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The effect of 15 wt.%Al₂O₃ addition on the equilibrium phase relations of CaO-SiO₂-TiO₂ system at 1400 °C in air

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Abstract: The combined processing of industrial wastes of titania-bearing slags with coal fly ash is an important part of the circular economy. In the present work, the effect of Al_2O_3 on the 1400 °C liquidus isotherms of the perovskite, rutile and tridymite primary phase fields in the $\text{CaO-SiO}_2\text{-TiO}_2\text{-Al}_2\text{O}_3$ system has been determined by employing a high-temperature equilibration-quenching technique, followed by X-ray Photoelectron Spectroscopy and Scanning Electron Microscopy-Energy Dispersive X-ray Spectrometry. Titanium was confirmed to be stable as TiO_2 in the present equilibria. The equilibrium solid phases of perovskite $\text{CaO}\cdot\text{TiO}_2$, rutile TiO_2 and tridymite SiO_2 were confirmed to be coexisting with the liquid oxide phase. The comparison of the addition of 0 to 15 wt.% Al_2O_3 was beneficial for expanding the primary phase field of perovskite to lower TiO_2 concentrations. Comparisons of the experimental 1400 °C isotherm with the predictions using FactSage and MTDATA databases confirmed some differences to the present experimental data, thus demonstrating the direction for updating the present thermodynamic titania-bearing oxide databases.

Keywords: Urban mining, titania-bearing slag, Al_2O_3 , phase diagram, perovskite, FactSage

Introduction

Urban mining^[1] has become a hot research topic due to the potential economic benefits from the high growth rate of solid waste and its high content of critical metals, e.g., Li, Co, Ni, Ti, and Al^[2,3]. The concept of urban waste has been extended from waste electrical and electronic equipment (WEEE), spent Li-ion batteries (LIBs), and magnet scrap, etc. to include industrial wastes,^[4] e.g., red mud, coal fly ash (a high Al_2O_3 waste), and titania-bearing furnace slags. The titania-bearing slags are by-products of the reduction smelting of vanadium titano-magnetite ore, producing 10 wt.% - 28 wt.% TiO_2 ^[5] from blast furnace smelting or 40 wt.% - 70 wt.% TiO_2 ^[6] from electric furnace smelting. In order to efficiently recover Ti values in the slag, different hydrometallurgical processes, including sulfuric acid leaching^[7], alkaline roasting-leaching^[8] and various pyrometallurgical processes including microwave assistant roasting^[9], supergravity separation^[10], and selective crystallization – separation^[11], have been proposed. In the pyrometallurgical processes, the key idea is to enhance the Ti element concentration in a titania-enriched phase by modifying the slag composition^[12]. Recent studies^[13, 14] have revealed that the addition of Al_2O_3 to titania-bearing slags has an effect on the precipitation of titania as perovskite (CaTiO_3), rutile (TiO_2), and anosovite ($\text{Al}_2\text{TiO}_5\text{-FeTi}_2\text{O}_5\text{-MgTi}_2\text{O}_5\text{-Ti}_3\text{O}_5$). Once the enhanced crystallization mechanism by addition of Al_2O_3 is explained thoroughly, it will provide the basis for the combined processing of urban wastes of titania-bearing slags with high Al_2O_3 -containing waste, such as coal fly ash.

The key to understanding the influence of Al_2O_3 on the precipitation behavior of titania-enriched phases is to clarify the effect of additions of Al_2O_3 on the equilibrium phase relations and isotherms. According to the composition characteristics^[15], titania-bearing slags can be described by the $\text{CaO-SiO}_2\text{-TiO}_2\text{-MgO-Al}_2\text{O}_3$ system. The core binary, ternary, as well as part of the quaternary systems, including CaO-TiO_2 ^[16,17], $\text{SiO}_2\text{-TiO}_2$ ^[18-21], $\text{Al}_2\text{O}_3\text{-TiO}_2$ ^[22-27], $\text{CaO-SiO}_2\text{-TiO}_2$ ^[28-30], CaO-MgO-TiO_2 ^[31], and $\text{CaO-Al}_2\text{O}_3\text{-SiO}_2\text{-TiO}_2$ ^[32], have been extensively investigated during the past decades, while the quaternary and quinary systems have received less attention. Zhao et al.^[33,34] carried out a series of equilibrium experiments in reducing conditions at carbon saturation, and the results were projected on quasi-ternary phase diagrams with fixed mass fraction ratios of $w(\text{MgO})/w(\text{CaO})=0.2\text{-}0.72$ and $w(\text{Al}_2\text{O}_3)/w(\text{SiO}_2)=0.4\text{-}0.6$. The equilibrium phase relations indicated the composition

range for anosovite. Correspondingly, Wang et al.^[35,36] designed compositions higher than 40 wt.% Al_2O_3 to explore the optimized composition range for anosovite primary phase in the systems of $\text{CaO-SiO}_2\text{-TiO}_2\text{-10wt.\% Al}_2\text{O}_3$ and $\text{CaO-SiO}_2\text{-TiO}_2\text{-10wt.\% Al}_2\text{O}_3\text{-5 wt.\% MgO}$ in air. Shi et al.^[37-45] determined the extent of the primary field of the perovskite phase for $\text{CaO-SiO}_2\text{-TiO}_2\text{-Al}_2\text{O}_3\text{-MgO}$ systems with lower than 30 wt.% TiO_2 at fixed (10 wt.% - 30 wt.%) Al_2O_3 and (0 wt.% - 15 wt.%) MgO . Moreover, commercial thermodynamic databases in MTDATA^[46], FactSage^[47], and HSC^[48] have been built based on different models. Nowadays, most of the databases are well optimized for low-order systems^[49,50]; however, significant inconsistencies occur in high-order systems due to the lack of experimental data. In conclusion, both the experimentally studied and calculated phase diagrams are far from being sufficient for understanding the boundaries of the primary fields of titania-enriched phases, which severely restricts the development of combined recycling processes for urban wastes.

Therefore, a long-term research focus on equilibrium phase relations has been conducted over the past years; an addition of 10 wt.% Al_2O_3 to the $\text{CaO-SiO}_2\text{-TiO}_2$ system was studied in our previous work^[51]. In this study, the equilibrium phase relations with a fixed addition of 15 wt.% Al_2O_3 for bulk composition were experimentally studied at 1400 °C in air. The computation predictions obtained by using FactSage and MTDATA database are compared to the experimental results. The aim of this study is to provide new data that can be used to update the thermodynamic database, and to provide important guidance for the development of combined recycling processes for titania-bearing slags and coal fly ash.

Experimental

High purity reagents were employed to avoid the influence of impurities, and oxide powders of CaO (99.99 wt.%), SiO_2 (99.99 wt.%), TiO_2 (99.8 wt.%), and Al_2O_3 (99.99 wt.%) from Alfa Aesar were carefully weighed in predetermined ratios into 0.15g samples. Then the weighed samples were carefully mixed and pressed into cylindrical buttons and stored in a desiccator before equilibration annealing. In the present research, the Al_2O_3 concentration was fixed to 15 wt.% to establish the effects on the $\text{CaO-SiO}_2\text{-TiO}_2$ system and its equilibrium phase relations.

The equilibrium experiments were conducted by a high-temperature gas-condensed equilibration–quenching technique^[52] in a vertical furnace (Nabertherm RHTV 120-150/18) with a temperature accuracy of ± 2 °C, as illustrated in Figure 1. The pressed sample was wrapped in a platinum foil suspended by a platinum wire in the even temperature zone of the tube furnace, in flowing air. The temperature of the uniform hot zone was first increased to 50 °C above the experimental temperature and kept at that temperature for 0.5 h to accelerate the dissolution processes for equilibrium, after which it was decreased to 1400 °C for a long enough time to guarantee that equilibrium was reached. Previous studies^[40-45, 53, 54] with different compositions and temperatures have confirmed that 24 h is sufficient for titania-bearing slags to reach equilibration; therefore, each sample was heated for 24 h at the equilibrium temperature.

After equilibrium was reached, the sample was quenched directly into the iced water placed below the vertical tube. The equilibrium phase assemblages were thus frozen from a high temperature to room temperature. The quenched sample was dried and mounted in epoxy resin, polished, and coated by carbon for EDS (Energy Dispersive X-ray Spectrometer; Thermo Fisher Scientific, Waltham, MA, USA) analysis.

The oxidation state of the titanium following the experiments was verified by XPS (X-ray Photoelectron Spectroscopy) measurements using a Kratos Axis Ultra system (Kratos Analytical Ltd, Manchester, UK), equipped with a monochromatic Al K α X-ray source. The measurement was performed using an analysis area of 0.3 mm \times 0.7 mm, with 80 keV pass energy and 1 eV energy step. Individual areas of C 1s, Si 2p, Ca 2p, Ti 2p, O 1s were recorded. An SEM (Scanning Electron Microscope; Tescan, Brno, Czech Republic) coupled with an UltraDry silicon drift EDS was used for characterizing the equilibrium micrographs and compositions. The standards (Astimex, Ontario Canada) utilized in the EDS analyses were rutile (Ti K α), quartz (Si K α), anhydrite (Ca K α), olivine (for O, K α), and metallic aluminum (for Al, K α). The raw EDS data were processed with NSS microanalysis software [50]. For each phase, at least six points or areas were randomly selected to ensure high accuracy, as indicated by the standard deviation of the average value. The Proza (Phi-Rho-Z) matrix correction procedure was employed for raw data processing before normalizing the analysis results [55].

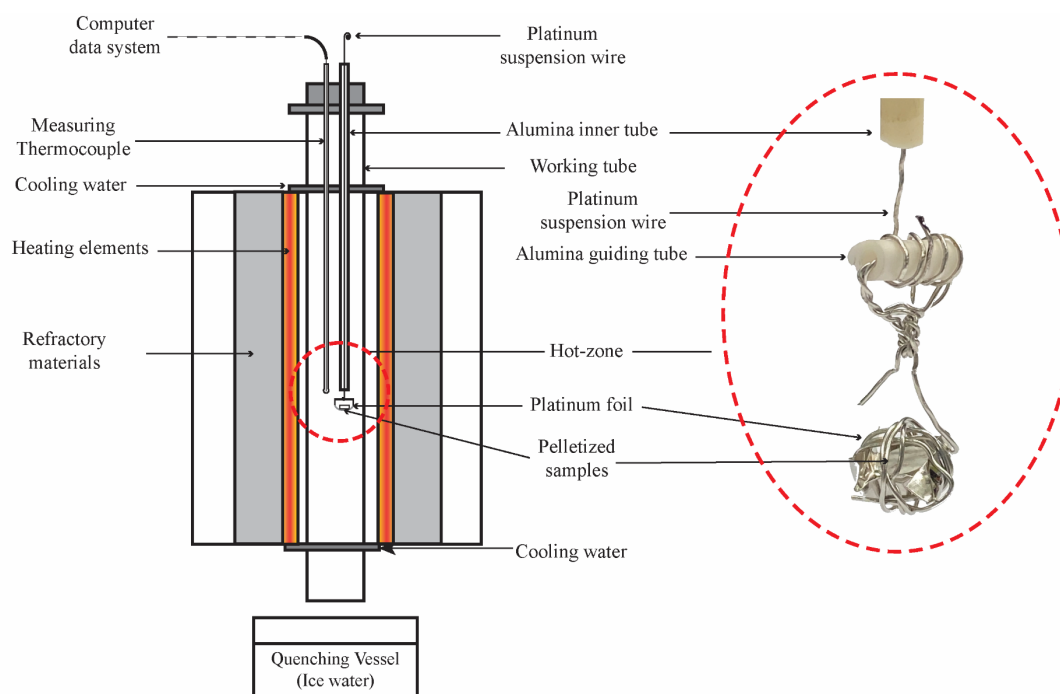
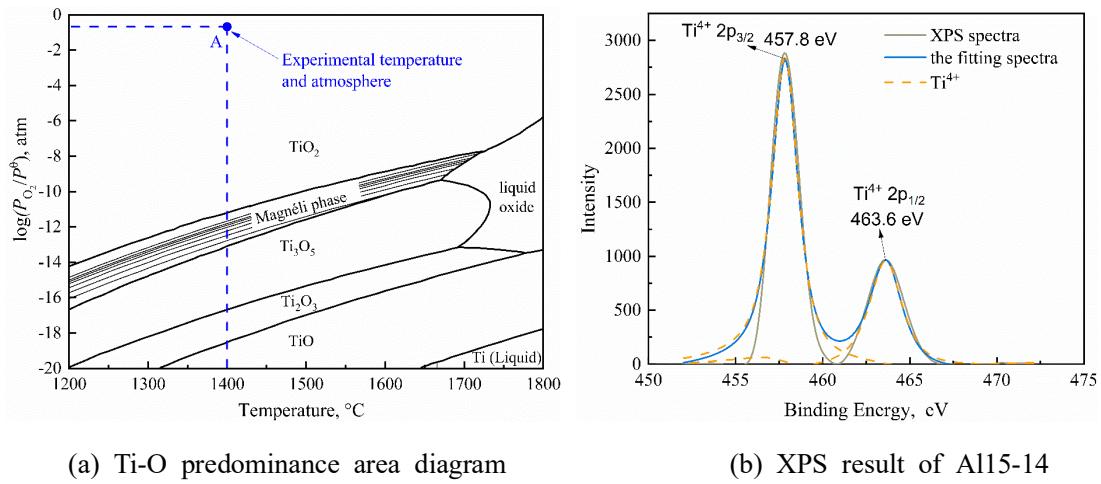


Figure 1. Graphical presentation of the vertical tube furnace used for the equilibrium experiments.

Results and Discussion

Determination of the oxidation state of Ti

It is essential to determine the oxidation state [56] when multi-valence elements are present in systems, such as titanium oxides in the quaternary CaO-SiO₂-TiO₂-Al₂O₃ system. As shown by the predominance phase diagram calculated by FactSage 8.0 [57] (Figure 2(a)), titanium can be stable as TiO₂, Magneli phases, Ti₃O₅, Ti₂O₃, TiO, and Ti, depending on the temperature and oxygen partial pressure. As indicated by label A in Figure 2(a), titanium should be stable as TiO₂ under the present experimental conditions, i.e., at 1400 °C in air. An equilibrated sample was delivered for XPS analysis (Figure 2(b)) and the XPS spectra verified that titanium was present as Ti⁴⁺ in the equilibrium conditions. Thus, the titanium oxide was expressed as TiO₂ for all samples in the present quaternary sections.



(a) Ti-O predominance area diagram (b) XPS result of Al15-14
Figure 2. Predominance phase diagram of the Ti-O system by FactSage (a) and the XPS spectrum for determining the oxidation state of titanium in the CaO-SiO₂-TiO₂-Al₂O₃ system in air of sample Al15-14 (b).

Equilibrium phase relations

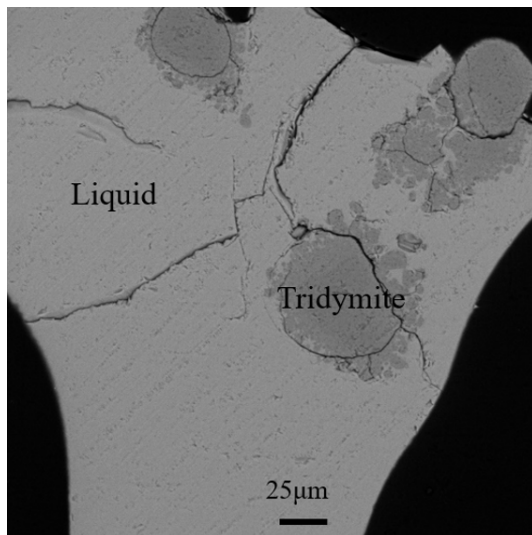
The SEM micrographs as well as the compositions of the equilibrium phases with fixed 15 wt.% Al₂O₃ in the CaO-SiO₂-TiO₂ system are presented in Figure 3 and Table 1. In the composition range studied in the present work, one single liquid phase region, three two-phase co-equilibrium domains (liquid with tridymite, rutile, and perovskite, respectively), and one three-phase co-equilibrium region (liquid coexisting with rutile and tridymite) were found.

In Figure 3(a), an example of a liquid-tridymite primary phase field is shown by sample Al15-2, indicating that the initial composition of this sample is located inside the primary phase field of tridymite. Similarly, the initial composition of sample Al 15-11 is within the primary phase field of rutile, as proved by the equilibrium result in Figure 3(b). In contrast, in Figure 3(c), a three-phase co-equilibrium is shown for sample Al15-3 with liquid coexisting with tridymite and rutile. According to the primary phase fields' adjacent rule^[58], the primary fields of tridymite and rutile are adjacent to each other. Furthermore, the liquid-perovskite primary field and single liquid are exhibited in Figure 3(d) and Figure 3(e) for samples Al15-23 and Al15-14, respectively.

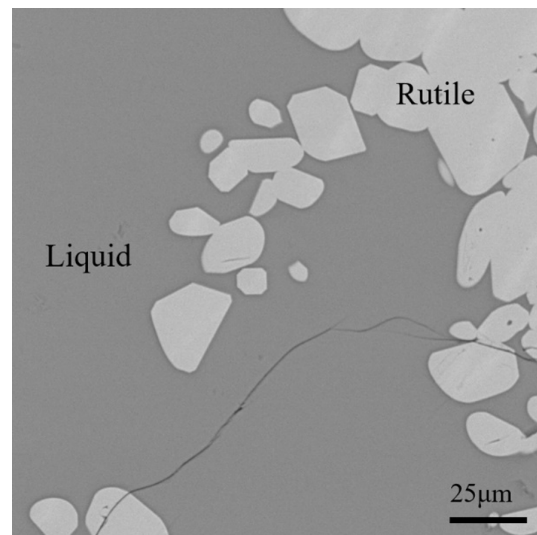
Table 1. The compositions for the equilibrium phases at 1400 °C in air.

No.	Initial compositions, wt. %				Equilibrium phases	Equilibrium compositions, wt. %				
	TiO ₂	SiO ₂	CaO	Al ₂ O ₃		TiO ₂	SiO ₂	CaO	Al ₂ O ₃	
<i>Liquid</i>										
Al15-12	5.00	40.00	40.00	15.00	Liquid	8.4 ± 0.1	39.9 ± 0.1	36.1 ± 0.1	15.7 ± 0.1	
Al15-13	10.00	37.50	37.50	15.00	Liquid	8.5 ± 0.1	40.0 ± 0.4	35.8 ± 0.5	15.7 ± 0.2	
Al15-15	20.00	32.50	32.50	15.00	Liquid	21.6 ± 0.1	32.8 ± 0.1	29.7 ± 0.1	16.0 ± 0.0(4)	
Al15-16	25.00	30.00	30.00	15.00	Liquid	26.8 ± 0.1	30.7 ± 0.1	27.3 ± 0.1	15.2 ± 0.0(4)	
Al15-17	30.00	27.50	27.50	15.00	Liquid	35.9 ± 0.3	25.5 ± 0.3	23.8 ± 0.1	14.9 ± 0.1	
Al15-18	35.00	25.00	25.00	15.00	Liquid	32.6 ± 0.1	21.8 ± 0.1	20.4 ± 0.1	25.2 ± 0.2	
Al15-19	40.00	22.50	22.50	15.00	Liquid	36.2 ± 0.1	25.3 ± 0.1	23.7 ± 0.1	14.8 ± 0.1	
<i>Liquid+ Tridymite</i>										
Al15-1	5.00	66.67	13.33	15.00	liquid	6.4 ± 0.7	65.0 ± 1.9	12.5 ± 1.4	16.1 ± 2.3	
					Tridymite	0.9 ± 0.1	97.1 ± 3.9	0.7 ± 0.2	1.4 ± 0.1	
Al15-2	10.00	62.50	12.50	15.00	Liquid	11.5± 1.8	63.1 ± 2.9	11.1 ± 1.4	14.4 ± 0.9	
					Tridymite	0.6 ± 0.1	99.3 ± 1.5	0.0	0.1 ± 0.0(3)	
<i>Liquid+Perovskite</i>										
Al15-14	15.00	35.00	35.00	15.00	Liquid	9.0 ± 0.1	30.9 ± 0.1	39.9 ± 0.0(4)	20.3 ± 0.0(3)	
					Perovskite	58.8 ± 0.1	0.2 ± 0. 0(3)	40.8 ± 0.1	0.2 ± 0.0(3)	
Al15-20	15.00	28.00	42.00	15.00	Liquid	12.1 ± 0.1	34.6 ± 0.1	36.6 ± 0.1	16.8 ± 0.2	
					Perovskite	58.1 ± 0.5	0.2 ± 0.1	40.9 ± 0.1	0.7 ± 0.2	
Al15-21	20.00	26.00	39.00	15.00	Liquid	16.0 ± 0.1	32.7 ± 0.2	32.3 ± 0.2	19.1 ± 0.4	
					Perovskite	58.3 ± 0.3	0.1 ± 0.0(4)	40.9 ± 0.1	0.7 ± 0.2	
Al15-22	25.00	24.00	36.00	15.00	Liquid	23.5 ± 0.1	28.8 ± 0.4	28.9 ± 0.2	18.8 ± 0.5	
					Perovskite	58.6 ± 0.3	0.1 ± 0.0(4)	40.8 ± 0.1	0.5 ± 0.2	
Al15-23	30.00	22.00	33.00	15.00	Liquid	29.6 ± 0.5	25.8 ± 0.5	26.7 ± 0.5	17.8 ± 0.4	
					Perovskite	58.6 ± 0.1	0.1 ± 0.0(2)	40.9 ± 0.1	0.5 ± 0.0(4)	
Al15-24	35.00	20.00	30.00	15.00	Liquid	37.5 ± 0.1	21.3 ± 0.1	25.3 ± 0.1	15.9 ± 0.1	
					Perovskite	58.4 ± 0.5	0.0	41.0 ± 0.7	0.5 ± 0.1	
<i>Liquid+ Rutile</i>										
Al15-4	20.00	54.17	10.83	15.00	Liquid	14.2 ± 0.8	57.8 ± 1.0	10.5 ± 0.4	17.5 ± 0.3	
					Rutile	98.5 ± 0.2	0.3 ± 0.1	0.4 ± 0.1	0.8 ± 0.0(4)	
Al15-5	25.00	50.00	10.00	15.00	Liquid	14.6 ± 0.4	55.6 ± 1.7	10.8 ± 0.4	19.0 ± 1.0	
					Rutile	98.5 ± 0.1	0.3 ± 0.0(4)	0.3 ± 0.1	0.9 ± 0.1	

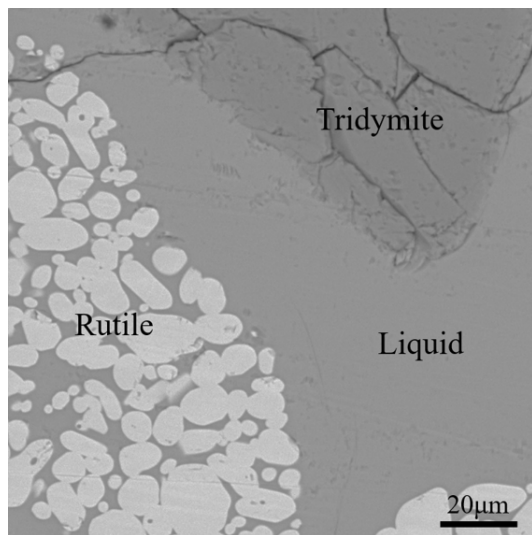
Al15-7	35.00	41.67	8.33	15.00	Liquid	13.7 ± 0.1	57.5 ± 0.1	$9.3 \pm 0.0(3)$	19.5 ± 0.1
					Rutile	98.1 ± 0.2	0.5 ± 0.1	$0.2 \pm 0.0(1)$	1.1 ± 0.2
Al15-9	30.00	39.29	15.71	15.00	Liquid	21.4 ± 0.3	46.1 ± 0.8	15.5 ± 0.2	17.0 ± 0.5
					Rutile	98.8 ± 0.1	$0.2 \pm 0.0(3)$	0.3 ± 0.1	$0.7 \pm 0.0(4)$
Al15-10	35.00	35.71	14.29	15.00	Liquid	22.6 ± 0.2	43.6 ± 0.1	15.9 ± 0.1	17.8 ± 0.2
					Rutile	98.9 ± 0.1	$0.2 \pm 0.0(3)$	0.2 ± 0.1	$0.7 \pm 0.0(4)$
Al15-11	40.00	32.14	12.86	15.00	Liquid	22.7 ± 0.3	42.7 ± 0.3	14.5 ± 0.1	20.1 ± 0.2
					Rutile	98.6 ± 0.3	0.3 ± 0.1	0.2 ± 0.1	$0.9 \pm 0.0(4)$
<i>Liquid+Tridymite+Rutile</i>									
Al15-3	15.00	58.33	11.67	15.00	Liquid	15.9 ± 1.5	59.0 ± 2.9	11.2 ± 1.1	13.9 ± 0.4
					Rutile	98.8 ± 0.1	$0.2 \pm 0.0(2)$	0.4 ± 0.1	$0.6 \pm 0.0(2)$
					Tridymite	0.9 ± 0.1	98.4 ± 1.3	0.0	$0.6 \pm 0.0(4)$
Al15-6	30.00	45.83	9.17	15.00	Liquid	14.5 ± 1.2	55.3 ± 2.9	10.0 ± 1.5	20.2 ± 1.5
					Rutile	98.5 ± 0.2	$0.3 \pm 0.0(4)$	$0.2 \pm 0.0(2)$	1.1 ± 0.2
					Tridymite	3.0 ± 0.2	95.9 ± 0.7	0.0	1.1 ± 0.3
Al15-8	40.00	37.50	7.50	15.00	Liquid	14.3 ± 0.2	53.4 ± 0.5	$9.4 \pm 0.0(2)$	22.9 ± 0.6
					Rutile	98.3 ± 0.3	$0.2 \pm 0.0(4)$	$0.2 \pm 0.0(2)$	1.2 ± 0.2
					Tridymite	$0.2 \pm 0.0(3)$	$99.8 \pm 0.0(1)$	0.0	0.0



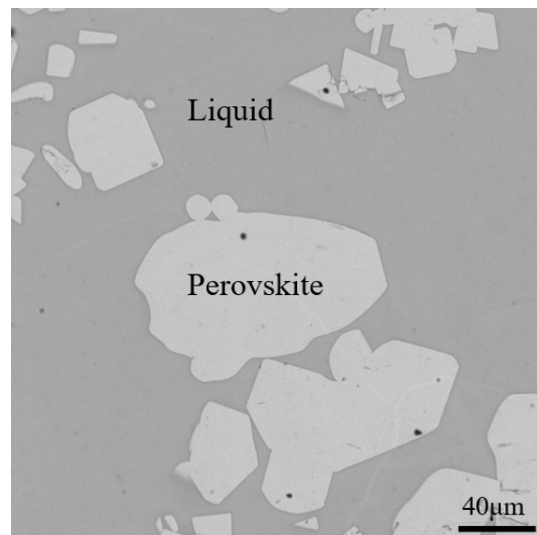
(a) Al15-2



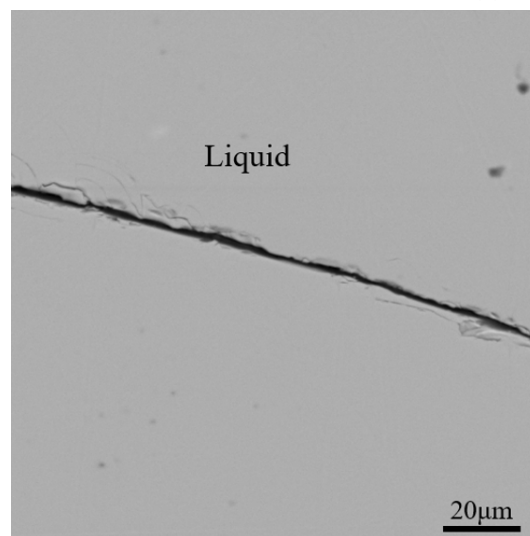
(b) Al15-11



(c) Al15-3



(d) Al15-23



(e) Al15-14

Figure 3. Micrographs for the equilibrium phase domains at 1400 °C in air for the CaO-SiO₂-TiO₂-15 wt.% Al₂O₃ system.

Projections of the 1400 °C isotherm

Based on the experimental results discussed above, the 1400 °C isotherm with the fixed addition of 15 wt.% Al_2O_3 was projected and plotted in the quasi-ternary $\text{CaO-SiO}_2\text{-TiO}_2$ triangle with solid lines, as shown in Figure 4. The normalization used for estimating the equilibrium compositions exactly on the 15 wt.% Al_2O_3 plane in the quaternary system of $\text{CaO-SiO}_2\text{-TiO}_2\text{-Al}_2\text{O}_3$ has been reported in detail in our previous publications [38-45].

The equilibrium liquid compositions were projected together with the liquidus isotherms and are shown in Figure 4. The computational prediction by FactSage 8.0 for the locations of the primary phase fields were also plotted, along with the experimental results. The calculation was done by employing the “FactPS” and “FToxid” databases [59] in the phase diagram module with the oxygen partial pressure P_{O_2} set to 0.21 atm. As can be seen in Figure 4, the predicted 1400 °C isotherm for the tridymite and rutile primary phase fields agrees well with the present experimental results. However, the calculated 1400 °C isotherm for the liquid-perovskite primary phase field shifts significantly to higher SiO_2 concentrations. This deviation may come from the description by the software itself that the oxide database related to TiO_x was mainly optimized in a reducing atmosphere for low-order systems.

The 1400 °C isotherm predicted by MTDATA 7.1 [46] was projected in Figure 5 for a comprehensive comparison with the present results and the calculations from FactSage. The MTDATA calculations were carried out by employing the Mtox 8.2 and Mtoxsup databases, where a full assessment of the $\text{CaO-Fe-Ti-O-MgO-Al}_2\text{O}_3\text{-SiO}_2$ system is available [60]. This means that, e.g., anorthite and plagioclase are terminal phases of a large solid solution phase called ‘feldspar’. Rutile, pseudobrookite, and perovskite are also solid solutions, whereas sphene (CaSiTiO_5) is a stoichiometric compound. In Figure 5, the 1400 °C isotherm predicted by MTDATA is labeled with dash-dot-dash lines. The major difference between FactSage and MTDATA is that sphene is not predicted to form as a primary phase by the Mtox database. Furthermore, the 1400 °C isotherm predicted by MTDATA is much more consistent with the present experimental results compared with the FactSage calculations. The experimental results of the present work are therefore important for the updating of present thermodynamic titania-bearing oxide databases.

The experimental results by DeVries et al. [61] and Chen et al. [51] were projected on Figure 6 to reveal the influence of 0 wt.% Al_2O_3 , 10 wt.% Al_2O_3 , and 15 wt.% Al_2O_3 on the 1400 °C liquidus isotherms in air. It can be concluded from Figure 6 that the addition of Al_2O_3 has an clear impact on the positions of the two-phase equilibrium isotherms. The addition of 10 wt.% and 15 wt.% Al_2O_3 was beneficial for extending the liquid-perovskite equilibrium to lower TiO_2 concentrations. This is useful for industrial applications for the modification of titania-bearing slag with an expanding composition range by a selective crystallization and separation technique. Similarly, the addition of 10 wt.% and 15 wt.% Al_2O_3 leads to the location of the liquid-rutile equilibrium isotherm moving to a lower TiO_2 and lower $w(\text{CaO})/w(\text{SiO}_2)$ ratio region, which results in the significant shrinkage of the liquid-tridymite equilibrium area.

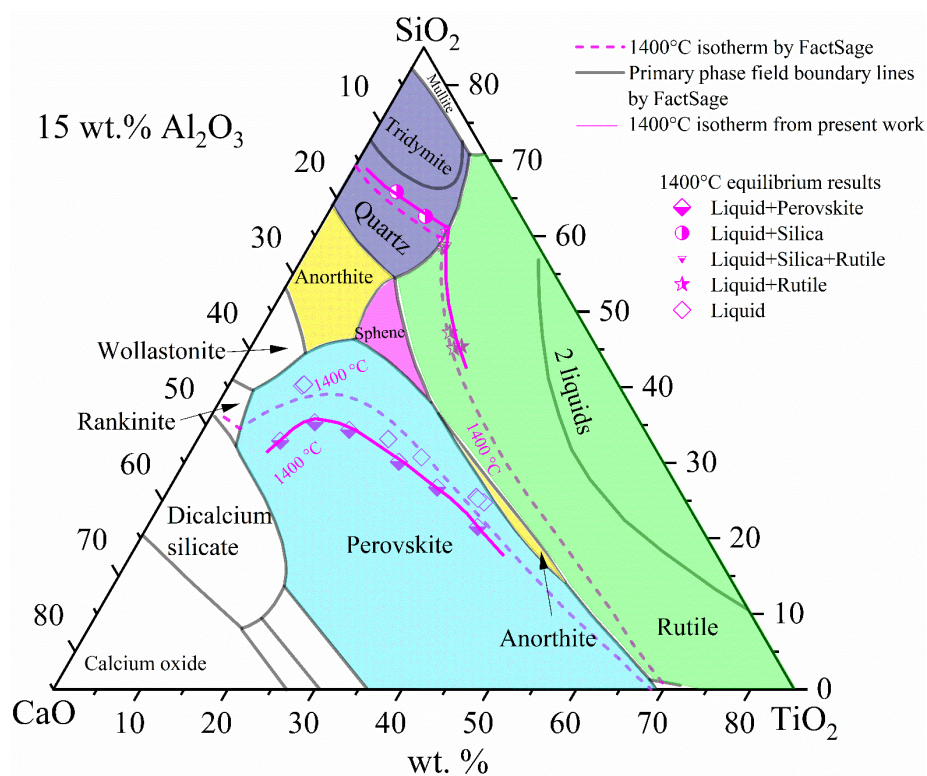


Figure 4. The 1400 °C liquidus isotherms for the CaO-SiO₂-TiO₂ system containing 15 wt.% Al₂O₃. The primary phase fields are described according to FactSage simulations.

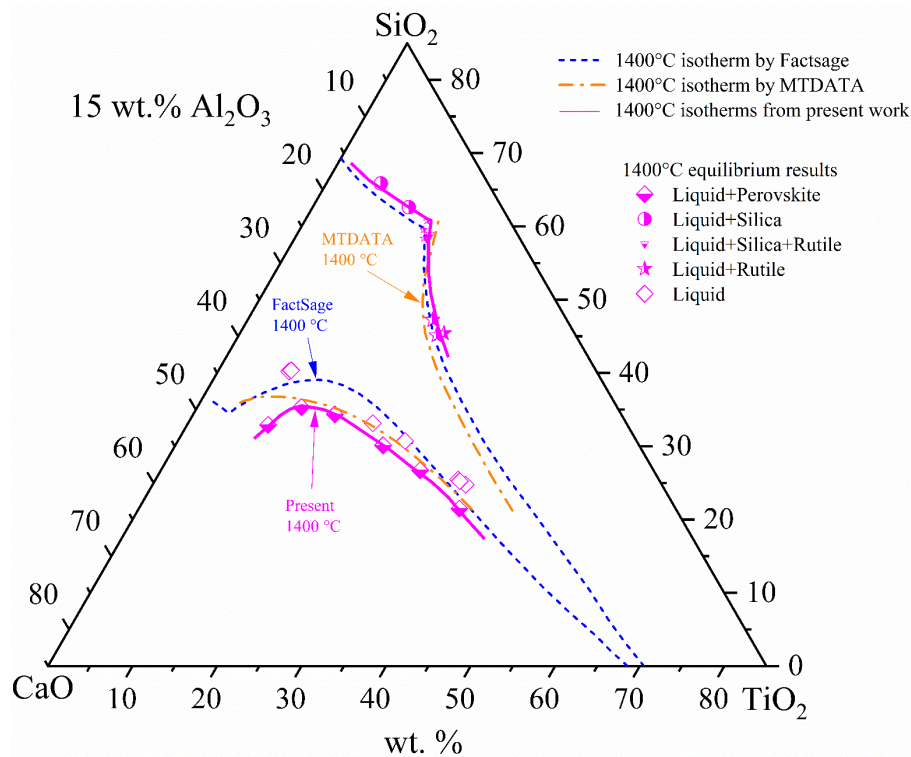


Figure 5. Comparison of the 1400 °C liquidus isotherms with the predictions by FactSage and MTDATA.

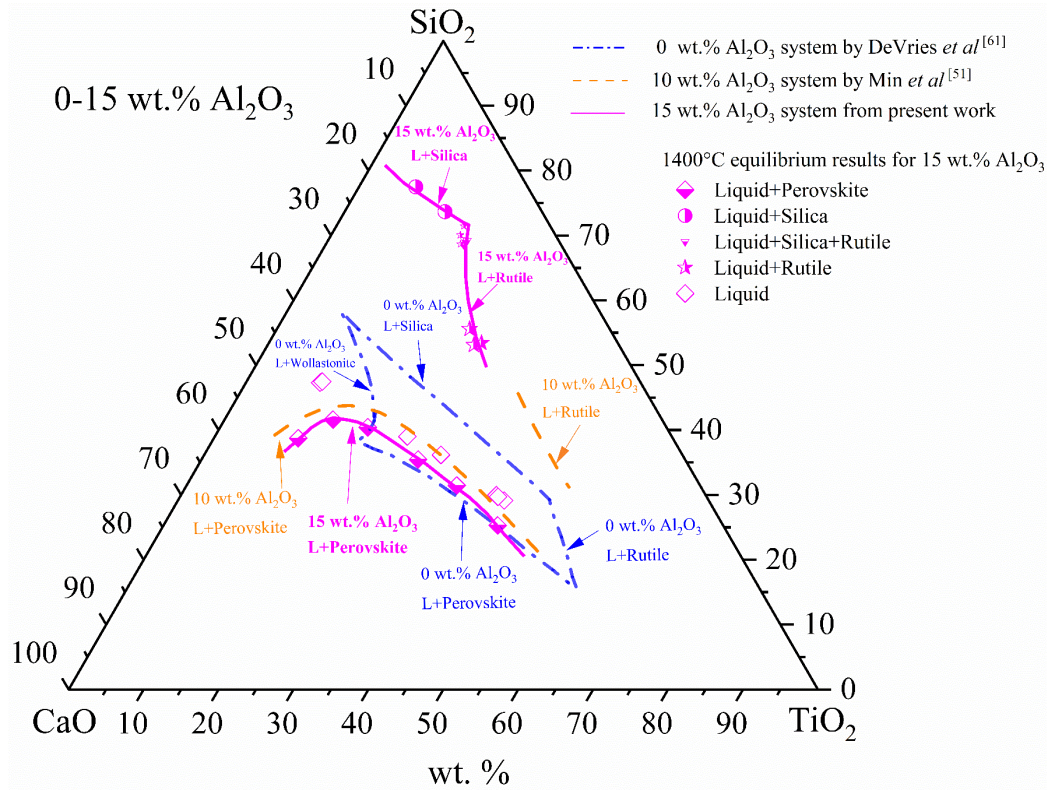


Figure 6. Projections of the 1400 °C liquidus isotherms for selected CaO-SiO₂-TiO₂-Al₂O₃ slag compositions on to the CaO-SiO₂-TiO₂ system.

Conclusions

In order to realize the combined recycling of titania-bearing slags and high Al₂O₃-containing wastes such as coal fly ash, the thermodynamic mechanism of the addition of Al₂O₃ in the equilibrium phase evolution was experimentally determined by a high-temperature thermodynamic equilibration-quenching technique. The results were compared with computational predictions by FactSage and MTDATA, as well as with results in the previous literature.

The XPS analysis confirmed that Ti was stable as TiO₂ under the present experimental conditions, confirming that the equilibrium phases containing Ti element can be expressed by the highest valence as Ti⁴⁺. The 1400 °C isotherm from the present work was projected onto the quasi-ternary phase diagram of CaO-SiO₂-TiO₂. The differences, confirmed by the comparisons with FactSage and MTDATA calculations, indicate the direction for updating the present thermodynamic titania-bearing oxide databases. This is important for providing accurate data and establishing the related process parameters.

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Disclosure statement

The authors report no conflicts of interest and the authors alone are responsible for the content and writing of the article.

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