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Spatially indirect intervalley excitons in bilayer WSe<sub>2</sub>

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Spatially indirect excitons with displaced wave functions of electrons and holes play a pivotal role in a large portfolio of fascinating physical phenomena and emerging optoelectronic applications, such as valleytronics, exciton spin Hall effect, excitonic integrated circuit, and high-temperature superfluidity. Here, we uncover three types of spatially indirect excitons (including their phonon replicas) and their quantum-confined Stark effects in hexagonal boron nitride encapsulated bilayer WSe<sub>2</sub> by performing electric field-tunable photoluminescence measurements. Because of different out-of-plane electric dipole moments, the energy order between the three types of spatially indirect excitons can be switched by a vertical electric field. Remarkably, we demonstrate, assisted by first-principles calculations, that the observed spatially indirect excitons in bilayer WSe<sub>2</sub> are also momentum indirect, involving electrons and holes from  $\Lambda$  and  $K/\Gamma$  valleys in the Brillouin zone, respectively. This is in contrast to the previously reported spatially indirect excitons with electrons and holes localized in the same valley. Furthermore, we find that the spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> can exhibit considerable, doping-sensitive circular polarization. The spatially indirect excitons with momentum-dark nature and highly tunable circular polarization may provide a firm basis for the understanding and engineering of technological applications in photonics and optoelectronics.

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Excitons, hydrogen-atom-like electron-hole pairs bound by their mutual Coulomb interaction, play an important role in a wide variety of intriguing optoelectronic properties of materials [1–4]. Depending on whether the wave functions of electrons and holes are spatially separated, excitons can be divided into two types: spatially direct and indirect excitons. Because of the separation of the electrons and holes, spatially indirect excitons have a much longer lifetime than spatially direct excitons and are predicted to exhibit a wide spectrum of emergent physical phenomena, including but not limit to quantum-confined Stark effect [5–7], Bose-Einstein condensation [8–14], strongly correlated excitonic insulator states [15–17], high-temperature superconductivity [18], valley physics [19–21], and dissipationless exciton transistors [22–24]. The recent emergence of two-dimensional transition metal dichalcogenides (TMDCs) and their van der Waals

(vdW) heterostructures offers an unprecedented platform to realize spatially indirect excitons. Indeed, spatially indirect excitons have thus far been demonstrated in a wide variety of TMDC homo- and heterostructures [19], such as MoS<sub>2</sub>/WS<sub>2</sub> [25–27], MoS<sub>2</sub>/WSe<sub>2</sub> [28,29], MoSe<sub>2</sub>/WSe<sub>2</sub> [20,22,30–33], and bilayer MoS<sub>2</sub> [7,34–39]. Specially, owing to the strongly reduced dielectric screening, spatially indirect excitons in homo-/heterobilayers of TMDCs possess substantial binding energies and show crucial advantages for applications, for example, superfluidity at high temperature [9].

To date, the studies of spatially indirect excitons have mainly focused on the momentum-bright species with electrons and holes localized in the same valley of the Brillouin zone (BZ) [7,19–25,29–42]. On the other hand, because of the existence of multiple electronic valleys, TMDC homo- and heterobilayers can also exhibit spatially indirect excitons with momentum-dark nature (that is, electrons and holes are from different valleys of the BZ) [6,28,43–45]. Since electrons and holes are further separated in momentum space, spatially indirect intervalley excitons, in principle, can possess a longer lifetime than spatially indirect but momentum-direct excitons and represent an advantageous scenario for numerous

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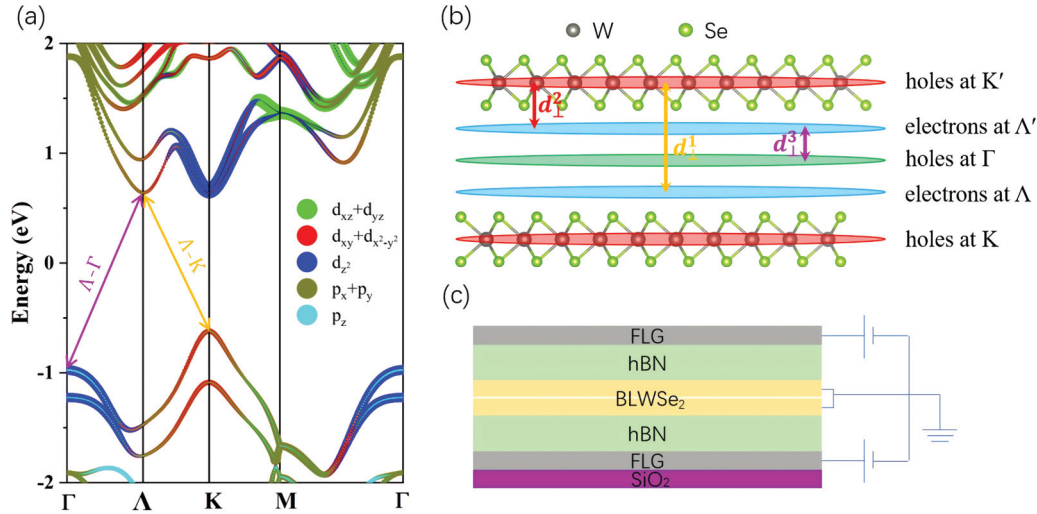


FIG. 1. (a) Orbital projected band structures of bilayer WSe<sub>2</sub>. Symbol size is proportional to its population in corresponding state. (b) Schematic image of the equivalent positions of spin-up wave functions at  $K/K'$  (red ellipses),  $\Lambda/\Lambda'$  (blue ellipses), and  $\Gamma$  points (green ellipse) in real space.  $d_{\perp}^{1-3}$  denote vertical distances between different wave functions. (c) Schematic of  $h$ -BN encapsulated bilayer WSe<sub>2</sub> device.

theoretical, experimental, and technological advances. However, in contrast to the well-studied spatially indirect excitons with momentum-bright features, experimental progress on spatially indirect intervalley excitons is still largely limited.

In this paper, we demonstrate three types of spatially indirect intervalley excitons (i.e., two  $\Lambda$ - $K$  transitions, one  $\Lambda$ - $\Gamma$  exciton, and their phonon replicas) and their quantum-confined Stark effects in hexagonal boron nitride ( $h$ -BN) encapsulated bilayer WSe<sub>2</sub> through the combination of electric field-dependent photoluminescence (PL) measurements and density functional theory (DFT) calculations. The energy order between the three types of spatially indirect intervalley excitons can be switched by an electric field, owing to their different electric dipole moments. Interestingly, these spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> show considerable negative circular polarization that is highly tunable with electron doping. Our results not only provide a complete understanding of the puzzling multiplet emissions in WSe<sub>2</sub> bilayers but also present possibilities for valleytronics, high-temperature superfluidity, and advanced functionalities in photonics and optoelectronics.

Among various TMDCs, bilayer WSe<sub>2</sub> provides a promising platform for spatially indirect intervalley excitons. First, for bilayer WSe<sub>2</sub>, the conduction band minimum is located at the  $\Lambda$  ( $\Lambda'$ ) points of the BZ, while the critical points of the valence band are at  $K/K'$  and  $\Gamma$ , as shown in Fig. 1(a) [46–49]. Consequently, the lowest exciton transition in bilayer WSe<sub>2</sub> should be momentum-indirect  $\Lambda$ - $K$  or  $\Lambda$ - $\Gamma$  excitons, in marked contrast to the momentum-direct  $K$ - $K$  transition in the monolayer case. Second, as the Bloch states at conduction band  $\Lambda$  and valence bands  $K$  and  $\Gamma$  have distinct orbital compositions [Fig. 1(a)], their wave functions show different interlayer hybridization and reside at different positions in real space [Fig. 1(b)] (Supplemental Material [50]) [47,51]. Therefore, momentum-indirect  $\Lambda$ - $K$  and  $\Lambda$ - $\Gamma$  excitons are also spatially indirect with finite out-of-plane electric dipole moments. Third, because of the substantial exciton-phonon coupling and the inevitable existence of defects [52–57],  $\Lambda$ - $K$

and  $\Lambda$ - $\Gamma$  transitions in bilayer WSe<sub>2</sub>, in principle, can be activated by phonon/defect scattering and show strong PL responses. Although there have been some studies on spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> [6,43,58–61], their underlying origin remains equivocal. In addition, previous researchers have reported only one type of  $\Lambda$ - $K$  exciton [6,43], the other type of  $\Lambda$ - $K$  transition and the  $\Lambda$ - $\Gamma$  exciton have not been revealed.

We fabricated high-quality  $h$ -BN encapsulated bilayer WSe<sub>2</sub> devices by a vdW-mediated dry transfer method (see Supplemental Material [50] for more details). Few-layer graphene was used as both the bottom and top gate electrodes to further screen the charged impurities on SiO<sub>2</sub> substrates and improve the device quality [Fig. 1(c)]. Three  $h$ -BN encapsulated bilayer WSe<sub>2</sub> devices (labeled as D1, D2, and D3) were studied, showing similar behavior (see Supplemental Material [50] for more details). Unless otherwise specified, the data presented here are taken from device D1 in a high vacuum at 10 K, excited by 1.96 eV (633 nm) radiation. The dual-gated devices enabled us to independently tune the vertical electric field ( $E_z$ ) and doping density ( $n_0$ ) (Supplemental Material [50]).

Figure 2(a) shows the PL spectrum of bilayer WSe<sub>2</sub> without applying gate voltages. Apart from the momentum-direct  $K$ - $K$  transitions at  $\sim 1.69$  eV ( $X_0$ ), seven lower energy peaks in the range of 1.50–1.65 eV (black dotted box), corresponding to the momentum-indirect transitions, can be clearly observed [6,59]. It is noteworthy that benefiting from the high quality of our samples, the number of momentum-indirect excitons revealed here is larger than that previously observed [6]. As we mentioned above, the momentum-indirect excitons in bilayer WSe<sub>2</sub> should also be spatially indirect. To confirm this, we performed electric-field-tunable PL measurements. Figure 2(b) depicts the color plot of PL spectra as a function of  $E_z$ . Obviously, all the momentum-indirect excitons are highly tunable with  $E_z$ , evidencing the quantum-confined Stark effects and their spatially indirect nature. Note that the emission energy of  $K$ - $K$  transition  $X_0$  remains unchanged

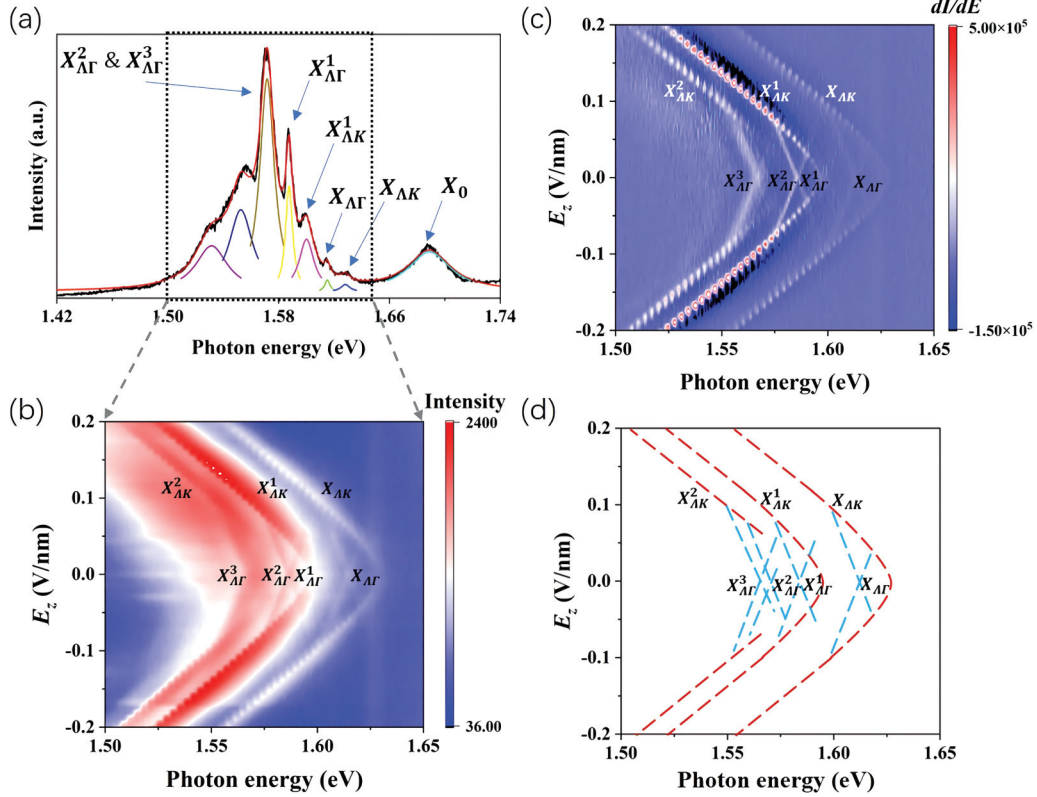


FIG. 2. (a) Photoluminescence (PL) spectrum of device D1 and its fitting under zero gate voltage. (b) Contour plot of the PL spectra as a function of photon energy (bottom axis) and  $E_z$  (left axis).  $n_0$  remains unchanged. (c) First-order energy derivative of (b). Spatially indirect intervalley excitons are labeled as  $X_{\Lambda K}$  ( $X_{\Lambda\Gamma}$ ),  $X_{\Lambda K}^1$  ( $X_{\Lambda\Gamma}^1$ ) and  $X_{\Lambda K}^2$  ( $X_{\Lambda\Gamma}^2$  and  $X_{\Lambda\Gamma}^3$ ) in sequence of decreasing emission energy. (d) Extracted emission energy as a function of  $E_z$  from (c) with red ( $X_{AK}$  and  $X_{AK}^{1,2}$ ) and blue ( $X_{\Lambda\Gamma}$  and  $X_{\Lambda\Gamma}^{1,2}$ ) dashed lines.

with  $E_z$  (Supplemental Material [50]). To better resolve the fine features, we plotted the first-order derivative of intensity ( $\frac{\partial I}{\partial E}$ ) [Fig. 2(c)]. Figure 2(d) displays the energies of different spatially indirect intervalley emissions as a function of  $E_z$ , extracted from Fig. 2(c). The spatially indirect intervalley excitons in bilayer WSe<sub>2</sub>, at first glance, can be divided into two types: one [blue dashed lines in Fig. 2(d)] with cross-shape features and the other [red dashed lines in Fig. 2(d)] with a conversion from nonlinear Stark shift at small  $|E_z|$  to linear Stark shift at large  $|E_z|$ .

We tentatively assigned the former (latter) type of spatially indirect intervalley excitons as  $\Lambda$ - $\Gamma$  ( $\Lambda$ - $K$ ) transitions. Note that, here, we use  $\Lambda$ - $K$  transitions to denote all the possible transitions between electrons at  $\Lambda/\Lambda'$  and holes at  $K/K'$  and the same for  $\Lambda$ - $\Gamma$  transitions. We extracted the vertical displacement of these excitons from Fig. 2(c) using  $d_{\perp} = -\frac{\partial E}{e \cdot \partial E_z}$ , where  $E$  is the emission energy, and  $e$  is the elementary charge. Note that the sign of  $d_{\perp}$  represents the direction of the electric dipole moment: positive (negative) means vertical upward (downward). For  $\Lambda$ - $\Gamma$  transitions, the  $d_{\perp}$  is nearly fixed at  $\pm 1.40$  Å [purple dots in Fig. 3(a)]. For  $\Lambda$ - $K$  transitions, the  $d_{\perp}$  is  $\sim \pm 1.80$  Å at zero electric field; then it gradually increases with the electric field; and finally, it saturates at  $\pm 4.50$  Å [yellow dots in Fig. 3(b)].

To support our assignment, we then performed DFT calculations to derive the equivalent positions of spin-up/down wave functions at conduction band  $\Lambda$  and valence bands  $K$  and  $\Gamma$ . The equivalent position of a wave function is defined

as  $r_z = \int_{-\infty}^{+\infty} r |\varphi(r)|^2 dr$ , where  $|\varphi(r)|^2$  denotes the probability density of wave function  $\varphi(r)$  at position  $r$ . The origin point (positive direction) is set as the midpoint between the two layers (vertical upward). For spin-up wave functions at conduction band  $\Lambda$  ( $\Lambda'$ ) and valence bands  $K$  ( $K'$ ) and  $\Gamma$ , the calculated equivalent positions at zero electric field are  $r_z = -0.22t$  ( $0.22t$ ),  $-0.48t$  ( $0.48t$ ) and  $0$ , respectively [Fig. 1(b)], where  $t = 6.6$  Å is the interlayer distance of bilayer WSe<sub>2</sub>. For spin-down wave functions, the equivalent positions can be obtained simply by time-reversal symmetry (Supplemental Material [50]). It is worth noting that the equivalent positions of  $\pm 0.48t$  indicate the virtually suppressed interlayer hybridization and spin-layer locking for holes at  $K/K'$  [62–64].

For  $\Lambda$ - $\Gamma$  transitions, there are two paths with equal transition probability [Fig. 3(c)]. One is from spin-up electrons at  $\Lambda$  to holes at  $\Gamma$  with  $d_{\perp} = r_z(\Gamma) - r_z(\Lambda_{\uparrow}) = 1.45$  Å, and another is from spin-down electrons at  $\Lambda$  to holes at  $\Gamma$  with  $d_{\perp} = r_z(\Gamma) - r_z(\Lambda_{\downarrow}) = -1.45$  Å. Here, we take transitions from  $\Lambda$  to  $\Gamma$  as an example; transitions from  $\Lambda'$  to  $\Gamma$  could give the same results (Supplemental Material [50]). Remarkably,  $d_{\perp}$  obtained by first-principles calculations ( $\pm 1.45$  Å) is in good agreement with the experiments ( $\pm 1.40$  Å), confirming our assignment of  $\Lambda$ - $\Gamma$  excitons [Fig. 3(a)].

For  $\Lambda$ - $K$  transitions (here, we focus on spin-up holes at the  $K$  valley), there are four possible transition paths [Fig. 3(d)], depending on the spin and valley configuration of carriers. It is noteworthy that spatially indirect intervalley excitons



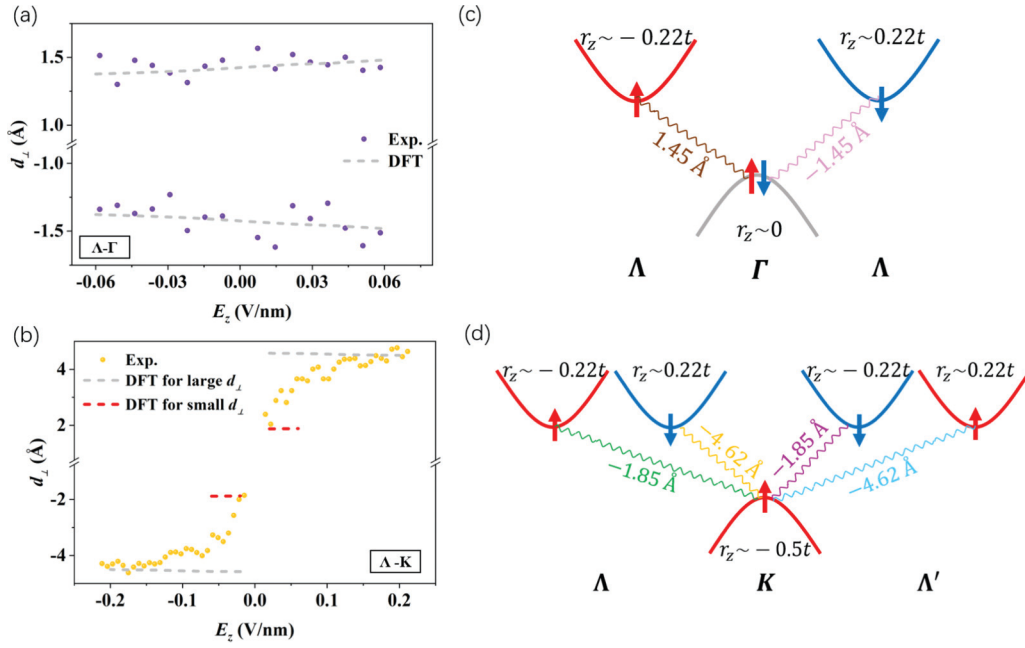


FIG. 3. (a) Experimental (purple dots) and calculated (dashed lines) vertical displacements of  $X_{\Lambda\Gamma}$  as a function of  $E_z$ . (b) Experimental (yellow dots) and theoretically calculated (dashed lines) vertical displacements of  $X_{\Lambda K}$  vs  $E_z$ . (c) and (d) Possible transition configurations of (c)  $X_{\Lambda\Gamma}$  and (d)  $X_{\Lambda K}$ .  $d_{\perp}$  of each configuration is denoted. Red (blue) curves represent spin-up (spin-down) bands. Valence  $\Gamma$  band is spin-degenerated.  $r_z$  denotes the equivalent position of wave function at zero electric field.

with spin-triplet configuration in bilayer WSe<sub>2</sub> may be bright because of the broken out-of-plane mirror symmetry [65]. Among the four possible transitions, two of them (i.e., transitions associated with spin-down electrons at  $\Lambda$  and spin-up electrons at  $\Lambda'$ ) have a large  $d_{\perp}$  ( $\sim -0.70t = -4.62$  Å), while the other two (i.e., transitions associated with spin-up electrons at  $\Lambda$  and spin-down electrons at  $\Lambda'$ ) have a small  $d_{\perp}$  ( $\sim -0.28t = -1.85$  Å) [Fig. 3(d)]. According to the spatial inversion symmetry, we know that, for spin-up holes at the  $K'$  valley, there are also four possible transitions but with opposite  $d_{\perp}$ : two of them with a large positive  $d_{\perp}$  ( $\sim 4.62$  Å) and the other two with a small positive  $d_{\perp}$  ( $\sim 1.85$  Å) (Supplemental Material [50]). For  $\Lambda$ - $K(K')$  transitions associated with spin-down holes, we can obtain similar results (Supplemental Material [50]). Again, a perfect agreement between theoretically calculated values and experimental results is obtained:  $d_{\perp} = \pm 1.85$  and  $\pm 4.62$  Å obtained by DFT calculations match the experiments under zero electric field ( $\pm 1.80$  Å) and large electric fields ( $\pm 4.50$  Å) well [Fig. 3(b)]. Note that first-principles calculations show that  $d_{\perp}$  change slightly with  $E_z$  [Figs. 3(a) and 3(b)]. For example, the large  $d_{\perp}$  of  $\Lambda$ - $K$  transition changes from  $\pm 4.62$  Å at zero electric field to  $\pm 4.50$  Å at  $E_z = 0.2$  V/nm, which is more consistent with our experimental results [Fig. 3(b)]. In short, we reveal three types of spatially indirect intervalley excitons: two  $\Lambda$ - $K$  transitions with different  $d_{\perp}$  and one  $\Lambda$ - $\Gamma$  exciton, providing a complete understanding of the multiplet emissions in bilayer WSe<sub>2</sub>.

Remarkably, our results manifest three unique features for these spatially indirect intervalley excitons. First, from the comparison of experimental results and first-principles calculations, it can be known that  $\Lambda$ - $K$  transition is dominated by the one with small  $d_{\perp}$  at  $E_z = 0$  and then gradually

becomes dominated by the one with large  $d_{\perp}$  as  $|E_z|$  increases. Such an exotic characteristic of the  $\Lambda$ - $K$  transition can be understood as follows. Since the wave functions of electrons and holes overlap more,  $\Lambda$ - $K$  excitons with small  $d_{\perp}$  possess larger binding energy than those with large  $d_{\perp}$ . As a result,  $\Lambda$ - $K$  excitons with small  $d_{\perp}$  have a lower energy and dominate the emission when  $E_z = 0$  (Supplemental Material [50]). When  $E_z$  is applied, the larger Stark shift would lead the  $\Lambda$ - $K$  transition with large  $d_{\perp}$  to having a lower energy and thus more occupancy than that with small  $d_{\perp}$ . Consequently, the  $\Lambda$ - $K$  transition with large  $d_{\perp}$  would gain an increasing contribution and eventually dominate the emission under a strong electric field (e.g.,  $|E_z| > 0.1$  V/nm). Note that, under an intermediate electric field, the emission is a mixed state, contributed by both  $\Lambda$ - $K$  transitions with large and small  $d_{\perp}$ . Second, for both  $\Lambda$ - $K$  and  $\Lambda$ - $\Gamma$  transitions, there are a series of replicas, labeled as  $X_{\Lambda K}^1$  ( $X_{\Lambda\Gamma}^1$ ),  $X_{\Lambda K}^{1,2}$  ( $X_{\Lambda\Gamma}^{1,2}$ ) and  $X_{\Lambda K}^{1,2,3}$  ( $X_{\Lambda\Gamma}^{1,2,3}$ ) in sequence of decreasing emission energy. For the two sets of highest-energy transitions (i.e.,  $X_{\Lambda K}$  and  $X_{\Lambda\Gamma}$ ), the emission intensities are much darker than that of their replicas at lower energy (i.e.,  $X_{\Lambda K}^{1,2}$  and  $X_{\Lambda\Gamma}^{1,2,3}$ ) [Fig. 2(b)], indicating that  $X_{\Lambda K}/X_{\Lambda\Gamma}$  and  $X_{\Lambda K}^{1,2}/X_{\Lambda\Gamma}^{1,2,3}$  have different origins. We tentatively attribute  $X_{\Lambda K}$  ( $X_{\Lambda\Gamma}$ ) and  $X_{\Lambda K}^{1,2}$  ( $X_{\Lambda\Gamma}^{1,2,3}$ ) to primary  $\Lambda$ - $K$  ( $\Lambda$ - $\Gamma$ ) transitions activated by defect scattering and their phonon replicas, respectively. Notably, the energy difference ( $\sim 42$  meV) between the primary  $X_{\Lambda K}$  ( $X_{\Lambda\Gamma}$ ) and the phonon replica  $X_{\Lambda K}^2$  ( $X_{\Lambda\Gamma}^3$ ) that dominates the emission outstrips the single phonon energy in WSe<sub>2</sub> ( $\sim 37$  meV) [56,66]. This indicates that phonon replicas come mainly from two-/multiphonon scattering, rather than one-phonon scattering. One plausible reason is that two-/multiphonon processes possess more scattering paths than one-phonon scattering. Third,  $X_{\Lambda\Gamma}$  is  $\sim 18$  meV lower than  $X_{\Lambda K}$  under zero electric field. This

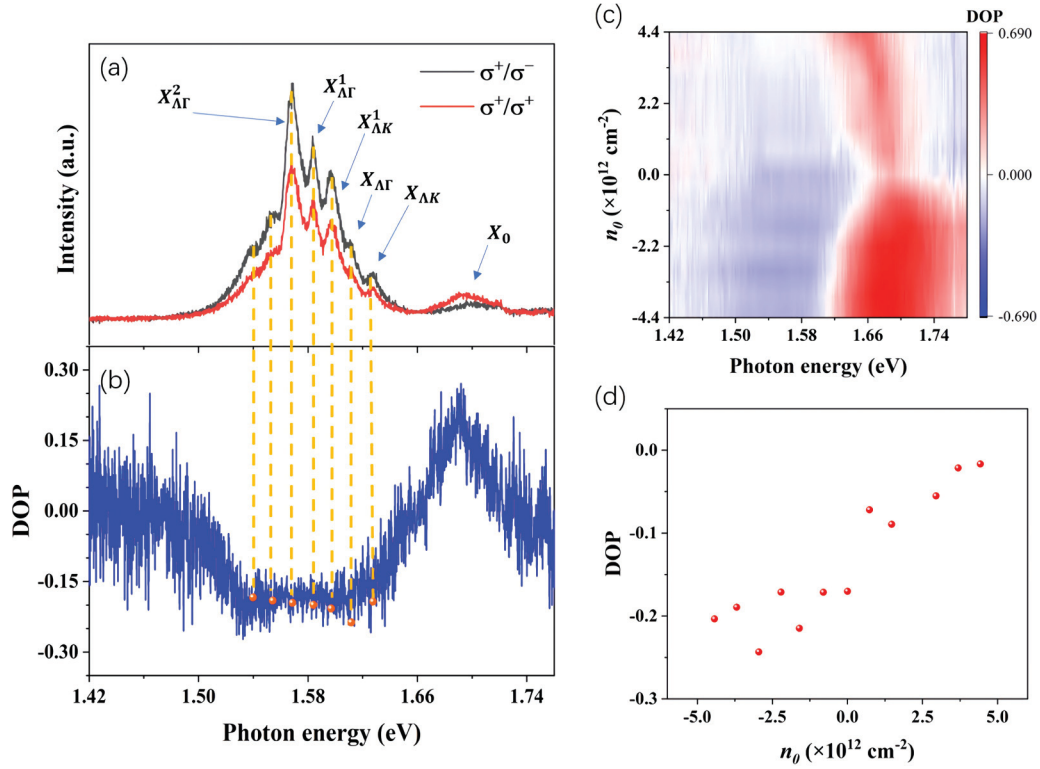


FIG. 4. (a) Photoluminescence (PL) spectra of device D2 under  $\sigma^+$  (red line) and  $\sigma^-$  (black line) detections, excited by  $\sigma^+$  light. (b) The degree of circular polarization (DOP) corresponding to (a) as a function of emission energy. DOPs calculated from the measured (blue line) and Lorentz-fitted intensities (orange dots) agree well with each other. (c) Contour plot of the DOP as a function of photon energy (bottom axis) and  $n_0$  (left axis).  $E_z$  remains unchanged. (d) The DOP vs  $n_0$ , calculated from the integral intensity in the energy range from 1.45 to 1.60 eV.  $n_0$  denotes the doping density induced by gate voltage.

seems a counterintuitive result because the valence  $\Gamma$  valley is located below the valence  $K$  valley [Fig. 1(a)] [6,49], which makes it natural to expect  $X_{\Lambda\Gamma}$  to have higher emission energy than  $X_{\Lambda K}$ . In fact, the observed transition energy is determined by the difference between the electronic bandgap and the exciton binding energy rather than electronic bandgap only. Since the effective mass of holes at the  $\Gamma$  point ( $\sim 1.01 m_e$ ;  $m_e$  is the free electron mass) is much larger than that at the  $K$  point ( $\sim 0.27 m_e$ ) [46,60],  $X_{\Lambda\Gamma}$  possesses a larger binding energy than  $X_{\Lambda K}$ , and thus, it can become the lower energy excitonic state.

Finally, we study the valley properties of spatially indirect intervalley excitons in bilayer WSe<sub>2</sub>. Figure 4(a) shows the helicity-resolved PL spectra of device D2 for cocircularly (red) and cross-circularly polarized detections (black), excited by  $\sigma^+$  radiation. We quantify the degree of circular polarization as  $\text{DOP} = \frac{I_{\text{co}} - I_{\text{cross}}}{I_{\text{co}} + I_{\text{cross}}}$ , where  $I_{\text{co}}$  and  $I_{\text{cross}}$  denote the intensities detected under co- and cross-circularly polarized configurations, respectively. Figure 4(b) shows the DOP against the photon energy: the blue line is calculated directly from the measured intensities, while the orange dots present the DOP of spatially indirect intervalley excitons calculated from the fitting intensities. It is explicit that DOPs calculated from the measured and Lorentz-fitted intensities of each exciton peak agree well with each other. Thus, for simplicity, all the following DOPs are calculated directly with the measured intensities. Obviously, both  $\Lambda$ - $K$  and  $\Lambda$ - $\Gamma$  transitions evince considerable negative DOP ( $\sim -0.2$ ),

whereas the momentum-direct  $K$ - $K$  transition has a positive DOP. Furthermore, we find that the DOP of spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> is highly tunable with doping density  $n_0$  [Fig. 4(c)]. Figure 4(d) shows the DOP as a function of  $n_0$ , calculated with the integrated intensity from 1.45 to 1.60 eV. The DOP almost keeps constant for hole doping but gradually vanishes with increasing electron doping density. Such negative, highly tunable circular polarization of spatially indirect intervalley excitons may provide device paradigms to exploit the valley degree of freedom other than  $K$  (e.g.,  $\Lambda$  and  $\Gamma$ ). In-depth theoretical studies, however, are required to fully figure out the optical selection rules/intervalley coupling mechanisms/the role of phonons and further the highly tunable negative circular polarization of spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> [67,68].

During the preparation of the manuscript, we became aware of a similar independent work by Altairy *et al.* [69]. Both our work and the work by Altairy *et al.* [69] clearly uncover the underlying origin of the multiplet emissions in bilayer WSe<sub>2</sub>, resolving previous debates. Meanwhile, our work unveils more features. First, our results demonstrate that there are two  $\Lambda$ - $K$  transitions with different  $d_{\perp}$  and with increasing  $E_z$ ,  $X_{\Lambda K}$  gradually changes from the one with small  $d_{\perp}$  to the one with large  $d_{\perp}$ , giving rise to the nonlinear Stark shift, while the work by Altairy *et al.* [69] only reveals the  $\Lambda$ - $K$  transition with large  $d_{\perp}$ . Second, we uncover the doping-tunable circular polarization of

these spatially indirect intervalley excitons and their phonon replicas, providing a firm basis for photonics and optoelectronics.

In summary, we reveal three types of spatially indirect intervalley excitons (i.e., two  $\Lambda$ - $K$  transitions, one  $\Lambda$ - $\Gamma$  exciton, and their phonon replicas) and their giant Stark shift in bilayer WSe<sub>2</sub> encapsulated by *h*-BN. Owing to their different electric dipole moments, the energy order and dominant luminescence between the three types of spatially indirect intervalley excitons can be switched by a vertical electric field. Remarkably, these spatially indirect intervalley excitons in bilayer WSe<sub>2</sub> show considerable negative circular polarization that is highly tunable with doping density. Our results not only provide a deep understanding of the multiplet momentum-dark emissions in bilayer WSe<sub>2</sub> but also hold a promising future for dissipationless exciton transport, high-temperature superfluidity, and valley-functional optoelectronic devices with multiple quantum degrees of freedom.

All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplemental Material [50]. Additional data related to this paper may be requested from the authors.

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The authors declare that they have no competing interests.

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