, the interactions between hydraulic and natural fractures involve arresting of the hydraulic fracture at the pre-existing fracture, its activation and development of wing-shaped tensile fracture from the tip of the natural fracture.
2. The comparison of the numerical results and the modified Renshaw and Pollard analytical criterion for fracture crossing shows a general agreement for a series of approach angles.
3. The presence of natural fractures that are inclined at large angles with respect to the horizontal hydraulic fracture does not prevent the development of sub-horizontal fracture planes for the HYDROCK method. Conversely, the presence of fractures inclined at low angles with respect to the horizontal hydraulic fracture can lead to fracture arrest and development of more complex fracture network. This may impair the thermal performance of the HYDROCK method due to the coalescence of multiple hydraulic fractures and a reduction of heat exchange area.
4. An increase of the aperture of the natural fracture does have an influence on the interaction mechanism due to higher permeability of the pre-existing fracture that can lead to double branching of the flow in the arrest and activation interaction mechanism, or shifting the offset location in the activation and offset crossing mechanism.
5. An increase of the natural fracture’s cohesion is likely to promote the crossing type of interaction mechanism at intermediate approach angles due to an increase of the shear strength of the natural fracture that prevents its opening by the fracturing fluid and its activation.
6. The interaction of hydraulic and natural fractures is dependent on the anisotropy of the in situ rock stresses and crossing of the natural fracture is more likely at intermediate approach angles with lower differential stress.
7. The fluid viscosity has an influence on the type of interactions between hydraulic and natural fractures at intermediate approach angles. The use of low viscosity fracturing fluid, such as water, results in more convoluted fracturing pattern that can be beneficial for creating a larger heat exchange area in the HYDROCK method.

In future, numerical simulations based on the fracture mechanics approach will be used to study the interactions of single and multiple hydraulic fractures in a fractured rock mass that contains one or more joint sets to study their influence on HYDROCK method at the field scale.

Conflicts of interest

The authors wish to confirm that there are no known conflicts of interest associated with this publication and there has been no significant financial support for this work that could have influenced its outcome.

Acknowledgement

The financial support from Aalto Doctoral Programme in Engineering and the International Collaboration Project on Coupled Fracture Mechanics Modelling – Phase 3 (project team consisting of CSIRO, SDUST, Posiva, KIGAM, KICT, CAS-IRSM, DUT/Mechsoft, SNU, LBNL, ETH, Aalto Univ., GFZ and TYUT) is kindly acknowledged.

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