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Salerno, Grazia

Topology puts solitons in the corner

Published in:
Nature Physics

DOI:
[10.1038/s41567-021-01282-4](https://doi.org/10.1038/s41567-021-01282-4)

Published: 01/09/2021

Document Version
Peer-reviewed accepted author manuscript, also known as Final accepted manuscript or Post-print

Please cite the original version:
Salerno, G. (2021). Topology puts solitons in the corner. *Nature Physics*, 17(9), 980-981.
<https://doi.org/10.1038/s41567-021-01282-4>

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1 PHOTONICS

2 **Topology puts solitons in the corner**

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4 Grazia Salerno, grazia.salerno@aalto.fi

5 Department of Applied Physics, Aalto University School of Science

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7 *Nonlinearity and topology are both linked to symmetries, but what happens when the*
8 *two are combined is not a trivial question. In a nonlinear photonic higher-order*
9 *topological insulator, solitons localize on the corners together with the topological*
10 *modes.*

11

12

13 Many physical phenomena are described as linear effects, even though nonlinearities
14 are important in a range of systems across the natural sciences. From fluids to atomic
15 condensates and optics, one hallmark of nonlinear systems is the soliton — a robust
16 and highly localized wave that doesn't change size or shape. Solitons are self-sustained
17 by a perfect balance between linear and nonlinear effects. But what happens to this
18 delicate balance when other localization effects are introduced? For example, one can
19 wonder if solitons can coexist with the localized edge states of a topological insulator.
20 Writing in *Nature Physics*, Marco Kirsch and colleagues have tackled this issue by
21 investigating the fate of topological boundary modes in the nonlinear regime of a
22 photonic system [1].

23

24 Topology is the study of the properties that are immutable under continuous
25 deformations. In condensed-matter physics, it was first applied to explain the quantum
26 Hall effect and topological insulators — bulk insulating materials that carry a perfectly
27 quantized transverse Hall current [2]. We now understand this quantum Hall current as
28 the transport of electrons through topological one-way states along a single-atom
29 layer on the edge of the system, and the existence of such edge states depends only
30 on intrinsic properties of the bulk. These states are characterized by a topological
31 invariant — a property that is constant under continuous deformations. If this invariant
32 is zero, the state has no specifically topological properties and is called 'trivial'. If it is
33 nonzero, the state is topological.

34

35 Topological concepts are no longer limited to condensed-matter systems, but appear
36 in every aspect of physics — from quantum mechanics to classical-waves like light.
37 Topological photonics, in particular, uses artificial structures specifically designed to
38 exhibit topological properties. Like the electronic states in a topological insulator, the
39 light propagation in such a non-trivial topological structure depends only on the
40 intrinsic design and not on external perturbations. This ability to control robust optical
41 transport is one of the main motivations for topological photonics. With the
42 demonstration of unidirectionally propagating edge states of light and topological
43 lasers, the field promises to deliver a range of applications.

44

45 If boundary modes of a standard topological insulator are localized at the edge, those
46 of higher-order topological insulators are located at the edge of the edge — corners
47 of a 2D system or hinges of a 3D system [3]. Higher-order topological systems require
48 the existence of crystalline symmetries of the lattice — such as inversion or mirror
49 symmetries — that affect how the electron density is centred within the unit cell, which
50 in turn determines the polarization of the crystal. In higher-order topological insulators,
51 the polarization is quantized, and a fractional charge accumulates on the corners of the
52 system.

53

54 So far, topological phases have mostly been studied in the linear regime, but work on
55 the effects of optical nonlinearities in photonic topological insulators has just begun [4,
56 5]. Kirsch and colleagues contributed to this recent effort by studying the role of
57 nonlinearities in higher-order topological systems. They used a system of coupled
58 waveguide arrays, arranged in a breathing kagome lattice (Fig. 1), which is known to be
59 a higher-order topological insulator model in the linear regime. By changing the
60 distance between the lattice sites, they realized two possible configurations: a
61 topological and a trivial one. Laser light entered the waveguides at the corner of the
62 lattice, propagated through the array by evanescently coupling to neighbouring sites,
63 and was collected at the end, where the intensity distribution on the detector provided
64 information about the lattice mode. Kirsch and colleagues introduced nonlinearities by
65 using a waveguide medium with a Kerr-type nonlinearity, such that the refractive index
66 depended on the light intensity.

67

68 For sufficiently high input power, solitons formed and the output light was confined
69 around the input waveguide. In the trivial case, the soliton was localized over the entire
70 unit cell of the lattice, whereas, for the topological case, the soliton was more strongly
71 localized on the corner site (Fig. 1). Kirsch and colleagues then calculated the
72 topological invariant, which for higher-order topological insulators is given by the bulk
73 polarization, to back up the different nature of these two types of corner modes.
74 Interestingly, the onset of nonlinearity proved not to be detrimental to the polarization
75 value, which remains non-zero in the topological case, and strictly zero in the trivial
76 configuration. Added nonlinearity therefore did not change the topological nature of
77 the modes. This analysis distinguishes between the emergence of nonlinear topological
78 corner states and the formation of trivial solitons in such structures.

79

80 The added nonlinearities had another effect: the bulk polarization was no longer
81 quantized, meaning that the symmetries protecting the topological corner modes were
82 broken. A very interesting scenario would be if nonlinearities could leave these
83 symmetries unbroken. Or even more strikingly if they could induce a non-trivial
84 topological phase starting from a trivial one. Preliminary steps in this direction have
85 been taken [6], but the study of nonlinear topological phases is still in its infancy. The
86 regime of strong nonlinearities is particularly interesting because it requires a quantum
87 optical description and genuine interaction-induced topological effects can appear [7,
88 8], which could result in the realization of strongly correlated topological phases of
89 photons.

90

91

92

93

94 Figure 1:

95 **Topological soliton formation.** An array of waveguides arranged on a
96 breathing kagome lattice is an optical model for a linear higher-order
97 topological insulator. Such a model has topological corner modes
98 originating from a nonzero bulk invariant. When the system enters a
99 nonlinear regime, the light becomes more localized and topological
100 solitons form on the corners of the system. This shows that the topological

101 order is robust against the onset of nonlinearity, leaving the bulk invariant
102 nonzero.

103

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