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*Published in:*
Monthly Notices of the Royal Astronomical Society

*DOI:*
10.1093/mnras/stab3059

*Published: 26/11/2021*

*Document Version*
Publisher's PDF, also known as Version of record

*Please cite the original version:*
Supernova induced processing of interstellar dust: impact of interstellar medium gas density and gas turbulence

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Accepted 2021 October 15. Received 2021 October 6; in original form 2021 August 31

ABSTRACT

Quantifying the efficiency of dust destruction in the interstellar medium (ISM) due to supernovae (SNe) is crucial for the understanding of galactic dust evolution. We present 3D hydrodynamic simulations of an SN blast wave propagating through the ISM. The interaction between the forward shock of the remnant and the surrounding ISM leads to destruction of ISM dust by the shock-heated gas. We consider the dust processing due to ion sputtering, accretion of atoms/molecules, and grain–grain collisions. Using 2D slices from the simulation time series, we apply post-processing calculations using the PAPERBOATS code. We find that efficiency of dust destruction depends strongly on the rate of grain shattering due to grain–grain collisions. The effective dust destruction is similar to previous theoretical estimates when grain–grain collisions are omitted, but with grain shattering included, the net destruction efficiency is roughly one order of magnitude higher. This result indicates that the dust-destruction rate in the ISM may have been severely underestimated in previous work, which only exacerbates the dust-budget crises seen in galaxies at high redshifts.

Key words: hydrodynamics – turbulence – supernovae: general – ISM: clouds – (ISM:) dust, extinction.

1 INTRODUCTION

Dust grains comprising silicates, iron oxides, and carbonaceous material are found throughout the interstellar medium (ISM). It is well established that evolved stars and supernovae (SNe) produce dust (Zhukovska, Gail & Trieloff 2008; Matsuur a et al. 2009; Gomez et al. 2012; Wesson et al. 2015; Niculescu-Duvaz et al. 2021), but dust grains are also consumed in star formation (e.g. Testi et al. 2012; Wesson et al. 2015; Zhukovska, Gail & Trieloff 2008; Matsuura et al. 2009; Gomez et al. 2012; Wesson et al. 2015; Niculescu-Duvaz et al. 2021), by the shock-heated gas. We consider the dust processing due to ion sputtering, accretion of atoms/molecules, and grain–grain collisions. These reduce the dust mass, change the shape of the grain-size distribution, and increase the gas-to-dust mass ratio (McKee 1989; Draine 1990; Jones et al. 1994; Slavin, Jones & Tielens 2004; Bocchio, Jones & Slavin 2014; Lakicˇevicˇ et al. 2015; Mattsson 2016). Consequently, high star-formation rates cause high rates of dust destruction, which seems at odds with the existence of massive starburst galaxies with very large dust masses at high redshifts (Bertoldi et al. 2003; Michałowski et al. 2010a; Michałowski, Watson & Hjorth 2010b; Gall, Andersen & Hjorth 2011a, b; Mattsson 2011; Watson et al. 2015).

Dust destruction by SN-induced processes is hard to quantify (see, e.g. Jones & Nuth 2011). The most commonly adopted calibration (based on the prescription by McKee 1989) for the solar neighbourhood suggests that the masses $M_{d,\text{gas}} = 800 M_\odot$ (corresponding to a present-day time-scale $\tau_{d,0} = 0.8$ Gyr) for carbonaceous dust and $M_{d,\text{gas}} = 1200 M_\odot$ ($\tau_{d,0} = 0.6$ Gyr) for silicates are the gas masses that are cleared of dust by a single SN event (Jones et al. 1994; Tielens et al. 1994). Similar gas masses are found by Slavin et al. (2015) and Hu et al. (2019) while the destruction time-scales can vary between 0.44 and 3.2 Gyr for carbonaceous dust and between 0.35 and 2 Gyr for silicates.

Dust grains can also grow by accretion of molecules, coagulation or ion trapping, thus providing a replenishment mechanism or even a dominant channel of dust formation (Draine 1990; Mattsson 2011; Kuo & Hirashita 2012; Kirchschlager, Barlow & Schmidt 2020). Radial distributions of dust in late-type galaxies suggest efficient grain growth by condensation in the ISM (Mattsson & Andersson 2012; Mattsson, Andersson & Munkhammar 2012; Mattsson et al. 2014b) and the overall levels of dust depletion in damped Lyα systems and quasar host galaxies point in the same direction (Kuo & Hirashita 2012; De Cia et al. 2013, 2016; Mattsson et al. 2014a). Overall, the interactions between the different types of grain processing mentioned above can be decisive for the average efficiency of dust condensation in the ISM and, obviously, also have a profound effect on the grain-size distribution.

In this paper, we study the survival rate of ISM dust when a single SN blast wave expands into an initially homogeneous ISM. We consider uniform ambient gas number density of 1 and 0.1 cm$^{-3}$, at rest and modestly perturbed, and compare effects on the dust transport, dust destruction, and grain growth. Hydrodynamic
Simulations with the PENCIL code (Pencil Code Collaboration et al. 2021) are used to mimic the expansion of the SN in the gas phase of the ISM, and post-processing simulations with the PAPERBOATS code (Kirchschlager et al. 2019) are used to model the dust evolution.

2 HYDRODYNAMIC SIMULATIONS

The simulations of the dust are applied to a background ISM gas modelling the hydrodynamics of an explosion of an SN. Each model is within a 3D periodic domain large enough to evolve the SN remnant beyond 1 Myr. The models have an equidistant grid resolution of 0.5 pc along each edge, sufficiently well resolved to obtain well converged solutions (Gent et al. 2020, 2021) and also to exhibit instabilities resembling Vishniac–Ostriker–Bertschinger (VOB) overstability (Vishniac 1983; Vishniac, Ostriker & Bertschinger 1985), Rayleigh–Taylor (RT), or potentially Richtmyer–Meshkov (RM) instability (Brouillet 2002).

The SN remnant is initialized by the injection of thermal energy $E_{th} = 10^{51}$ erg within a sphere of initial nominal radius of $R_0$, following a radial profile as

$$ E(r) = E_0 \exp \left[ -\left( r/R_0 \right)^2 \right], $$

where $r$ is the radial distance to the explosion origin, $R_0 = 2.5$ pc, and $E_0$ is the normalising coefficient set such that the volume integral of $E(r)$ is equal to $E_{th}$. This smooth profile has been found to avoid numerical artifacts, which more easily emerge when applying stepped or much steeper profiles in the injected energy distributions, while still recovering an expansion closely resembling the Sedov–Taylor solution well in advance of the snowplough phase of relevance to this study. The remnant origin is located on a grid point in the centre of the domain. The initial condition creates a blast wave, which rapidly evacuates the ISM from the origin of the sphere and continues to expand into the ambient ISM. Within a short time, still within the adiabatic expansion phase of the SN lifespan, the properties of the remnant converge to a solution fitting the Sedov–Taylor analytic solution (Taylor 1950; Sedov 1959)

$$ R = \left( \frac{E_{th}}{\rho_0} \right)^{1/5} t^{2/5}, $$

where $R$ is the remnant radius, $\rho_0$ is the ambient gas density, and $\kappa \approx 2.026$ is the dimensionless parameter for $\gamma = 5/3$ (Ostriker & McKee 1988). We neglect any additional mass from the SN ejecta.

Non-adiabatic heating $\Gamma$ and cooling $\Lambda(T)$ are included (Gent et al. 2013b). Cooling by radiative losses follow Wolfire et al. (1995) and Sarazin & White (1987), using a piecewise power-law dependence of the cooling coefficient on temperature. The contribution from far-ultraviolet heating follows Wolfire et al. (1995, see Gent et al. 2013a), which vanishes for temperatures somewhat $\gtrsim 10^4$ K. When radiative cooling processes are included, the SN evolution changes. As the remnant expands and the shock front accumulates more gas from the ambient ISM, cooling becomes more efficient in the increasingly dense shell. Loss of energy more rapidly reduces the shell speed. As demonstrated by Gent et al. (2020) at resolution better than 1 pc our solution converges to the semi-analytical non-adiabatic solutions obtained by Cioffi, McKee & Bertschinger (1988), slightly modified to account for cooling in our model continuing to apply for $T < 10^4$ K.

To integrate these solutions we use the PENCIL code (Pencil Code Collaboration et al. 2021) for the system of non-ideal, compressible, non-isothermal HD equations

$$ \frac{D\rho}{Dt} = -\rho \nabla \cdot u + \nabla \cdot \xi D \nabla \rho, $$

$$ \frac{D\rho \nabla}{Dt} = -\rho c_s^2 \nabla \left( \frac{s}{c_p} + \ln \rho \right) $$

$$ + \nabla \cdot \left( 2 \rho \nu \nabla \right) + \rho \nabla \left( \xi \nabla \cdot u \right) $$

$$ + \nabla \cdot \left( 2 \rho \nu \nabla \right) - u \nabla \cdot \left( \xi \nabla \nabla \rho \right), $$

$$ \rho T \frac{D\rho s}{Dt} = E_{th} \sigma + \rho \Gamma - \rho^2 \Lambda $$

$$ + \frac{2 \rho \nu |\nabla|^2 + \rho \xi (\nabla \cdot u)^2}{2} $$

$$ + \nabla \cdot \left( \xi \rho \nabla s \right) + \rho T \nabla \xi \nabla \xi $$

$$ - \left( \xi \frac{\nabla \xi \nabla \rho \nabla \xi}{\xi \nabla \nabla \rho} \right), $$

with the ideal gas equation of state closing the system. Most variables take their usual meanings, with $\rho \nabla$ being the first-order traceless rate of strain tensor and $\nabla \nabla$ the second-order rate of strain tensor, to resolve grid-scale instabilities (see, e.g. Brandenburg & Sarson 2002; Haugen & Brandenburg 2004; Gent et al. 2021), with mesh Reynolds number set to be $\simeq 1$ for each $\delta x$. The incidence of SN denoted by $\sigma$ occurs once at $t = 0$.

In order to study the effects of gas density and turbulence on the evolution of the ISM gas impacted by a blast wave, we model the hydrodynamics of four different scenarios (Table 1). Initially, the gas temperature of the pre-shock gas amounts to $T_{gas} = 10^4$ K, the mean molecular weight is $\mu_{gas} = 0.531$ representing an ionized hydrogen gas, and the gas density is homogeneous with $n_{gas, 0} = 0.1$ cm$^{-3}$ or 1 cm$^{-3}$, respectively. Both shock velocity and gas temperature decrease with time as a result of expansion. For simulations without turbulence the pre-shock gas is in rest, while we adopt velocity fluctuations of 0.2 km s$^{-1}$ in the turbulent scenario which cause density inhomogeneities with ongoing time.

The spatial resolution of the simulations is 0.5 pc and the temporal resolution of the output frames is 250 yr. The total simulation time is for all scenarios 1 Myr which is similar to the expected time-scale for the existence of a SN blast wave before it is obliterated and cancelled out in the ISM due to density inhomogeneities and further

Table 1. Overview of the hydrodynamic simulation setup. The index (A–D) refers to a certain simulation setup. $n_{gas, 0}$ is the gas number density of the unperturbed ambient medium at $t = 0$, $n_{grid}$ is the number of grid cells in one dimension, and $l_{box}$ is the size of the domain in one dimension.

<table>
<thead>
<tr>
<th>Index</th>
<th>$n_{gas, 0}$ (cm$^{-3}$)</th>
<th>Turbulence</th>
<th>$n_{grid}$</th>
<th>$l_{box}$ (pc)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.1</td>
<td>No</td>
<td>512</td>
<td>256</td>
</tr>
<tr>
<td>B</td>
<td>1.0</td>
<td>No</td>
<td>512</td>
<td>160</td>
</tr>
<tr>
<td>C</td>
<td>0.1</td>
<td>Yes</td>
<td>512</td>
<td>256</td>
</tr>
<tr>
<td>D</td>
<td>1.0</td>
<td>Yes</td>
<td>320</td>
<td>160</td>
</tr>
</tbody>
</table>

\(^1\)https://github.com/pencil-code

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3 DUST PROCESSING

We use our post-processing code PAPERBOATS (Kirchschlager et al. 2019) to study the dust evolution in the turbulent or non-turbulent ISM gas when impacted by an SN shock wave. Based on the temporally and spatially resolved gas density, gas velocity, and gas temperature output of PENCIL, we investigate the dust transport and derive the dust-destruction rate. We give here a short overview of the processes considered and refer to Kirchschlager et al. (2019) for a detailed description.

3.1 Dust processes

PAPERBOATS is a dust processing code which simulates the dust transport as well as grain destruction and growth processes in a gaseous medium. The dust is accelerated by the streaming gas taking into account both collisional and plasma drag (Baines, Williams & Asebiomio 1965; Draine & Salpeter 1979). The calculation of the grain charges follows the analytical description derived by Fry, Fields & Ellis (2020) with respect to impinging plasma particles, secondary electrons, transmitted plasma particles, and field emission. The gas is assumed to be fully ionized. Destruction processes include thermal and non-thermal (kinematic) sputtering (e.g. Barlow 1978; Shull 1978; Tielens et al. 1994) as well as fragmentation and vaporization in grain–grain collisions (e.g. Jones, Tielens & Hollenbach 1996; Hirashita & Yan 2009). Growth processes comprise the coagulation (stickling) in grain–grain collisions and the accretion of gas on to the surface of the grains which are present either at low relative velocities or when the impact energy of a gas particle is below a certain threshold. The effect of ion trapping where ions that are responsible for sputtering events penetrate into the grain and get trapped (Kirchschlager et al. 2020) is not included in this study. Coulomb interactions between a gas ion and a charged dust grain in a sputtering event as well as between two charged grains in a grain–grain collision are taken into account as is the size dependence of the sputtering yield (Bocchio et al. 2012). Although PAPERBOATS is able to treat 3D simulations, we consider here only the central slice through the middle of the box of the PENCIL output (a single cell in z-direction) due to the large computational effort for highly resolved 3D post-processing simulations.

3.2 Dust model

The grains in our simulations are made of compact silicate material and assumed to be spherical with radius $a$. The initial grain-size distribution follows a power-law $a^{-\gamma}$ with index $\gamma = 3.5$ and minimum and maximum grain size $a_{\text{min}} = 5$ nm and $a_{\text{max}} = 250$ nm, respectively (MRN distribution; Mathis, Rumpl & Nordsieck 1977). The grain sizes are binned in 20 log-spaced size bins which range from 0.6 to 350 nm, allowing the dust to get partly destroyed or to grow due to destruction and growth processes. Dust particles with sizes below 0.6 nm is treated as completely destroyed and is assigned to the gas phase, known as ‘dusty gas’ (see Kirchschlager et al. 2019). The material parameters required for the dust post-processing (for sputtering, grain–grain collisions, and charging) are given in table 2 of Kirchschlager et al. (2019). Initially, the dust is at rest and homogeneously distributed in the domain with a gas-to-dust mass ratio of $\Delta_g d = 100$ (for comparison, in Appendix A we show the results for $\Delta_g d = 10$).

4 RESULTS AND DISCUSSION

4.1 3D hydrodynamic simulations of SN blast waves

We have performed simulations of an SN blast wave expanding in a 3D domain using the PENCIL code as described in Section 2. We present four different runs (see Table 1) where we consider both a low- and a high-density ambient ISM ($n_{\text{gas}, 0} = 0.1$ g cm$^{-3}$ and $n_{\text{gas}, 0} = 1.0$ g cm$^{-3}$, respectively) and explore possible effects due to turbulence induced instabilities (and overstabilities).

4.1.1 Low-density ISM

In Fig. 1, we show the resultant shell structure at $t = 1$ Myr for a blast wave propagating through an ISM gas with a uniform density $n_{\text{gas}, 0} = 0.1$ g cm$^{-3}$ at $t = 0$. Upper panels show a logarithmic density slice through the middle of the simulation box, while the lower panels show projected linear density, similar to what would be detected by observations. The left-hand panels show the case of a homogeneous ambient medium (simulation A, see index in Table 1) and the right-hand panels show the results including the turbulence-like initial velocity field (simulation C). The physical size of the shell at $t = 1$ Myr is ~220 pc across, which is somewhat larger than most observed SN remnants and about twice the size of the shell for the high-density case (see below). Moreover, we note that the low-density runs are prone to develop instabilities. The case without ‘turbulence’ (simulation A) shows only small perturbations in the shell, which we interpret as an example of artificial VOB overstability induced by limitations of the Cartesian grid. With ‘turbulence’ included (simulation C, right-hand panels in Fig. 1) we see a clear case of VOB overstability after ~500 kyr (also reflected in the dust, see Fig. 6). The VOB ‘wiggles’ appear to induce instabilities, which we interpret as being of RM type (Brouillette 2002), although it should be emphasized that it is difficult to tell from the simulation result, since the scale of the VOB ‘wiggles’ are of the order a few pc and thus the whole phenomenon is not sufficiently resolved (grid resolution: 0.5 pc).

4.1.2 High-density ISM

The typical average gas density in the local ISM of the Galaxy is $n_{\text{gas}, 0} \sim 1.0$ g cm$^{-3}$. Hence, we also present simulations of a blast wave propagating through an ISM gas with a uniform density $n_{\text{gas}, 0} = 1.0$ g cm$^{-3}$ at $t = 0$. Higher density means that the blast wave slows down faster, i.e. the shell structure is smaller (~140 pc across) and less evolved at $t = 1$ Myr. We chose not to continue the simulations (B and D) beyond this point, because a sound-to-noise ratio (SNR) will eventually merge with the ISM and is unlikely to survive much longer than 1 Myr (the oldest known SNR is the Lambda Orionis Ring with an estimated age of 1 Myr; Dolan & Mathieu 2002). In Fig. 2 (same as Fig. 1, but for $n_{\text{gas}, 0} = 1.0$ g cm$^{-3}$) we note that the characteristic ‘wiggles’ of the VOB overstability are present, but no secondary instabilities (‘plumes’ of RT or RM type) appear to have formed at 1 Myr. The lower right-hand panel of Fig. 2 also shows regions of enhanced density in the projected shell, which is consistent with what is seen in observations.
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4.1.3 Weakly turbulent ISM

In the context of dust processing, the most important difference between the $n_{\text{gas}, 0} = 0.1 \text{ g cm}^{-3}$ and $n_{\text{gas}, 0} = 1.0 \text{ g cm}^{-3}$ simulations is of course the density contrast. The shells of the shocked material in simulations B and D contain much more matter than the shells forming in simulations A and C. Compared to the high-density simulation with turbulence (D), the low-density simulation (C) shows more small-scale structure at and near the remnant shell, which may potentially amplify the dust processing (more about this in Section 4.2 below). In order to emphasize the instabilities induced by turbulence, we present in Fig. 3 cutouts of the shell structure at 1 Myr.

To get a handle on how much variance is caused by the turbulence in the background ISM, we have performed simulations corresponding to simulation C and D but without the SN blast wave (see Appendix B). In Fig. B1, we show the resultant gas-density structure (slices through the middle of the box) after 1 Myr of decay from the initial state with uniform density and a Kolmogorov (1941) velocity spectrum. We see that the velocity variations rapidly produce density fluctuations in the background and that the simulation corresponding to case D ($n_{\text{gas}, 0} = 1.0 \text{ g cm}^{-3}$) shows about twice as much relative variance in $\rho$ compared to case C ($n_{\text{gas}, 0} = 0.1 \text{ g cm}^{-3}$).

For the processing of dust grains the kinetic-energy variance of the background ISM is more important and we note that it is $\sim 25$ per cent larger for $n_{\text{gas}, 0} = 0.1 \text{ g cm}^{-3}$ compared to $n_{\text{gas}, 0} = 1.0 \text{ g cm}^{-3}$.

4.2 Dust processing induced by the shock wave

In Figs 4–7, we show the resultant evolution of the dust component from the post-processing runs with PAPERBOATS for all four simulations. The overall evolution is rather similar regardless of the different initial conditions.

We determine the dust mass survival rate $\eta = M/M_{t=0}$ after 1 Myr within a radius of 128 pc for the low-density case ($n_{\text{gas}, 0} = 0.1 \text{ cm}^{-3}$)
and within a radius of 70 pc for the high-density case \( n_{\text{gas},0} = 1.0 \text{ cm}^{-3} \). The radii are extended to encompass the secondary instabilities beyond the shell when background turbulence is considered. The dust survival rates for \( n_{\text{gas},0} = 1.0 \text{ cm}^{-3} \) are higher than for \( n_{\text{gas},0} = 0.1 \text{ cm}^{-3} \) (Table 2, Fig. 8). The higher gas density causes a slower evolution and thus smaller gas and dust velocities which reduces the destruction. On the other hand, the dust survival rates for \( \Delta_{gd} = 100 \) (Fig. 8) are between 67 and 80 per cent and for \( \Delta_{gd} = 10 \) (Fig. A2) between 43 and 55 per cent. This gives an indication of the importance of the gas-to-dust ratio \( \Delta_{gd} \) and implies that the dust-mass fraction being destroyed increases with the amount of dust initially present in the ISM (when the gas density is unchanged). A very dusty ISM will lose more of its dust due to destruction by SNe than a dust-poor ISM, conceptually hypothesized in, e.g. Mattsson et al.
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4.2.1 Creation of nano-sized grains

The top rows of Figs 4–7 show the formation and evolution of the 0.6 nm grains. Due to the initial minimum dust grain radius of 5 nm, smaller grains are not present at the beginning and have to be formed due to sputtering and grain–grain collisions. These small grains are well coupled to the gas and accumulate in a dust shell which is in conjunction with the shell of shocked gas.

Nano-sized grains are of fundamental importance for the rate of dust-mass destruction as they are much more easily destroyed by sputtering. This effect is even greater if the gas-to-dust mass ratio is lower than usual ($\Delta_{gd} = 10$ instead of 100), which results in an elevated grain–grain collision rate.

4.2.2 Intermediate-sized grains

For grains of intermediate sizes ($a \sim 10$ nm), all simulations display a distinct dust shell forming and efficient dust cleansing inside these shells. The low-density simulations (A and C) also show a secondary shell forming (see, in particular, the evolution of $a = 24$ nm grains in Figs 4 and 6), which is due to a reverse shock that appears early on and then 'bounces' at the origin and propagates outwards again.
A secondary shell is clearly visible at $t = 200$ kyr in Figs 4 and 6. These secondary shells (and reverse shocks in the dust) do not seem to affect the dust processing much, which is reasonable given that the density in the secondary shell is lower compared to the primary shell formed by the forward shock.

4.2.3 Destruction of large grains

The largest grains in our simulations ($a \gtrsim 100$ nm) are mainly destroyed by the SN shock as it propagates. However, the destruction is not due to direct ion sputtering of these large grains, but rather a result of destructive grain–grain collisions, i.e. grain shattering and vaporization. As outlined in Kirchschlager et al. (2019), grain–grain collisions and sputtering are synergistic processes. The destruction of grain mass is then the result of sputtering of the small splinters created by the shattering of large grains.

In simulation A (low density), large grains are effectively destroyed as the shock propagates outwards (see evolution for $a = 180$ nm in Fig. 4). In simulation B (high density), on the other hand, the SN ‘bubble’ is not only cleansed from large dust grains, but also large grains are accumulated in a dust shell building up in conjunction with the shell of shocked gas (see evolution for $a = 180$ nm in Fig. 5).

4.2.4 Evolution of the grain-size distribution

As large grains are partly destroyed by shattering and nano-sized grains formed in that process are sputtered away by the ionized gas, we expect some evolution of the grain-size distribution. Fig. 9 shows the resultant grain-size distribution at $t = 0$, 200, and 1000 kyr in case of $n_{\text{gas},0} = 0.1 \text{ cm}^{-3}$ (simulations A and C; left-hand panel) and $n_{\text{gas},0} = 1.0 \text{ cm}^{-3}$ (simulations B and D; right-hand panel).
Normalized to the gas density $n_{\text{gas}, 0}$, the typical number of nano-sized grains in the low-density cases after 1 Myr is more than twice of that in the high-density cases. Furthermore, large grains are also shattered at a higher rate if the overall matter density is low ($n_{\text{gas}, 0} = 0.1 \, \text{cm}^{-3}$), which is reflected in the shape of the grain-size distribution. This is completely in line with what we argued above: dust is destroyed by destructive grain–grain collisions combined with ion sputtering. The large grains are thus depleted while tiny grains are created. The shape of the grain-size distribution in the intermediate-size range is not much affected, however. The slope of the grain-size distribution of the debris from grain–grain collisions is similar to that of the MRN-like distribution we use for the initial ISM dust component. Thus, the shape of the grain-size distribution is retained in the intermediate-size range (roughly $a \sim 5 \cdots 50 \, \text{nm}$), while some evolution occurs in the small-grain end as well as in the large-grain end of the grain-size distribution.

Although the main effect on the large-grain end of the grain-size distribution is depletion due to shattering, some grains will actually grow and become bigger than the initial maximum grain size ($a_{\text{max}} = 250 \, \text{nm}$), which can be discerned in both panels of Fig. 9. The net growth is very small, however, and the growth processes (coagulation of grains and accretion of molecules on to grains) must be regarded as very inefficient and negligible in the first approximation.

4.2.5 Impact of weak ISM turbulence

Comparing the high-density cases (simulations B and D), adding ‘turbulence’ has little effect on the dust processing and the formation of a dust shell, while the increased number of density structures seen in the low-density case (simulation C) leads to a broader and less distinct dust shell. During the first $\sim 500 \, \text{kyr}$ we see essentially no
difference in the overall dust-destruction rate between simulations A and C (Fig. 8), which is mainly due to the fact that $u_s/u_{t,\text{max}} \gg 1$, where $u_s$ is the expansion velocity of the shell and $u_{t,\text{max}}$ is the maximum velocity of the background ‘turbulence’. As the expansion slows down and $u_s/u_{t,\text{max}} \sim 1$, the energy variance in the background becomes significant at the same time as instabilities can form. After $\sim 500$ kyr the dust-destruction rate is somewhat higher when turbulence is considered.

5 DESTROYED DUST MASSES AND DESTRUCTION TIME-SCALES

In order to emphasize the importance of grain–grain collisions for the destroyed dust masses as well as to compare our destruction rates with previous studies, we also conduct ‘turbulence’ simulations C and D without grain–grain collisions and consider only thermal and non-thermal sputtering as well as gas accretion (Section 5.1). The combined destruction by sputtering and grain–grain collisions is discussed in Section 5.2. The results for the dust mass survival rates, the total destroyed dust masses, and gas masses cleared of dust of all simulations are summarized in Table 2.
Figure 8. Evolution of the total dust mass within a distance of 128 pc (simulation A and C) or 70 pc (simulation B and D) from the explosion centre, respectively. Left-hand panel: Dust survival rate $\eta = M_t / M_0$ as a function of time. Right-hand panel: Destruction rate $dM/dt$ as a function of time.

Figure 9. Dust mass density per grain size for $n_{\text{gas}} = 0.1$ cm$^{-3}$ (left-hand panel) and 1.0 cm$^{-3}$ (right-hand panel). The initial dust mass density ($t = 0$) is shown as grey solid line and the final distribution with (without) turbulence as green (violet) solid line. The dashed lines show the distribution at $t = 200$ kyr.

5.1 Destruction by sputtering only

When the grain–grain collision rate is forced to zero, the net dust destruction is reduced by a factor of 10 (see Fig. 10, yellow lines). After $\sim$100 kyr (low density) or $\sim$30 kyr (high density), the gas temperature in the shocked shell drops below $10^5$ K while the relative velocity between gas and dust is not higher than 200 km s$^{-1}$. Following e.g. Goodson et al. (2016), sputtering becomes insignificant at those gas temperatures and velocities, and the slope of the destruction curve flattens. For the low-density case, the dust destruction saturates, while the higher gas density in simulation D even causes a slight dust mass growth due to gas accretion after 145 kyr. The destroyed dust mass after 1 Myr is $M_{\text{dust, dust}} = 5.6 M_\odot$ for $n_{\text{gas},0} = 0.1$ cm$^{-3}$ (dust survival rate $\eta = 97.4$ per cent within 128 pc) and $M_{\text{dust, dust}} = 8.0 M_\odot$ for $n_{\text{gas},0} = 1.0$ cm$^{-3}$ ($\eta = 97.7$ per cent within 70 pc). The gas mass cleared of dust, defined as $M_{\text{cl, gas}} = \Delta M_{\text{dust, dust}}$ (e.g. Hu et al. 2019), amounts to $M_{\text{cl, gas}} = 560 M_\odot$ for $n_{\text{gas},0} = 0.1$ cm$^{-3}$ and $M_{\text{cl, gas}} = 800 M_\odot$ for $n_{\text{gas},0} = 1.0$ cm$^{-3}$.

Figure 10. Destroyed dust masses for simulation A, B, C, and D (red and blue lines). Additionally, we show the results of turbulence simulations C and D when only sputtering as destruction process is considered (yellow lines).
We can also calculate the dust destruction time-scale\(^2\)

\[
\tau_{\text{destr}} = -\frac{t}{\ln(\eta)}
\]

as a function of time \(t\) (Fig. 11). Considering only sputtering as destruction process, \(\tau_{\text{destr}}\) amounts to \(\sim 40\) Myr for the low- and the high-density cases after 1 Myr.

We compare our results to previous studies that mainly model dust destruction in single SN blast waves. It is different to other destruction time-scales considering a tight coupling between gas and dust, they had to neglect grain–grain collisions and non-thermal sputtering. In the case of high-density cases after 1 Myr.

\(\eta = 70.2\) per cent and the destruction time-scale amounts to \(\tau_{\text{destr}} = 2.8\) Myr. For the other three simulations B–D, the destruction process, \(\tau_{\text{destr}}\) amounts to \(\sim 40\) Myr for the two high-density cases (simulation B and D), and \(\eta = 67\) per cent (\(\tau_{\text{destr}} = 2.5\) Myr) for the low-density case with turbulence (simulation C).

The destroyed dust masses are one order of magnitude larger and the destruction time-scales one order of magnitude smaller compared to dust destruction by pure sputtering (Section 5.1). As mentioned above, the destruction is evoked by the direct destruction in grain–grain collisions (catastrophic fragmentation, vaporization) but also by the proceeding sputtering of the small fragments. The masses of 64–70 M\(_\odot\) of dust destroyed by a single SN blast wave in a homogeneous medium are a big challenge for SNe as potential dust factories as well as for infrared observations of the Large Magellanic Cloud which showed that an average mass of 1.2–11.2 M\(_\odot\) of dust is removed per SN (Lakićević et al. 2015).

The significance of grain–grain collisions is also demonstrated by the collisional time-scale \(\tau_{\text{col}}\). As outlined in Kirchschlager et al. (2019), the collisional time-scale under the assumption of a single grain size is

\[
\tau_{\text{col}} = \frac{4 \Delta g_\text{d} \rho_{\text{bulk}} a}{3 m_{a.m.u.} \pi_{\text{gas}}} \frac{\tau}{\left(\pi_{\text{gas}}/\text{cm}^{-3}\right) \left(\pi/(\text{km s}^{-1})\right)} \text{Myr}, \tag{7}
\]

where \(a\) is the grain radius, \(\pi_{\text{gas}}\) is the mean gas number density, \(\tau\) is the mean relative velocity between the grains, and \(m_{a.m.u.}\) and \(\rho_{\text{bulk}} = 3.3\text{ g cm}^{-3}\) are the atomic mass unit and the silicate density, respectively. Assuming a typical gas density in the forward shock shell of \(\pi_{\text{gas}} = 10\text{ cm}^{-3}\) for \(n_{\text{gas},0} = 1.0\text{ cm}^{-3}\) (see bottom row in Figs 5 and 7), grains with radius \(a = 10\) nm, and a mean velocity \(\tau = 50\text{ km s}^{-1}\), the collisional time-scale is \(\tau_{\text{col}} \approx 112\) kyr, which is \(\sim 11\) per cent of the total simulation time. For \(n_{\text{gas},0} = 0.1\text{ cm}^{-3}\), the typical gas density in the forward shock shell is \(\pi_{\text{gas}} = 1\text{ cm}^{-3}\) (Figs 4 and 6) and the mean velocity is \(\tau = 100\text{ km s}^{-1}\), resulting in \(\tau_{\text{col}} \approx 560\) kyr. In both cases, the time-scale for grain–grain collisions is less than the simulation time, revealing that a significant number of grains is involved in grain–grain collisions.

5.2 Destruction by grain–grain collisions and sputtering

When taking grain–grain collisions into account, dust destruction is more efficient (Table 1). For the low-density case without turbulence (simulation A), 64.7 M\(_\odot\) of dust is destroyed and a gas mass of 6470 M\(_\odot\) is cleared of dust. This is related to a dust survival rate of \(\eta = 70.2\) per cent and the destruction time-scale amounts to \(\tau_{\text{destr}} = 2.8\) Myr. For the other three simulations B–D, the destruction process amounts to 4.5 Myr for the two high-density cases (simulation B and D), and \(\eta = 67\) per cent (\(\tau_{\text{destr}} = 2.5\) Myr) for the low-density case with turbulence (simulation C).

In summary, we can conclude that our results for the sputtered dust masses and the gas masses cleared of dust are consistent with masses derived in previous studies.
The outcome of the collisions depends strongly on the collision energy that declines with evolution time as the blast wave velocity and thus the relative velocity between dust grains decrease. Fig. 12 shows the number rate of dust grains involved in vaporization, fragmentation, bouncing, or sticking. Vaporization is the dominant process in the first 30 kyr only, followed by fragmentation (until 100 kyr), before non-destructive processes as bouncing and coagulation take over. While the number of dust grains that are vaporized is steeply falling with time ($\propto r^{-3}$), the effect of fragmentation decreases slowly ($\propto r^{-1}$). The fragmentation rate at 1 Myr is only a factor of $\sim 30$ below the maximum fragmentation rate at 30 kyr. We note that, although the total dust mass in the ambient ISM decreases with time, the total number of dust grains can even increase as initially large grains are fragmented into smaller pieces. This will increase the number of dust grains involved in vaporization, fragmentation, bouncing, and sticking to higher levels.

We can conclude that grain–grain collisions have a crucial effect on the total dust survival rate. Moreover, the temporal evolution of the remnant and in particular its blast wave velocity and gas density determine the predominance of different collision processes, starting with high energetic processes as vaporization over grain shattering down to non-destructive processes as bouncing and coagulation.

6 CONCLUSIONS

We have conducted 3D hydrodynamic simulations of an SN blast wave propagating through the ISM for an evolution time of 1 Myr. The late-stage evolution ($t \geq 0.1$ Myr), which is dominated by the interaction between the forward shock and the surrounding ISM, has been of primary interest as our aim has been to study the destruction of ISM dust. We calculated the dust processing due to sputtering, accretion of atoms/molecules, and grain–grain collisions (vaporization, fragmentation, and coagulation) in 2D slices from the output of the hydrodynamic simulations.

We have considered both a low ($n_{\text{gas,0}} = 0.1 \, \text{cm}^{-3}$) and a normal/high-density ISM gas density ($n_{\text{gas,0}} = 1.0 \, \text{cm}^{-3}$) and explored also the impact of adding a weakly compressive turbulent background, which means we have presented four different simulations. Our conclusions based on these simulations are:

(i) The SN blast wave creates an evacuated region around the explosion centre, surrounded by a shell structure of compressed gas.

(ii) Gas turbulence creates gas density fluctuations which evoke VOB overstabilities and RM instabilities at the forward shock region. For the low-density ISM, these instabilities can extend outwards to $\sim 125$ pc.

(iii) The dust survival rate for $n_{\text{gas,0}} = 0.1 \, \text{cm}^{-3}$ is lower than for $n_{\text{gas,0}} = 1.0 \, \text{cm}^{-3}$ ($67-70$ versus $80$ per cent) as a higher density means that the blast wave slows down faster. The dust survival rate for a gas-to-dust mass ratio $\Delta_{\text{gd}} = 10$ is lower than for $\Delta_{\text{gd}} = 100$ ($43-55$ versus $67-80$ per cent) as the larger grain number density increases the frequency of grain–grain collisions. For all studied scenarios, the largest dust survival rate is $80$ per cent for $n_{\text{gas,0}} = 1.0 \, \text{cm}^{-3}$ and $\Delta_{\text{gd}} = 100$.

(iv) For the low gas density, the destroyed dust masses are $10$ per cent higher when turbulence is considered. Turbulence has a negligible effect on the destroyed dust masses in the high-density case, for both gas-to-dust mass ratios $\Delta_{\text{gd}} = 10$ and $100$.

(v) Taking sputtering and grain–grain collisions into account, the total destroyed dust masses for a gas-to-dust mass ratio $\Delta_{\text{gd}} = 100$ are between $64.7$ and $71.6 M_\odot$ and the gas masses cleared of dust are $6470-7160 M_\odot$. Considering only sputtering in the turbulence cases, the total destroyed dust masses are $5.6-8.0 M_\odot$.

(vi) The time-scale for destruction by sputtering and grain–grain collisions within the front of the forward shock amounts to $2.5-4.5$ Myr. In contrast, $\sim 40$ Myr are required when only sputtering is considered.

It is well known that dust grains can form in the ejecta of core-collapse SNe and the derived dust masses are in the range of $\sim 0.1-1$ solar masses (Gall et al. 2014; Owen & Barlow 2015; Wesson et al. 2015; Bevan & Barlow 2016; Bevan, Barlow & Milisavljevic 2017; Bevan et al. 2019; Priestley, Barlow & De Looze 2019; Priestley et al. 2020; Niculescu-Duvaz et al. 2021). The dust masses destroyed in a homogeneous medium around the SN are much larger, even when only sputtering is considered. This makes SNe net dust destroyers and worsens the dust-budget crises seen in galaxies at high redshifts. Ways to reduce the amount of destroyed dust have been reported to be the extensive evacuation of the stellar environment in form of wind-blown bubbles before the explosion (Martínez-González et al. 2019), or the consideration of a more complex, turbulent multiphase ISM that mitigates the blast wave earlier (Hu et al. 2019). However, the impact of grain–grain collisions on these scenarios has to be studied in the future.

ACKNOWLEDGEMENTS

FK acknowledges funding from the European Research Council grant SNDUST ERC-2015-AdG-694520. LM acknowledges funding from the Swedish Research Council (Vetenskapsrådet), grant no. 2015-04505. FAG acknowledges support from the Academy of Finland ReSoLVE Center of Excellence (grant no. 307411) and the ERC under the EU’s Horizon 2020 research and innovation programme (Project UniSDyn, grant 818665). The hydrodynamic simulations were performed using computational resources provided by the Swedish National Infrastructure for Computing (SNIC) at the PDC Center for High Performance Computing, KTH Royal Institute of Technology in Stockholm.

DATA AVAILABILITY

The data underlying this article will be made available upon request.
REFERENCES

Gall C. et al., 2014, Nature, 511, 326
Komolgorov A., 1941, Dokl. Akad. Nauk SSSR, 30, 301
Mattson L., 2016, Planet. Space Sci., 133, 107
Ostriker J. P., McKee C. F., 1988, Rev. Mod. Phys., 60, 1
Pencil Code Collaboration et al., 2021, J. Open Source Softw., 6, 2807

APPENDIX A: DUST PROCESSING FOR $\Delta GD = 10$

The amount of destroyed dust and in particular the efficiency of grain–collisional destruction strongly depend on the number density of dust grains and thus on the gas-to-dust mass ratio $\Delta gd$. We conducted the post-processing simulations A–D using PAPERBOATS for $\Delta gd = 10$. The dust evolution for simulation C ($n_{gas} = 1.0$ g cm$^{-3}$, turbulence) is shown in Fig. A1 and the survival rates and grain-size distributions for all four set-ups in Figs A2 and A3.
Figure A1. Same as Fig. 6 (simulation C, $n_{\text{gas},0} = 1.0\ \text{g cm}^{-3}, \text{turbulence}$) but for the gas-to-dust mass ratio $\Delta_{\text{gd}} = 10$. 

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APPENDIX B: TURBULENCE-LIKE INITIAL VELOCITY FIELD

To quantify the variance in the ambient ISM density distribution that is caused by turbulence, we have performed simulations corresponding to C and D but without the SN blast wave (Fig. B1). Obviously, the velocity variations produce fluctuations in the gas. The logarithm of the normalized gas density varies up to $\sim 10$ per cent for $n_{\text{gas},0} = 0.1$ g cm$^{-3}$ and $\sim 30$ per cent for $n_{\text{gas},0} = 1.0$ g cm$^{-3}$. The normalized heating rate for $n_{\text{gas},0} = 1.0$ g cm$^{-3}$ is essentially proportional to $\ln \rho$, thus indicating a polytropic behaviour of the gas. The case with $n_{\text{gas},0} = 0.1$ g cm$^{-3}$, on the other hand, shows a heating pattern which is much less correlated with $\ln \rho$. This is the reason why simulation C has its peculiar pattern of instabilities, since a non-polytropic gas can be expected to be prone to small-scale instabilities. The range of the specific kinetic energy, $E_{\text{kin}} = \frac{1}{2} |\mathbf{u}|^2$, of the flow is, on the other hand, $\sim 25$ per cent greater for $n_{\text{gas},0} = 0.1$ g cm$^{-3}$ compared to $n_{\text{gas},0} = 1.0$ g cm$^{-3}$, which is crucial for the dust processing.

Figure A2. Same as Fig. 8 but for the gas-to-dust mass ratio $\Delta_{\text{gd}} = 10$.

Figure A3. Same as Fig. 9 but for the gas-to-dust mass ratio $\Delta_{\text{gd}} = 10$.
**APPENDIX C: DUST DESTRUCTION IN THE FIRST 100 KYR**

In order to highlight the dust destruction during the early years, we show in Fig. C1 the destruction curves (Fig. 10) on a logarithmic scale zoomed in to the first 100 kyr. We can see that for all simulation set-ups less than 0.3 $M_\odot$ of dust is destroyed within the first 1 kyr and less than 40 $M_\odot$ of dust within the first 100 kyr.

**Figure B1.** Gas-density structure (upper panels), normalized net heating rate (middle panels), and specific kinetic energy ($E_{\text{kin}} = \frac{1}{2} |u|^2$) distribution (lower panels) without SN blast wave after 1 Myr of decay from the initial state with uniform density and a Kolmogorov (1941) velocity spectrum. Left-hand panel: $n_{\text{gas},0} = 0.1 \text{ g cm}^{-3}$. Right-hand panel: $n_{\text{gas},0} = 1.0 \text{ g cm}^{-3}$. 

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Figure C1. The first 100 kyr of the destroyed dust masses and cleared gas masses on a logarithmic scale (line colours and types are the same as in Fig. 10).

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