Potkina, M. N.; Lobanov, I. S.; Tretiakov, O. A.; Jónsson, H.; Uzdin, V. M.

Stability of long-lived antiskyrmions in the Mn-Pt-Sn tetragonal Heusler material

Published in:
Physical Review B

DOI:
10.1103/PhysRevB.102.134430

Published: 26/10/2020

Please cite the original version:

This material is protected by copyright and other intellectual property rights, and duplication or sale of all or part of any of the repository collections is not permitted, except that material may be duplicated by you for your research use or educational purposes in electronic or print form. You must obtain permission for any other use. Electronic or print copies may not be offered, whether for sale or otherwise to anyone who is not an authorised user.
Stability of long-lived antiskyrmions in the Mn-Pt-Sn tetragonal Heusler material

M. N. Potkina,1,2,3 I. S. Lobanov,2,3 O. A. Tretiakov,4 H. Jónsson,1,5 and V. M. Uzdin2,3

1Science Institute and Faculty of Physical Sciences, University of Iceland, 107 Reykjavík, Iceland
2Department of Physics, St. Petersburg State University, 198504 St. Petersburg, Russia
3Faculty of Physics and Engineering, ITMO University, 197101 St. Petersburg, Russia
4School of Physics, The University of New South Wales, Sydney 2052, Australia
5Department of Applied Physics, Aalto University, FIN-00076 Espoo, Finland

 DOI: 10.1103/PhysRevB.102.134430

(Received 15 August 2020; revised 28 September 2020; accepted 1 October 2020; published 26 October 2020)

The lifetime of antiskyrmions at room temperature in an Mn–Pt–Sn tetragonal Heusler material has been calculated using an atomic scale representation including nearly a million spins. The evaluation of the pre-exponential factor in the Arrhenius rate expression for this large system is made possible by implementation of harmonic transition state theory that avoids evaluation of the eigenvalues of the Hessian matrix. The parameter values in the extended Heisenberg Hamiltonian, including anisotropic Dzyaloshinskii-Moriya interaction, are chosen to reproduce experimental observations [Nayak et al., Nature (London) 548, 561 (2017)], in particular, the 150-nm diameter. The calculated results are consistent with the long lifetime observed in the laboratory and this exceptional stability of the antiskyrmions is found to result from large activation energy for collapse due to strong exchange coupling while the pre-exponential factor in the Arrhenius expression for the lifetime is found to have a typical magnitude of 10^{-12} s, despite the large number of spins. The long lifetime is, therefore, found to result from energetic effects rather than entropic effects in this system.

I. INTRODUCTION

Skyrmions and antiskyrmions are localized magnetic states that have been proposed as elements in future spintronics devices [1–3]. Along with interesting transport properties, such states can exhibit particlelike behavior and carry a topological charge that enhances their stability with respect to the uniform ferromagnetic or antiferromagnetic states. A key issue is the lifetime of (anti)skyrmions and its dependence on temperature and applied magnetic field. The challenge is to find or design materials where such magnetic states are sufficiently stable at ambient temperature and still small enough to be used in high density spintronic devices. Figure 1 shows the spin configuration of an antiskyrmion as well as that of a skyrmion.

So far, stability at room temperature has mainly been obtained for large skyrmions with a diameter of 50 nm or more [4,5]. It is important to understand what determines the lifetime in order to guide the search for materials where smaller (anti)skyrmions are sufficiently stable at room temperature. From recent experimental studies of skyrmions in Fe_{1-x}Co_{x}Si, a large, destabilizing entropic contribution which reduces the lifetime of skyrmions has been reported [6]. On the other hand, theoretical studies have found that isolated skyrmions can be stabilized by entropic contributions [7–11]. The question we address here is whether this is also the case for the recently observed stable antiskyrmions in acentric tetragonal Heusler compounds [12]. The diameter of these antiskyrmions is large, 150 nm, but it may be possible to modify materials parameters in some way to obtain smaller antiskyrmions that are still stable at room temperature.

Antiskyrmions offer some advantage over skyrmions in that they can under some conditions move in the direction of an applied spin polarized current, while skyrmions necessarily move at an angle [13].

Skyrmions have been studied for several systems and recent reviews have summarized results obtained [3,4]. The annihilation of a skyrmion can occur through various mechanisms, in particular collapse in the interior of the sample [14–17] and escape through the boundary of the magnetic domain [16–18]. Two skyrmions can also merge to form a single skyrmion (and the reverse can also occur, i.e., a division of a skyrmion into two) [19]. The calculated lifetime estimates have taken into account the influence of a magnetic field [18], point defects [17], and the width of the track where the skyrmion resides [17]. Calculations have also been carried out for skyrmions in antiferromagnets [20,21]. Recent calculations have addressed how the various materials parameters, such as the Dzyaloshinskii-Moriya interaction (DMI) and anisotropy constants affect the activation energy for the collapse of a skyrmion [7]. The results show that the activation energy is not simply a function of the size of the skyrmion although the two tend to be correlated.

Fewer studies have been carried out on antiskyrmions. They are stabilized by anisotropic Dzyaloshinskii-Moriya interaction (DMI) while isotropic DMI stabilizes skyrmions [12,22]. Some aspects of antiskyrmions in systems with anisotropic DMI have been studied theoretically [13,23–25]. Antiskyrmions can also be stabilized by the magnetostatic interactions, for example, in ion-irradiated Co/Pt multilayer films [26]. Antiskyrmions have, furthermore, been discussed...
in relation to skyrmion-antiskyrmion pair production [27–29], in particular, in frustrated ferromagnetic films [30–32]. Monte Carlo simulations using parameters estimated from electronic density functional theory calculations have been used to simulate both skyrmions and antiskyrmions in the Pd/Fe/Ir(111) system and the predicted spin-polarized scanning tunneling microscopy images found to be similar [33]. Antiskyrmions as well as skyrmions in ferromagnetic films have been simulated using the micromagnetic approximation and the effect of the dipole-dipole interaction shown to provide larger stabilization for antiskyrmions [34]. The energy barrier for collapse cannot, however, be evaluated within the micromagnetic approximation since the collapse mechanism involves a singularity that requires a discrete lattice representation.

It is of great interest for potential spintronic applications to carry out more studies of antiskyrmions. Only a few calculations of antiskyrmions have been reported so far, and they have mainly focused on stabilization by frustrated exchange rather than the anisotropic DMI [31,35,36]. Simulation studies of the factors that affect thermal stability have, furthermore, been limited so far to rather small skyrmions that are unstable at room temperature. An important challenge is to extend the simulation methodology in order to make it applicable to high energy barrier for collapse resulting mainly from the dipole-dipole interaction shown to provide larger stabilization for antiskyrmions [23,38].

The parameters in the extended Heisenberg Hamiltonian are chosen here to mimic the Mn–Pt–Sn inverse Heusler compound where antiskyrmions have been observed over long time scale at room temperature [12]. The diameter of an antiskyrmion in this material has been measured to be approximately 150 nm, corresponding to 230 lattice constants, and accurate atomic scale modeling therefore requires a square lattice containing at least 900 lattice points, i.e., nearly a million spins. In order to evaluate the activation energy and estimate the lifetime of the antiskyrmion, it is necessary to use a discrete atomic lattice, rather than the continuum approximation invoked in micromagnetic simulations.

The parameters in the Hamiltonian used here are chosen to be consistent with the previously determined micromagnetic model parameters for this system [12]. There, the antiskyrmions at \( T = 300 \) K were modeled using the following parameter values: exchange stiffness \( A = 1.2 \times 10^{-10} \) J/m, Dzyaloshinskii-Moriya parameter \( d = 6 \times 10^{-3} \) J/m², saturation magnetization \( M_s = 445 \) kA/m, external field \( B = 0.29 \) T, zero anisotropy, and an in-plane lattice constant of \( a = 0.63 \) nm and out-of-plane lattice constant of \( c = 1.22 \) nm. These micromagnetic parameter values are converted to parameters for the atomic scale lattice Hamiltonian as \( J = 2cA = 1830 \) meV, \( D = acd = 29 \) meV, \( K = 0 \), and \( \mu = a^2cM_s = 1.37 \) meV/T. We note, however, that the micromagnetic simulations can only be used to determine these quantities relative to the exchange parameter, \( J \), so our calculations are carried out in terms of scaled parameters \( D/J = 0.016 \) and \( \mu/J = 7.5 \times 10^{-4} \) T⁻¹.

III. CALCULATIONS OF THE LIFETIME

The lifetime of a magnetic state can generally be described by an Arrhenius rate law, \( \tau = \tau_0 \exp(E_a/k_B T) \), where \( E_a \) is the activation energy for the annihilation event and \( \tau_0 \) is the so-called pre-exponential factor. The two parameters, \( \tau_0 \) and \( E_a \), can be estimated using the harmonic approximation to transition state theory (HTST) for magnetic degrees of freedom [39,40]. It is based on an analysis of the

\[
\mathcal{H} = - \sum_{(i,j)} [J \mathbf{S}_i \cdot \mathbf{S}_j + D_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j)] - \sum_i \left[ \mu \mathbf{B} \cdot \mathbf{S}_i + KS_{z_i}^2 \right].
\]

(1)
multidimensional energy surface of the system, describing how the energy depends on the angular variables specifying the direction of all the magnetic moments in the system. In the case of interest, the antiskyrmion corresponds to a local minimum on the energy surface, whereas the homogeneous ferromagnetic phase corresponds to the global minimum. The activation energy for annihilation can be estimated as the highest rise in energy along the minimum energy path (MEP) connecting the antiskyrmion minimum to the ferromagnetic minimum. The point of highest energy on the MEP corresponds to a first order saddle point on the energy surface. The MEP can be found using the geodesic nudged elastic band method [14]. The computational effort is reduced here by making use of prior knowledge about the shape of the MEP and by focusing only on a small part of the MEP near the maximum [41].

In HTST, the pre-exponential factor \( \tau_0 \) is related to the relative vibrational entropy of the initial and transition states as well as the flux through the transition state. The vibrational entropy is estimated by approximating the energy surface in the vicinity of the local minimum and the saddle point as quadratic functions to obtain the frequencies of the vibrational modes. The vibrational entropy of a state is then given by the product of the vibrational frequencies for that state. Normally this involves evaluating the eigenvalues of the Hessian matrix [39], but for large systems, this becomes a challenging calculation. Below, we briefly describe a more efficient method for evaluating \( \tau_0 \) that does not require the evaluation of the eigenvalues and makes it possible to carry out calculations for the large system studied here. Additional information about the method can be found in Ref. [42]. The lowest couple of eigenvalues of the Hessian are still calculated explicitly using the Lanczos method to ensure that only one negative eigenvalue is found at the obtained saddle point and to test for the possible presence of zero modes.

An atomic scale simulation of such a large system is computationally challenging because of the large number of variables. In order to reduce computational effort, we use the following scaling method. A sequence of calculations is carried out for systems with decreasing in-plane lattice constant, \( a \), and increasing number of spins in such a way as to keep the values of the parameters corresponding to the micromagnetic model constant. Letting \( a_N = a_1/N \) denote the in-plane lattice constant after \( N \) iterations and referring to the relationship between micromagnetic model parameters, which are kept constant, and atomic lattice parameters, which depend on the lattice constant, the following scaling relationships are obtained: \( D_N = D_1/N \) and \( \mu_N = \mu_1/N^2 \) while the exchange constant \( J \) is unchanged as it is independent of \( a \). The number of spins is \( 45N \times 45N \), starting from \( N = 1 \), and eventually reaching the \( 900 \times 900 \) when \( N = 20 \) giving spacing between sites that corresponds to the lattice constant of the Mn–Pt–Sn inverse Heusler compound. The calculation for an MEP for a given \( N \) starts from an initial guess obtained from the calculation with \( N = 1 \). The minimum energy path, as well as initial and saddle point configurations, for \( N = 1 \) are presented in Fig. 2. Figure 3 shows the spin configurations corresponding to the first three values of \( N \).

The pre-exponential factor is evaluated separately for each \( N \) but without having to determine the eigenvalues of the Hessian as has been done in previous calculations [39,40]. It is difficult to obtain high enough accuracy for the eigenvalues when the number of spins is so large. Since the dipole-dipole interaction is not included here explicitly, only the nearest neighbors interact making it possible to write the Hessian matrix in a block tri-diagonal form and thereby evaluate the determinant of the Hessian. The pre-exponential factor is then evaluated from the determinant directly without having to determine the eigenvalues. It can be written as

\[
\tau_0 = \frac{2\pi}{\lambda \Omega_0},
\]

where the factor \( \Omega_0 \) is a ratio of determinants of the Hessian at the initial state minimum \( H^{\text{min}} \) and at the saddle point \( H^{\text{sp}} \).
eigenvectors and eigenvalues of in spin-related basis without the evaluation of the whole set of numerically even for large systems since it can be computed with circles), as a function of the scaling parameter $N$. The inset shows the pre-exponential factor in the Arrhenius rate law for antiskyrmion collapse as a function of $N$ assuming $J = 110$ meV. The lattice parameter in the coarse grained simulation model corresponds that of the Mn–Pt–Sn inverse Heusler compound [12] when $N = 20$.

\[ \Omega_0 = \sqrt{\frac{\det H_{\text{min}}}{\det H^\text{sp}}} \]  \hspace{1cm} (3)

It is connected with the ratio of the entropy of the initial state and the entropy of the transition state, both evaluated within the harmonic approximation. The factor $\lambda$ is connected with the dynamics of the system through the transition state and is evaluated from a basis invariant expression as

\[ \lambda = \sqrt{\frac{b \cdot H^\text{sp} b}{|\xi|}}, \text{ with } b = \frac{\gamma \zeta}{\mu} S^\text{sp} \times \mathbf{e}, \]  \hspace{1cm} (4)

where $S^\text{sp}$ is the spin configuration at the saddle point, $\xi$ the negative eigenvalue of $H^\text{sp}$, $\mathbf{e}$ the corresponding eigenvector (a unit tangent vector to the MEP at the saddle point), and $\gamma$ the gyromagnetic ratio. This expression for $\lambda$ can be evaluated numerically even for large systems since it can be computed in spin-related basis without the evaluation of the whole set of eigenvectors and eigenvalues of $H^\text{sp}$ [21].

Figure 4 shows the energy of the antiskyrmion with respect to the uniform ferromagnetic state and the energy of the saddle point as a function of the scaling parameter $N$. The energy at the local minimum corresponding to the antiskyrmion almost reaches a constant as the parameter $N$ is increased, while the energy of the saddle point is still increasing at $N = 20$. The lattice effects are still strong at $N = 20$ and the Belavin-Polyakov limit [43] of $4\pi J$ has not yet been reached. For the full $900 \times 900$ lattice corresponding to $N = 20$, the antiskyrmion energy is found to be $E_m/J = 1.27$ and the saddle point energy $E_s/J = 11.38$. Thus, the energy barrier for the collapse of the antiskyrmion is $E_c/J = 10.11$. (See Ref. [44] for an animation of the MEP for antiskyrmion collapse when $N = 1$).

The largest uncertainty lies in the value of the exchange parameter, $J$. The value of exchange stiffness used in the micromagnetic modeling of Nayak et al. [12] corresponds to $J = 1830$ meV for the lattice representation. Even for a much smaller value of $J = 110$ meV, the activation energy for collapse is large, ca. 1 eV. However, the pre-exponential factor turns out to have a typical value of $10^{-12}$ s (see inset in Fig. 4). Together, these values give a lifetime of a month at room temperature. A larger value of $J$ would give even longer lifetime. This high stability is in good agreement with the reported experimental observations [12]. The reason for the long lifetime is the large activation energy for the collapse of the antiskyrmion in this material while the pre-exponential factor, which is related to entropic effects, has a value that is similar to what has been calculated previously for the collapse of small skyrmions [18].

**IV. CONCLUSIONS**

Calculations of the lifetime of large but submicron scale antiskyrmions in Mn–Pt–Sn tetragonal Heusler material are presented. The results are consistent with the observed stability at room temperature in recent experiments [12] and show that the long lifetime is due to large activation energy for collapse rather than entropic effects. Since the atomic scale representation of this system requires roughly a million spins, the calculations are challenging and are made possible by using a scaling approach to evaluate the activation energy and an improved method for evaluating the pre-exponential factor in the Arrhenius rate expression. The latter is possible because the dipole-dipole interaction is not included here. Previous studies using the micromagnetic approach have shown that the dipole-dipole interaction makes antiskyrmions more stable with respect to skyrmions [34]. The rate of collapse cannot, however, be evaluated from micromagnetic simulations but we expect that the inclusion of dipole-dipole interaction would further increase the activation energy while not affecting the value of the pre-exponential factor significantly.

**ACKNOWLEDGMENTS**

This work was supported by the Icelandic Research Fund, the Research Fund of the University of Iceland, and the Russian Science Foundation (Grant 19-42-06302). The calculations were carried out at the Icelandic Research High Performance Computing facility.


